

MEASURING CONDITIONS AND UNCERTAINTIES  
FOR THE COMPARISON AND CALIBRATION  
OF NATIONAL DOSIMETRIC STANDARDS AT THE BIPM\*

P. J. Allisy-Roberts, D.T. Burns and C. Kessler



May 2011

BUREAU INTERNATIONAL DES POIDS ET MESURES

F-92310 Sèvres

\*This report supersedes the *Rapport BIPM-2009/04* by P. J. Allisy-Roberts, D.T. Burns and C. Kessler

**Table of contents**

	page
I. Introduction	3
II. General remarks	3
III. Comparison and calibration in terms of air kerma (x-rays, $^{60}\text{Co}$ , $^{137}\text{Cs}$ )	4
IV. Comparison and calibration in terms of absorbed dose to water ( $^{60}\text{Co}$ )	5
V. Comparison and calibration in terms of ambient dose equivalent ( $^{60}\text{Co}$ , $^{137}\text{Cs}$ )	5
VI. Use of calibration coefficients	6
VII. Comparison and calibration uncertainties	6
Table 1. X-rays (10 kV to 50 kV). Conditions of measurement at the BIPM	7
Table 2. X-rays (10 kV to 50 kV). Physical constants and correction factors used in the BIPM determination of the air-kerma rate	8
Table 3. X-rays (10 kV to 50 kV). Estimated relative standard uncertainties in the BIPM determination of the air-kerma rate	10
Table 4. X-rays (100 kV to 250 kV). Conditions of measurement at the BIPM	11
Table 5. X-rays (100 kV to 250 kV). Physical constants and correction factors used in the BIPM determination of the air-kerma rate	12
Table 6. X-rays (100 kV to 250 kV). Estimated relative standard uncertainties in the BIPM determination of the air-kerma rate	13
Table 7. $^{60}\text{Co}$ gamma radiation. Conditions of measurement at the BIPM	14
Table 8. $^{60}\text{Co}$ gamma radiation. Physical constants and correction factors used in the BIPM determination of the air-kerma rate, and their estimated relative standard uncertainties	15
Table 9. $^{60}\text{Co}$ gamma radiation. Physical constants and correction factors used in the BIPM ionometric determination of the absorbed-dose rate to water at $5\text{ g cm}^{-2}$ , and their estimated relative standard uncertainties	16
Table 10. $^{60}\text{Co}$ gamma radiation for radiation-protection level at 3.5 m. Physical constants and correction factors used in the BIPM determination of the air-kerma rate and ambient dose equivalent rate, and their estimated relative standard uncertainties	17
Table 11. $^{137}\text{Cs}$ gamma radiation. Conditions of measurement at the BIPM	18
Table 12. $^{137}\text{Cs}$ gamma radiation. Physical constants and correction factors used in the BIPM determination of the air-kerma rate, and their estimated relative standard uncertainties	19
Table 13. $^{137}\text{Cs}$ gamma radiation. Physical constants and correction factors used in the BIPM determination of the air-kerma rate at 3 m and the ambient dose equivalent rate, and their estimated relative standard uncertainties	20
References	21

**Abstract.** Information is presented on the experimental conditions used in the x- and  $\gamma$ -radiation beams at the BIPM for comparisons of national primary standards and calibrations of national secondary standards in terms of air kerma, absorbed dose to water and ambient dose equivalent, together with the uncertainties involved in the determination of these dosimetric quantities.

## I. Introduction

For each signatory of the Metre Convention and for a given type of measurement, the BIPM works with the National Metrology Institute or a laboratory designated nationally for the purpose (NMI). For those laboratories that hold national primary standards, the BIPM compares these standards against the BIPM reference standards, either directly using the primary standards in the BIPM reference beams or indirectly through the calibration of transfer instruments by both the BIPM and the national laboratory. For those that do not hold primary standards, the BIPM calibrates secondary standards that are then normally used as national reference instruments. For this reason, the chambers should be instruments of good quality; in particular with respect to leakage current and both short- and long-term stability.

Comparisons, characterizations and calibrations of ionization chambers are performed at the BIPM in terms of:

- air kerma in the low- (including mammography) and medium-energy x-ray ranges and in  $^{60}\text{Co}$  and  $^{137}\text{Cs}$  gamma radiations;
- absorbed dose to water in  $^{60}\text{Co}$  gamma radiation;
- ambient dose equivalent in  $^{60}\text{Co}$  and  $^{137}\text{Cs}$  gamma radiations.

The present report documents the conditions of measurement at the BIPM, the values for the physical constants and correction factors, and the estimated uncertainties in the determination of the primary quantities and of calibration coefficients.

## II. General remarks

The reference plane is specified in terms of a distance from the radiation source or, in the case of low-energy x-rays, from the beam exit window. The reference point is the intersection of the beam axis with the reference plane.

For chamber types other than parallel plate, the chamber is positioned with its axis in the reference plane and with the stated point of measurement of the chamber at the reference point. For measurements in gamma radiation the chamber is used with the build-up cap provided. The orientation of the chamber is such that the number or text inscribed on the stem faces the radiation source, unless a different orientation is indicated. Parallel-plate chambers are calibrated with the front surface of the chamber casing<sup>1</sup> in the reference plane, unless a different surface is indicated on the chamber, and with the entrance window centred on the beam axis.

All chambers are irradiated for at least thirty minutes, with the appropriate polarizing potential applied, before any measurements are made.

The leakage current is normally measured before and after each set of measurements and a correction applied based on the mean value. A chamber for which the relative leakage current is high, and in particular for which the leakage is also variable, is unsuitable for use as a transfer instrument and might also be considered unsuitable for calibration. In the latter case, a study note is issued.

---

<sup>1</sup> Clarification made subsequent to initial publication

The irradiation facilities at the BIPM are temperature controlled (close to 20 °C) at the level of around 100 mK. For air-kerma measurements in  $^{60}\text{Co}$  and  $^{137}\text{Cs}$ , an additional, passive enclosure is used to ensure temperature stability below 50 mK. The BIPM reference conditions for air temperature, pressure and relative humidity are  $T_0 = 293.15 \text{ K}$ ,  $P_0 = 101.325 \text{ kPa}$  and 50 % respectively. As the relative humidity is controlled within the range 47 % to 53 %, no humidity correction is applied.

