

## Key comparisons CCPR-K3.b, APMP.PR-K3.b, CCPR-K3.b.2, CCPR-K3.b.1, and EUROMET.PR-K3.b.1

**MEASURAND :** Luminous responsivity of photometers

The individual measurements,  $x_i$ , of the participating laboratories correspond to the results of a virtual calibration of the luminous responsivity of the same photometer.

### Key comparison CCPR-K3.b

The key comparison reference value,  $x_R$ , is calculated as the weighted mean of the participant's results, weighted by the inverse square of the individual standard uncertainties,  $u_i$ , with the application of a minimum uncertainty cutoff of 0.2%.

The KRISS is excluded from the calculation of  $x_R$ .

The standard uncertainty of  $x_R$  is  $u_R = 0.06\%$ .

The degree of equivalence of each laboratory with respect to the reference value is given by a pair of terms:

$D_i = (x_i - x_R)$  and  $U_i$ , its expanded uncertainty ( $k = 2$ ), both expressed in relative units.

$U_i = 2(u_i^2 + u_R^2 - u_{corr}^2 + u_{transfer}^2)^{1/2}$ , where  $u_{corr}$  is the correlation between  $u_i$  and  $u_R$ .  $u_{transfer} = 0.09\%$ .

The degree of equivalence between two laboratories is given by a pair of terms:

$D_{ij} = D_i - D_j = (x_i - x_j)$  and  $U_{ij}$ , its expanded uncertainty ( $k = 2$ ), both expressed in relative units.

$U_{ij} = 2(u_i^2 + u_j^2 + 2u_{transfer}^2)^{1/2}$ .

### MSL primary reference

Subsequent to the key comparison CCPR-K3.b and prior to the key comparison APMP.PR-K3.b, MSL re-established their primary reference, finding a relative change in value of  $+0.96\%$  with a standard uncertainty of  $0.04\%$ .

## Key comparisons CCPR-K3.b, APMP.PR-K3.b, CCPR-K3.b.2, CCPR-K3.b.1, and EUROMET.PR-K3.b.1

### Linking APMP.PR-K3.b results to CCPR-K3.b results

Three laboratories (NMIA, MSL and KRISS) participated in both comparisons. KRISS identified a problem with their reference photometer in the CCPR-K3.b key comparison, and the values obtained were not reliable. The two linking laboratories are thus: NMIA and MSL.

The computation of the linkage is described on pages 6 and 7 of the APMP.PR-K3.b Final Report.

The calculation of the degrees of equivalence relative to the CCPR-K3.b key comparison reference value,  $D_i$ , and  $U_i$ , and between pairs of laboratories,  $D_{ij}$  and  $U_{ij}$ , is available from the Appendix B of the same Final Report.

#### Notes:

- For the two linking laboratories (NMIA and MSL), no new results are generated by the key comparison APMP.PR-K3.b.
- A new result is produced by the key comparison APMP.PR-K3.b for KRISS.
- The degrees of equivalence between two participants in APMP.PR-K3.b only, or between one participant in APMP.PR-K3.b only and one of the linking laboratories (NMIA or MSL) are calculated directly from the results of APMP.PR-K3.b:  
 $D_{ij}$  is calculated as the difference of the deviations of laboratories  $i$  and  $j$  from the pilot laboratory, and  
 $U_{ij}$  is calculated as twice the square root of the quadratic sum of the standard uncertainties of the deviations of laboratories  $i$  and  $j$  from the pilot laboratory.
- The degrees of equivalence between one participant in APMP.PR-K3.b only and one participant in CCPR-K3.b (except NMIA and MSL) are calculated as:  
 $D_{ij} = D_i - D_j$  and  $U_{ij} = (U_i^2 + U_j^2)^{1/2}$ . The correlation brought by the key comparison reference value is negligible.

## **Key comparisons CCPR-K3.b, APMP.PR-K3.b, CCPR-K3.b.2, CCPR-K3.b.1, and EUROMET.PR-K3.b.1**

### **Linking CCPR-K3.b.2 results to CCPR-K3.b results**

The link to the key comparison CCPR-K3.b is given by the pilot laboratory HUT that participated in both comparisons.  
No new results are produced by the key comparison CCPR-K3.b.2 for HUT.

The degree of equivalence of KRISS relative to the CCPR-K3.b key comparison reference value is given by:  
 $D_{\text{KRISS}} = -0.0053$  and  $U_{\text{KRISS}} = 0.0060$ , see Appendix 2 of the Final Report.

The degrees of equivalence between KRISS participant in CCPR-K3.b.2 and one laboratory  $j$  participant in CCPR-K3.b are calculated,  
see Appendix 2 of the Final Report.

The degrees of equivalence between KRISS participant in CCPR-K3.b.2 and one participant in APMP.PR-K3.b are not calculated.

### **Linking CCPR-K3.b.1 results to CCPR-K3.b results**

The link to the key comparison CCPR-K3.b is given by the pilot laboratory NMIA that participated in both comparisons.  
No new results are produced by the key comparison CCPR-K3.b.1 for NMIA.

The degree of equivalence of SPRING Singapore relative to the CCPR-K3.b key comparison reference value is given by:  
 $D_{\text{SPRING Singapore}} = 0.0017$  and  $U_{\text{SPRING Singapore}} = 0.0030$ , see section 9 of the Final Report.

The pair-wise degrees of equivalence involving SPRING Singapore participant in CCPR-K3.b.1 are not calculated.

### **Linking EUROMET.PR-K3.b.1 results to CCPR-K3.b results**

The link to the key comparison CCPR-K3.b is given by the pilot laboratory IFA that participated in both comparisons.  
No new results are produced by the key comparison EUROMET.PR-K3.b.1 for IFA.

The degree of equivalence of UME relative to the CCPR-K3.b key comparison reference value is given by:  
 $D_{\text{UME}} = 0.0041$  and  $U_{\text{UME}} = 0.0063$ , see Appendix 2 of the Final Report.

The degrees of equivalence between UME and the laboratories participant in CCPR-K3.b are given in Appendix 2 of the Final Report,  
and reported in the Matrix of equivalence.

## Matrix of equivalence

Lab <