Calibration of national standards: No correction is applied for lack of saturation; the air-kerma rate is stated in the certificate. For the thimble chamber types calibrated in gamma radiation, the radial non-uniformity correction for the BIPM beams is small and is stated in the certificate, although no correction factor is applied. In x-rays, chambers of larger dimensions may be calibrated and the radial uniformity of the beam shows more variation from one laboratory to another. For these reasons, the appropriate correction factor is always applied. For calibrations at radiation-protection levels in terms of ambient dose equivalent, the radial non-uniformity correction for the BIPM beams is stated in the certificate although no correction is applied as a similar correction is assumed at the national laboratory.

Comparisons of national standards: the measuring conditions are clearly stated in the comparison report.

### III. Comparison and calibration in terms of air kerma (x-rays, $^{60}\text{Co}$ , $^{137}\text{Cs}$ )

The primary standard, transfer chamber or national reference standard is operated in air at the stated reference distance. The ionization current  $I$  is determined under the BIPM reference conditions of air temperature, pressure and humidity. The value of  $I$  is given by

$$I = I_{\text{exp}} (TP_0)/(T_0P), \quad (1)$$

where  $I_{\text{exp}}$  is the ionization current measured at temperature  $T$  (expressed in K) and pressure  $P$  (expressed in kPa).

For a transfer chamber or national reference standard, the calibration coefficient  $N_K$  is defined by the relation

$$N_K = \dot{K}_{\text{BIPM}} / I, \quad (2)$$

where  $\dot{K}_{\text{BIPM}}$  is the air-kerma rate at the reference point, measured with the BIPM standard.

When requested, the calibration coefficient for exposure,  $N_X$ , is supplied, evaluated as

$$N_X = N_K (1-g)/(W/e), \quad (3)$$

where  $g$  is the fraction of electron energy lost in radiative processes in air [1],  $W$  is the mean energy expended to produce an ion pair in dry air, and  $e$  is the electron charge [1, 2].

Details of the conditions of measurement at the BIPM and the uncertainties in the determination of  $\dot{K}_{\text{BIPM}}$  are given in Tables 1 to 6 for x-rays, in Tables 7 and 8 for  $^{60}\text{Co}$  and in Tables 11 and 12 for  $^{137}\text{Cs}$ . In these tables, the relative standard uncertainties estimated by statistical methods (Type A) are denoted by  $s_i$  and those estimated by other means (Type B) are designated by  $u_i$ .

#### IV. Comparison and calibration in terms of absorbed dose to water ( $^{60}\text{Co}$ )

When a primary standard is compared directly, the measuring conditions are stated clearly in the comparison report. For indirect comparisons and calibrations, the transfer chamber or national reference standard is placed in its waterproof sleeve and positioned in the BIPM cubic water phantom of side 30 cm. Its axis is placed in the reference plane, at the reference depth of  $5 \text{ g cm}^{-2}$  in water. This depth includes the window of the phantom (PMMA,  $0.476 \text{ g cm}^{-2}$ ) and is corrected for the change in water density with temperature. As well as correctly orienting the chamber, a reference mark on the sleeve is rotated so as to point towards the radiation source, unless a different orientation is indicated.

The calibration coefficient,  $N_{D,w}$ , is determined using the relation

$$N_{D,w} = \dot{D}_w / (I_w k_{pf}), \quad (4)$$

where:

$\dot{D}_w$  is the absorbed dose rate to water at the reference point, measured using the BIPM standard at a depth of  $5 \text{ g cm}^{-2}$  in water;

$I_w$  is the ionization current measured using the chamber under the BIPM reference conditions of air temperature, pressure and humidity;

$k_{pf} = 0.9996$  is a correction factor applied to  $I_w$  for the non-equivalence with water of the PMMA window of the phantom.

The conditions of measurement at the BIPM are given in Table 7. The physical constants and correction factors used in the ionometric determination of the absorbed dose rate to water at  $5 \text{ g cm}^{-2}$  are given in Table 9 along with their estimated relative uncertainties.

#### V. Comparison and calibration in terms of ambient dose equivalent ( $^{60}\text{Co}$ , $^{137}\text{Cs}$ )

The primary standard, transfer chamber or national reference standard is positioned in air, with its axis in the reference plane.

For a transfer chamber or national reference standard, the calibration coefficient,  $N_H$ , is determined using the relation

$$N_H = \dot{H}^*(10) / I_H, \quad (5)$$

where:

$\dot{H}^*(10)$  is the ambient dose equivalent rate, which for  $^{60}\text{Co}$  radiation is measured using the BIPM standard and for  $^{137}\text{Cs}$  radiation is deduced by calculation from the measured air-kerma rate;

$I_H$  is the ionization current measured by the chamber under the BIPM reference conditions of air temperature, pressure and humidity.

The conditions of measurement at the BIPM are given in Tables 7 and 11 for  $^{60}\text{Co}$  and  $^{137}\text{Cs}$ , respectively. The physical constants and correction factors used in the ionometric determination of the ambient dose equivalent are given in [3] and in Table 10 for  $^{60}\text{Co}$  and in Tables 12 and 13 for  $^{137}\text{Cs}$ .

## VI. Use of calibration coefficients

A transfer chamber or national reference standard calibrated in the BIPM beam can be used in another beam, taking the calibration coefficients  $N_K$ ,  $N_{D,w}$  or  $N_H$ , obtained from (2), (4) and (5), respectively, to determine  $K$ ,  $D_w$  or  $H^*$  (10) in that beam, subject to certain provisions as listed below:

(a) The humidity conditions must not differ significantly from those of the calibration at the BIPM. If the relative humidity is outside the range 30 % to 70 %, the data given in [4] should be used.

(b) The conditions of measurement must not differ significantly from those of the calibration at the BIPM. Otherwise, additional corrections may be necessary (see for example [5] and [6]). Particular attention should be paid to:

- the radiation quality, particularly in the x-ray range;
- the distance from the source;
- the dimensions of the radiation field, in particular with regard to the radiation scattered by the stem and the support for calibration in terms of air kerma;
- the intensity of the ionization current, which can produce a change in the ion recombination;
- the radial non-uniformity of the beam over the cross-section of the chamber [7, 8].

## VII. Comparison and calibration uncertainties

The uncertainties associated with dosimetry measurements made at the BIPM are analysed in accordance with the *Guide to the Expression of Uncertainty in Measurement* [9]. The uncertainty budgets for the dosimetry standards are given in Tables 3, 6, 8, 9, 10, 12 and 13. For comparisons, the BIPM standard uncertainties are combined with those associated with the primary or transfer chamber, taking correlation into account, to give the combined standard uncertainty of the comparison results. The detailed uncertainty budgets are given in the comparison report. For the calibration of national reference standards, the BIPM standard uncertainties are combined with the uncertainties associated with the chamber under calibration to give the combined standard uncertainty of the calibration coefficient. This value is given in the calibration certificate.

It is emphasized that the uncertainty associated with BIPM calibrations is a combined *standard* uncertainty without the application of a coverage factor  $k$ . This long-standing practice of not applying a coverage factor is considered to facilitate the combination of the BIPM and NMI uncertainties and thus simplify the subsequent dissemination of the standard to the customers of the NMI.

The BIPM dosimetry measurements fulfil the criteria of section G.6.6 of [9]. In particular, for the purpose of calculating the expanded uncertainty for their end result at a specified level of confidence, an NMI can assume that the effective number of degrees of freedom for a BIPM calibration is sufficient to be able to use a coverage factor  $k = 2$  for a level of confidence of approximately 95 %. Any exceptions are noted in the calibration certificate.

**Table 1. X-rays (10 kV to 50 kV)**  
**Conditions of measurement at the BIPM**

X-ray tube	W-anode	Mo-anode
Distance between beryllium window of x-ray tube and reference plane of standard	50 cm	60 cm
Beam diameter in reference plane	8.4 cm	10 cm
Beryllium filtration	≈ 3.0 mm	0.8 mm

**Reference qualities W-anode x-ray tube** (recommended by Section I of CCEMRI [10, 11])

X-ray tube voltage /kV	10	30	25	50 (b)	50 (a) <sup>(2)</sup>
Al filtration /mm	0	0.208	0.372	1.008	3.989
Al half-value layer /mm	0.037	0.169	0.242	1.017	2.262
$\bar{\mu}/\rho$ <sup>(1)</sup> /(cm <sup>2</sup> g <sup>-1</sup> )	14.84	3.66	2.60	0.75	0.38
air-kerma rate /(mGy s <sup>-1</sup> )	1.00	1.00	1.00	1.00	1.00

**Reference qualities Mo-anode x-ray tube** (endorsed by the CCRI(I) [12])

X-ray tube voltage /kV	25	28	30	35
Mo filtration /μm	30	30	30	30
Al half-value layer /mm	0.277	0.310	0.329	0.365
$\bar{\mu}/\rho$ <sup>(1)</sup> /(cm <sup>2</sup> g <sup>-1</sup> )	2.20	1.99	1.91	1.74
air-kerma rate /(mGy s <sup>-1</sup> )	2.00	2.00	2.00	2.00

<sup>(1)</sup> mass air-attenuation coefficient

<sup>(2)</sup> the more-filtered of the two 50 kV radiation qualities

**Reference qualities W-anode x-ray tube, Mo filter** (endorsed by the CCRI(I) [12])

X-ray tube voltage /kV	23	25	28	30	35	40	50
Mo filtration /μm	60	60	60	60	60	60	60
Al half-value layer /mm	0.332	0.342	0.355	0.364	0.388	0.417	0.489
$\bar{\mu}/\rho$ <sup>(1)</sup> /(cm <sup>2</sup> g <sup>-1</sup> )	1.79	1.75	1.70	1.67	1.60	1.53	1.40
air-kerma rate /(mGy s <sup>-1</sup> )	1.00	1.00	1.00	1.00	1.00	1.00	1.00

<sup>(1)</sup> mass air-attenuation coefficient

Table 2. X-rays (10 kV to 50 kV)

Physical constants and correction factors used in the BIPM determination of the air-kerma rate <sup>(1)</sup>Dry air density (273.15 K, 101.325 kPa) = 1.2930 kg m<sup>-3</sup> $W/e = 33.97 \text{ J C}^{-1}$ :

<b>W-anode x-ray tube</b>						
Measuring volume FAC-L-01: 1.2004 cm <sup>3</sup>						
X-ray tube voltage /kV		10	30	25	50 (b)	50 (a)
<i>Correction factors</i>						
$k_{sc}$	scattered radiation	0.9962	0.9972	0.9973	0.9977	0.9979
$k_{fl}$	fluorescence	0.9952	0.9971	0.9969	0.9980	0.9985
$k_e$	electron loss	1.0000	1.0000	1.0000	1.0000	1.0000
$k_s$	saturation	1.0006	1.0007	1.0007	1.0007	1.0007
$k_{pol}$	polarity	1.0005	1.0005	1.0005	1.0005	1.0005
$k_a$	air attenuation <sup>(2)</sup>	1.1957	1.0451	1.0319	1.0091	1.0046
$k_d$	field distortion	1.0000	1.0000	1.0000	1.0000	1.0000
$k_{dia}$	diaphragm <sup>(3)</sup>	0.9999	0.9995	0.9996	0.9989	0.9984
$k_p$	wall transmission	1.0000	1.0000	1.0000	1.0000	1.0000
$k_h$	humidity	0.998	0.998	0.998	0.998	0.998
1-g	radiative loss	1.0000	1.0000	1.0000	1.0000	1.0000
<b>Mo-anode x-ray tube</b>						
Measuring volume FAC-L-02: 1.2197 cm <sup>3</sup>						
X-ray tube voltage /kV		25	28	30	35	
<i>Correction factors</i>						
$k_{sc}$	scattered radiation	0.9977	0.9977	0.9978	0.9978	
$k_{fl}$	fluorescence	0.9975	0.9976	0.9976	0.9977	
$k_e$	electron loss	1.0000	1.0000	1.0000	1.0000	
$k_s$	saturation	1.0015	1.0015	1.0015	1.0015	
$k_{pol}$	polarity	1.0000	1.0000	1.0000	1.0000	
$k_a$	air attenuation <sup>(2)</sup>	1.0269	1.0244	1.0233	1.0212	
$k_d$	field distortion	1.0000	1.0000	1.0000	1.0000	
$k_{dia}$	diaphragm	0.9996	0.9995	0.9995	0.9995	
$k_p$	wall transmission	1.0000	1.0000	1.0000	1.0000	
$k_h$	humidity	0.998	0.998	0.998	0.998	
1-g	radiative loss	1.0000	1.0000	1.0000	1.0000	

<sup>(1)</sup> Details on the determination of the air-kerma rate are given in [13] and on the correction factors in [14] for the W-anode qualities and in [15] for the Mo-anode qualities.<sup>(2)</sup> Values at 273.15 K and 101.325 kPa for an attenuation length of 10.0 cm.<sup>(3)</sup> Values adopted September 2009 [16].

**W-anode x-ray tube, Mo filter**Measuring volume FAC-L-01: 1.2004 cm<sup>3</sup>

X-ray tube voltage /kV		23	25	28	30	35	40	50
<i>Correction factors</i>								
$k_{sc}$	scattered radiation	0.9974	0.9974	0.9974	0.9974	0.9974	0.9974	0.9975
$k_{fl}$	fluorescence	0.9972	0.9972	0.9972	0.9972	0.9973	0.9973	0.9975
$k_e$	electron loss	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
$k_s$	saturation	1.0006	1.0006	1.0006	1.0006	1.0006	1.0006	1.0006
$k_{pol}$	polarity	1.0005	1.0005	1.0005	1.0005	1.0005	1.0005	1.0005
$k_a$	air attenuation <sup>(2)</sup>	1.0218	1.0213	1.0208	1.0203	1.0195	1.0187	1.0170
$k_d$	field distortion	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
$k_{dia}$	diaphragm <sup>(3)</sup>	0.9995	0.9995	0.9995	0.9995	0.9995	0.9995	0.9994
$k_p$	wall transmission	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
$k_h$	humidity	0.998	0.998	0.998	0.998	0.998	0.998	0.998
1-g	radiative loss	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000

<sup>(1)</sup> Details on the determination of the air-kerma rate are given in [13] and on the correction factors in [14] for the W-anode qualities and in [15] for the Mo-anode qualities.

<sup>(2)</sup> Values at 293.15 K and 101.325 kPa for an attenuation length of 10.0 cm.

<sup>(3)</sup> Values adopted September 2009 [16].

Table 3. X-rays (10 kV to 50 kV)

## Estimated relative standard uncertainties in the BIPM determination of the air-kerma rate

Symbol	Parameter / unit	$10^2 \times$ Relative standard uncertainty <sup>(1)</sup>	
		$s_i$	$u_i$
<i>Physical constants</i>			
$\rho_a$	dry air density (0°C, 101.325 kPa) / (kg m <sup>-3</sup> )	–	0.01
$W/e$	mean energy per charge / (J C <sup>-1</sup> )	–	0.15
$g$	fraction of energy lost in radiative processes	–	0.01
<i>Correction factors</i>			
$k_{sc}$	scattered radiation	–	0.03
$k_{fl}$	fluorescence	–	0.05
$k_e$	electron loss	–	0.01
$k_s$	saturation	0.01	0.01
$k_{pol}$	polarity	0.01	–
$k_a$	air attenuation	0.02	0.01
$k_d$	field distortion	–	0.07
$k_{dia}$	diaphragm	–	0.03
$k_p$	wall transmission	0.01	–
$k_h$	humidity	–	0.03
<i>Measurement of <math>I/\nu</math></i>			
$I$	ionization current ( $T, P$ , air compressibility)	0.02	0.02
$\nu$	volume	0.03	0.05
	positioning of standard	0.01	0.01
<i>Combined uncertainty of the BIPM determination of air-kerma rate</i>			
	quadratic summation	0.05	0.19
	combined relative standard uncertainty		0.20

<sup>(1)</sup>  $s_i$  represents the relative uncertainty estimated by statistical methods (Type A);  
 $u_i$  represents the relative uncertainty estimated by other methods (Type B).

**Table 4. X-rays (100 kV to 250 kV)****Conditions of measurement at the BIPM**

Distance between focal spot and reference plane of standard: 120 cm

Beam diameter in the reference plane: 9.8 cm

Inherent filtration:  $\approx 3$  mm Be**Reference qualities** (recommended by Section I of the CCEMRI [10])

X-ray tube voltage /kV	100	135	180	250
Al filtration /mm	3.431	2.228	2.228	2.228
Cu filtration /mm	–	0.232	0.485	1.570
Al half-value layer /mm	4.030	–	–	–
Cu half-value layer /mm	0.149	0.489	0.977	2.484
$\bar{\mu}/\rho$ <sup>(1)</sup> /(cm <sup>2</sup> g <sup>-1</sup> )	0.290	0.190	0.162	0.137
air-kerma rate /(mGy s <sup>-1</sup> )	0.50	0.50	0.50	0.50

<sup>(1)</sup> mass air-attenuation coefficient

Table 5. X-rays (100 kV to 250 kV)

Physical constants and correction factors used in the BIPM determination of the air-kerma rate <sup>(1)</sup>

Dry air density (273.15 K, 101.325 kPa) = 1.2930 kg m<sup>-3</sup>

W/e = 33.97 J C<sup>-1</sup>

<b>W-anode x-ray tube</b>				
Measuring volume FAC-M-01: 4.6554 cm <sup>3</sup>				
X-ray tube voltage /kV	100	135	180	250
<i>Correction factors</i>				
$k_{sc}$ scattered radiation	0.9952	0.9959	0.9964	0.9974
$k_{fl}$ fluorescence	0.9985	0.9992	0.9994	0.9999
$k_e$ electron loss <sup>(2)</sup>	1.0000	1.0015	1.0047	1.0085
$k_s$ saturation	1.0010	1.0010	1.0010	1.0010
$k_{pol}$ polarity	1.0002	1.0002	1.0002	1.0002
$k_a$ air attenuation <sup>(3)</sup>	1.0099	1.0065	1.0055	1.0047
$k_d$ field distortion	1.0000	1.0000	1.0000	1.0000
$k_{dia}$ diaphragm <sup>(2)</sup>	0.9995	0.9993	0.9991	0.9980
$k_p$ wall transmission	1.0000	1.0000	0.9999	0.9988
$k_h$ humidity	0.998	0.998	0.998	0.998
1-g radiative loss	0.9999	0.9999	0.9998	0.9997

<sup>(1)</sup> Details on the determination of the air-kerma rate can be found in [17].

<sup>(2)</sup> Values adopted September 2009 [16].

<sup>(3)</sup> Values at 293.15 K and 101.325 kPa for an attenuation length of 28.15 cm.

Table 6. X-rays (100 kV to 250 kV)

## Estimated relative standard uncertainties in the BIPM determination of the air-kerma rate

Symbol	Parameter / unit	$10^2 \times$ Relative standard uncertainty <sup>(1)</sup>	
		$s_i$	$u_i$
<i>Physical constants</i>			
$\rho_a$	dry air density (0°C, 101.325 kPa) / kg m <sup>-3</sup>	–	0.01
$W/e$	mean energy per charge / J C <sup>-1</sup>	–	0.15
$g$	fraction of energy lost in radiative processes	–	0.01
<i>Correction factors</i>			
$k_{sc}$	scattered radiation	–	0.03
$k_{fl}$	fluorescence	–	0.03
$k_e$	electron loss	–	0.05
$k_s$	saturation	0.02	0.01
$k_{pol}$	polarity	0.01	–
$k_a$	air attenuation	0.02	0.01
$k_d$	field distortion	–	0.07
$k_{dia}$	diaphragm	–	0.03
$k_p$	wall transmission	0.01	–
$k_h$	humidity	–	0.03
<i>Measurement of <math>I / v</math></i>			
$I$	ionization current ( $T, P$ , air compressibility)	0.02	0.02
$v$	volume	0.01	0.05
	positioning of standard	0.01	0.01
<i>Combined uncertainty of the BIPM determination of air-kerma rate</i>			
	quadratic summation	0.04	0.19
	combined relative standard uncertainty		0.20

<sup>(1)</sup>  $s_i$  represents the relative uncertainty estimated by statistical methods (Type A);  
 $u_i$  represents the relative uncertainty estimated by other methods (Type B).

Table 7. <sup>60</sup>Co gamma radiation

Conditions of measurement at the BIPM

---

Radiotherapy level

*Measurement of air kerma and absorbed dose*

CISBio source activity (2011-01-01)	≈ 65 TBq
source dimensions	
diameter	20 mm
length	14 mm
contribution of incident scattered radiation (in terms of energy fluence)	21 %
distance from source centre to reference plane	1 m
beam section in the reference plane <sup>(1)</sup>	10 cm × 10 cm
reference depth for absorbed dose measurement	5 g cm <sup>-2</sup>

Radiation-protection level

NBS source activity (2011-01-01)	≈ 0.7 TBq
source dimensions	
diameter	5 mm
length	6 mm
contribution of incident scattered radiation (in terms of energy fluence)	8 %

*Measurement of air kerma*

distance from source centre to reference planes	1.12 m	3.5 m
beam diameter in the reference planes	26 cm	80 cm

*Measurement of ambient dose equivalent*

distance from source centre to reference plane for ambient dose equivalent	3.5 m
beam diameter in the reference plane	80 cm

---

<sup>(1)</sup> The photon fluence rate at the centre of each side of the 10 cm × 10 cm field is 50 % of the photon fluence rate at the centre of the square.

Table 8.  $^{60}\text{Co}$  gamma radiation

Physical constants and correction factors used in the BIPM determination of the air-kerma rate <sup>(1)</sup>, and their estimated relative standard uncertainties

Symbol	Parameter / unit	Value	10 <sup>2</sup> × Relative standard uncertainty <sup>(2)</sup>	
			$s_i$	$u_i$
<i>Physical constants</i>				
$\rho_a$	dry air density (0°C, 101.325 kPa) / (kg m <sup>-3</sup> )	1.2930	–	0.01
$(\bar{\mu}_{\text{en}}/\rho)_{\text{a,c}}$	ratio of mass energy-absorption coefficients	0.9989	0.01	0.04
$s_{\text{c,a}}$	ratio of mass stopping powers	1.0010	}	0.11 <sup>(3)</sup>
$W/e$	mean energy per charge / (J C <sup>-1</sup> )	33.97		
$g$	fraction of energy lost in radiative processes in air	0.0031	–	0.02
<i>Correction factors</i>				
$k_g$	re-absorption of radiative loss	0.9996	–	0.01
$k_h$	humidity	0.9970	–	0.03
$k_s$	saturation	1.0022	0.01	0.02
$k_{\text{st}}$	stem scattering	1.0000	0.01	–
$k_{\text{wall}}$	wall attenuation and scattering	1.0011	}	– <sup>(4)</sup>
$k_{\text{an}}$	axial non-uniformity	1.0020		
$k_{\text{rn}}$	radial non-uniformity	1.0015 <sup>(5)</sup>		
<i>Measurement of <math>I/v</math></i>				
$v$	effective volume / cm <sup>3</sup>	6.8855 <sup>(6)</sup>	–	0.08 <sup>(4)</sup>
$I$	ionization current ( $T$ , $P$ , air compressibility)	–	–	0.02
	short-term reproducibility (including positioning and current measurement) <sup>(7)</sup>	–	0.01	–
<i>Combined uncertainty of the BIPM determination of air-kerma rate at 1 m <sup>(8)</sup></i>				
quadratic summation			0.02	0.15
combined relative standard uncertainty			0.15	

<sup>(1)</sup> Details on the determination of air kerma are given in [18] and [19] with the new correction factors in [20].

<sup>(2)</sup>  $s_i$  represents the relative uncertainty estimated by statistical methods (Type A);

$u_i$  represents the relative uncertainty estimated by other methods (Type B).

<sup>(3)</sup> Uncertainty value for the product  $s_{\text{c,a}} W/e$ , as agreed by the CCRI [21].

<sup>(4)</sup> The uncertainties for  $k_{\text{wall}}$  and  $k_{\text{an}}$  are included in the determination of the effective volume [20].

<sup>(5)</sup> For the radiotherapy-level beam; 1.0003 for the radiation-protection beam

<sup>(6)</sup> For standard CH6-1 used in the radiotherapy-level beam; the volume of the standard CH2 used in the radiation-protection beam is 6.8570 cm<sup>3</sup>, representing the original measured volume 6.8116 cm<sup>3</sup> increased by the factor 1.0076 determined ionometrically following a chamber repair and reduced by the factor 1.0009 described in [20].

<sup>(7)</sup> Over a period of 3 months. The long-term reproducibility over a period of 15 years,  $u_{\text{rep}}$ , is 0.0004.

<sup>(8)</sup> For the radiotherapy-level beam; 1.12 m for the radiation-protection beam.

Table 9.  $^{60}\text{Co}$  gamma radiation

Physical constants and correction factors used in the BIPM ionometric determination of the absorbed-dose rate to water <sup>(1)</sup> at  $5 \text{ g cm}^{-2}$ , and their estimated relative standard uncertainties

Symbol	Parameter / unit	Value	$10^2 \times$ Relative standard uncertainty <sup>(2)</sup>	
			$s_i$	$u_i$
<i>Physical constants</i>				
$\rho_a$	dry air density ( $0^\circ\text{C}$ , $101.325 \text{ kPa}$ ) / ( $\text{kg m}^{-3}$ )	1.2930	–	0.01
$(\bar{\mu}_{\text{en}}/\rho)_{\text{w,c}}$	ratio of mass energy-absorption coefficients	1.1125 <sup>(3)</sup>	0.01 <sup>(3)</sup>	0.14 <sup>(3)</sup>
$s_{\text{c,a}}$	ratio of mass stopping powers	1.0030	}	0.11 <sup>(4)</sup>
$W/e$	mean energy per charge / ( $\text{J C}^{-1}$ )	33.97		
<i>Correction factors</i> <sup>(5)</sup>				
$k_p$	fluence perturbation	1.1107	0.05	0.17
$k_{\text{ps}}$	polythene envelope of the chamber	0.9994	0.01	0.01
$k_{\text{pf}}$	front face of the phantom	0.9996	–	0.01
$k_{\text{rn}}$	radial non-uniformity	1.0056	0.01	0.03
$k_s$	saturation	1.0017	0.01	0.01
$k_h$	humidity	0.9970	–	0.03
<i>Measurement of <math>I/\nu</math></i>				
$\nu$	volume / $\text{cm}^3$	6.8810 <sup>(6)</sup>	0.19	0.03
$I$	ionization current ( $T$ , $P$ , air compressibility)	–	–	0.02
	short-term reproducibility (including positioning and current measurement) <sup>(7)</sup>		0.02	–
<i>Combined uncertainty of the BIPM determination of absorbed-dose rate to water</i>				
quadratic summation			0.20	0.21
combined relative standard uncertainty			0.29	

<sup>(1)</sup> Details on the determination of absorbed dose to water are given in [22].

<sup>(2)</sup>  $s_i$  represents the relative uncertainty estimated by statistical methods (Type A);  
 $u_i$  represents the relative uncertainty estimated by other methods (Type B).

<sup>(3)</sup> Included in the uncertainties for  $k_p$ .

<sup>(4)</sup> Uncertainty value for the product  $s_{\text{c,a}} W/e$ , as agreed by the CCRI [21].

<sup>(5)</sup> Values for the radiotherapy-level beam.

<sup>(6)</sup> Standard CH4-1.

<sup>(7)</sup> Over a period of 3 months. The long-term reproducibility over a period of 15 years,  $u_{\text{rep}}$ , is 0.0006.

Table 10.  $^{60}\text{Co}$  gamma radiation for radiation-protection level at 3.5 mPhysical constants and correction factors used in the BIPM determination of the air-kerma rate<sup>(1)</sup> and ambient dose equivalent rate<sup>(2)</sup> and their estimated relative standard uncertainties

Symbol	Parameter / unit	Value	$10^2 \times$ Relative standard uncertainty <sup>(3)</sup>	
			$s_i$	$u_i$
<i>Physical constants</i>				
$\rho_a$	dry air density (0°C, 101.325 kPa) / (kg m <sup>-3</sup> )	1.2930	–	0.01
$(\bar{\mu}_{\text{en}}/\rho)_{\text{a,c}}$	ratio of mass energy-absorption coefficients	0.9989	0.01	0.04
$s_{\text{c,a}}$	ratio of mass stopping powers	1.0003	}	0.11 <sup>(4)</sup>
$W/e$	mean energy per charge / (J C <sup>-1</sup> )	33.97		
$g$	fraction of energy lost in radiative processes in air	0.0031	–	0.02
<i>Correction factors</i>				
$k_g$	re-absorption of radiative loss	0.9996	–	0.01
$k_h$	humidity	0.9970	–	0.03
$k_s$	saturation	1.0018	0.01	0.02
$k_{\text{st}}$	stem scattering	1.0000	0.01	–
$k_{\text{wall}}$	wall attenuation and scattering	1.0016	}	– <sup>(5)</sup>
$k_{\text{an}}$	axial non-uniformity	1.0004		
$k_{\text{rn}}$	radial non-uniformity	1.0002	–	0.02
<i>Measurement of <math>I/\nu</math></i>				
$\nu$	effective volume / cm <sup>3</sup>	6.8283 <sup>(6)</sup>	–	0.08 <sup>(5)</sup>
$I$	ionization current ( $T, P$ , air compressibility)	–	–	0.02
	short-term reproducibility (including positioning and current measurement)	–	0.10	–
<i>Combined uncertainty of the BIPM determination of air-kerma rate at 3.5 m</i>				
	quadratic summation		0.10	0.15
	combined relative standard uncertainty			0.18
<i>Combined uncertainty of the BIPM determination of ambient dose equivalent rate at 3.5 m</i>				
$\dot{K}_{\text{BIPM}}$	air-kerma rate at 3.5 m		0.10	0.15
$\dot{H}^*(10)/\dot{K}$	ratio of the ambient dose equivalent to air kerma / (Sv Gy <sup>-1</sup> )	1.143	–	0.22
	quadratic summation		0.10	0.27
	combined relative standard uncertainty			0.29

<sup>(1)</sup> Details on the determination of air kerma are given in [18] and [19] with the new correction factors in [20].<sup>(2)</sup> Details on the determination of the ambient dose equivalent rate  $\dot{H}^*(10)$  are given in [3].<sup>(3)</sup>  $s_i$  represents the relative uncertainty estimated by statistical methods (Type A); $u_i$  represents the relative uncertainty estimated by other methods (Type B).<sup>(4)</sup> Uncertainty value for the product  $s_{\text{c,a}} W/e$ , as agreed by the CCRI [21].<sup>(5)</sup> The uncertainties for  $k_{\text{wall}}$  and  $k_{\text{an}}$  are included in the determination of the effective volume [20].<sup>(6)</sup> For standard CH5-2, the measured volume 6.8344 cm<sup>3</sup> reduced by the factor 1.0009 [20].

Table 11.  $^{137}\text{Cs}$  gamma radiation

Conditions of measurement at the BIPM

---

<i>Source details</i>		
source activity (2011)		≈ 0.6 TBq
source dimensions		
diameter		12 mm
length		23 mm
contribution of incident scattered radiation (in terms of energy fluence)		30 %
<i>Measurement of air kerma</i>		
distance from source centre to reference plane	1 m	3 m
beam diameter in the reference plane	11 cm or 20 cm	60 cm
<i>Measurement of ambient dose equivalent</i>		
distance from source centre to reference plane		3 m
beam diameter in the reference plane		60 cm

---

Table 12.  $^{137}\text{Cs}$  gamma radiation

Physical constants and correction factors used in the BIPM determination of the air-kerma rate <sup>(1)</sup>, and their estimated relative standard uncertainties

Symbol	Parameter / unit	Value	$10^2 \times$ Relative standard uncertainty <sup>(2)</sup>	
			$s_i$	$u_i$
<i>Physical constants</i>				
$\rho_a$	dry air density (0°C, 101.325 kPa) / (kg m <sup>-3</sup> )	1.2930	–	0.01
$(\bar{\mu}_{\text{en}}/\rho)_{\text{a,c}}$	ratio of mass energy-absorption coefficients	0.9990	–	0.05
$s_{\text{c,a}}$	ratio of mass stopping powers	1.0104	}	0.11 <sup>(3)</sup>
$W/e$	mean energy per charge / (J C <sup>-1</sup> )	33.97		
$g$	fraction of energy lost in radiative processes in air	0.0012	–	0.02
<i>Correction factors</i>				
$k_h$	humidity	0.9970	–	0.03
$k_s$	saturation	1.0018	0.01	0.02
$k_{\text{st}}$	stem scattering	0.9998	0.01	–
$k_{\text{wall}}$	wall attenuation and scattering	1.0002	0.01	–
$k_{\text{an}}$	axial non-uniformity	1.0018	–	0.04
$k_{\text{rn}}$	radial non-uniformity	1.0070	0.01	0.10
<i>Measurement of <math>I/\nu</math></i>				
$\nu$	volume / cm <sup>3</sup>	6.7967 <sup>(4)</sup>	–	0.08
$I$	ionization current ( $T, P$ , air compressibility)	–	–	0.02
	short-term reproducibility (including positioning and current measurement) <sup>(5)</sup>	–	0.02	–
<i>Combined uncertainty of the BIPM determination of air-kerma rate at 1 m</i>				
quadratic summation			0.03	0.19
combined relative standard uncertainty			0.19	

<sup>(1)</sup> Details on the determination of air kerma are given in [23] with the new correction factors in [24].

<sup>(2)</sup>  $s_i$  represents the relative uncertainty estimated by statistical methods (Type A);

$u_i$  represents the relative uncertainty estimated by other methods (Type B).

<sup>(3)</sup> Uncertainty value for the product  $s_{\text{c,a}} W/e$ , as agreed by the CCRI [21].

<sup>(4)</sup> For standard CH5-1 the measured volume 6.8028 cm<sup>3</sup> reduced by the factor 1.0009 [22].

<sup>(5)</sup> Over a period of 3 months. The long-term reproducibility over a period of 15 years,  $u_{\text{rep}}$  is 0.0004.

Table 13.  $^{137}\text{Cs}$  gamma radiation

Physical constants and correction factors used in the BIPM determination of the air-kerma rate at 3 m and the ambient dose equivalent rate <sup>(1)</sup>, and their estimated relative standard uncertainties

Symbol	Parameter / unit	Value	$10^2 \times$ Relative standard uncertainty <sup>(2)</sup>	
			$s_i$	$u_i$
<i>Physical constants</i>				
$\rho_a$	dry air density (0°C, 101.325 kPa) / (kg m <sup>-3</sup> )	1.2930	–	0.01
$(\bar{\mu}_{\text{en}}/\rho)_{\text{a,c}}$	ratio of mass energy-absorption coefficients	0.9990	–	0.05
$s_{\text{c,a}}$	ratio of mass stopping powers	1.0104	}	0.11 <sup>(3)</sup>
$W/e$	mean energy per charge / (J C <sup>-1</sup> )	33.97		
$g$	fraction of energy lost in radiative processes in air	0.0012	–	0.02
<i>Correction factors</i>				
$k_h$	humidity	0.9970	–	0.03
$k_s$	saturation	1.0018	0.01	0.02
$k_{\text{st}}$	stem scattering	0.9998	0.01	–
$k_{\text{wall}}$	wall attenuation and scattering	1.0008	0.01	–
$k_{\text{an}}$	axial non-uniformity	1.0004	–	0.04
$k_{\text{rn}}$	radial non-uniformity	1.0004	0.01	0.10
<i>Measurement of <math>I/\nu</math></i>				
$\nu$	volume / cm <sup>3</sup>	6.7967 <sup>(4)</sup>	–	0.08
$I$	ionization current ( $T, P$ , air compressibility)	–	–	0.02
	short-term reproducibility (including positioning and current measurement)	–	0.10	–
<i>Combined uncertainty of the BIPM determination of air-kerma rate at 3 m</i>				
quadratic summation			0.10	0.19
combined relative standard uncertainty			0.21	
<i>Combined uncertainty of the BIPM determination of ambient dose equivalent rate at 3 m</i>				
$\dot{K}_{\text{BIPM}}$	air-kerma rate at 3 m	–	0.10	0.19
$\dot{H}^*(10)/\dot{K}$	ratio of the ambient dose equivalent to air kerma / (Sv Gy <sup>-1</sup> )	1.216	–	0.45
quadratic summation			0.10	0.49
combined relative standard uncertainty			0.50	

<sup>(1)</sup> Details on the determination of the ambient dose equivalent rate  $\dot{H}^*(10)$  are given in [23].

<sup>(2)</sup>  $s_i$  represents the relative uncertainty estimated by statistical methods (Type A);  
 $u_i$  represents the relative uncertainty estimated by other methods (Type B).

<sup>(3)</sup> Uncertainty value for the product  $s_{\text{c,a}} W/e$ , as agreed by the CCRI [21].

<sup>(4)</sup> For standard CH5-1 the measured volume 6.8028cm<sup>3</sup> reduced by the factor 1.0009 [24].

## References

- [1] BIPM, Constantes physiques pour les étalons de mesure de rayonnement, in *Com. Cons. Etalons Mes. Ray. Ionisants (Section I)*, 1985, **11**, R45 (Offilib, F-75240 Paris Cedex 05).
- [2] Boutillon M, Perroche-Roux A-M. Re-evaluation of the  $W$  value for electrons in dry air, [1987, \*Phys. Med. Biol.\* \*\*32\*\*, 213-219.](#)
- [3] Kessler C, Roger P, Re-establishment of the air kerma and ambient dose equivalent standards for the BIPM protection-level  $^{60}\text{Co}$  beam, [2005, \*Rapport BIPM-05/08\*, 7 pp](#)
- [4] BIPM, Correction d'humidité, in *Com. Cons. Etalons Mes. Ray. Ionisants (Section I)*, 1977, **4**, R(I)6 (Offilib, F-75240 Paris Cedex 05).
- [5] Boutillon M, Perroche A-M, Determination of calibration factors in terms of air kerma and absorbed dose to water in the  $^{60}\text{Co}$  gamma rays, 1993, *SSDL Newsletter*, **32**.
- [6] Boutillon M, Behaviour of transfer chambers in the low-energy x-ray range, [1996 \*Metrologia\* \*\*33\*\* 479-484.](#)
- [7] Boutillon M, Perroche A-M, Radial non-uniformity of the BIPM  $^{60}\text{Co}$  beam, [1989, \*Rapport BIPM\* 89/2.](#)
- [8] Boutillon M, Perroche A-M, Determination of air kerma for  $^{137}\text{Cs}$  gamma rays, 1993, CCEMRI(I)/93-3.
- [9] *Guide to the Expression of Uncertainty in Measurement*, [JCGM 100:2008](#) (GUM with minor corrections).
- [10] BIPM, Qualités de rayonnement, in *Com. Cons. Etalons Mes. Ray. Ionisants (Section I)*, 1972, **2**, R15 (Offilib, 75240 Paris Cedex 05).
- [11] BIPM, Qualités de rayonnement, in *Com. Cons. Etalons Mes. Ray. Ionisants (Section I)*, 1975, **3**, R(I)6 (Offilib, F-75240 Paris Cedex 05).
- [12] BIPM, Mammography dosimetry radiation qualities, in *Consultative Committee for Ionizing Radiation, 22nd meeting report (2011)*, 2011, p X
- [13] Boutillon M, Henry WH, Lamperti PJ, Comparison of exposure standards in the 10-50 kV x-ray region, [1969, \*Metrologia\*, \*\*5\*\*, 1-11.](#)
- [14] Burns DT, Changes to the BIPM primary air-kerma standards for x-rays, [2004, \*Metrologia\*, \*\*41\*\*, L3.](#)
- [15] Kessler C., Roger P., Burns D.T., Establishment of reference radiation qualities for mammography, 2010, [Rapport BIPM-2010/01](#), 10 pp
- [16] Burns DT, Kessler C, Allisy PJ, Re-evaluation of the BIPM international standards for air kerma in x-rays, 2009, [Metrologia, \*\*46\*\*, L21-L23](#)
- [17] Boutillon M, Mesure de l'exposition au BIPM dans le domaine des rayons X de 100 à 250 kV, [1978, \*Rapport BIPM\*-78/3.](#)
- [18] Boutillon M, Niatel MT, A study of a graphite chamber for absolute exposure measurement of  $^{60}\text{Co}$  Gamma rays, [1973, \*Metrologia\*, \*\*9\*\*, 139-146.](#)
- [19] Burns DT, A new approach to the determination of air kerma using primary-standard cavity ionization chambers, [2006, \*Phys. Med. Biol.\* \*\*51\*\*, 929-942](#)
- [20] Burns DT, Allisy PJ, Kessler C, Re-evaluation of the BIPM international standard for air kerma in  $^{60}\text{Co}$  gamma radiation, [2007, \*Metrologia\*, \*\*44\*\*, L53-L56.](#)
- [21] The value of  $W/e$  and its uncertainty, in [Com. Cons. Ray. Ionisants, 1999, \*\*16\*\*, 145.](#)
- [22] Boutillon M, Perroche A-M, 1993, Ionometric determination of absorbed dose to water for cobalt-60 gamma rays, [1993, \*Phys. Med. Biol.\* \*\*38\*\*, 439-454.](#)
- [23] Boutillon M, Allisy-Roberts PJ, Measurement of air kerma and ambient dose equivalent in a  $^{137}\text{Cs}$  beam, [1996, \*Rapport BIPM\*-96/07, 12 pp.](#)
- [24] Kessler C, Burns DT, Allisy PJ, Re-evaluation of the BIPM standard for air kerma in  $^{137}\text{Cs}$  gamma radiation, 2009, [Metrologia, \*\*46\*\*, L24-L25.](#)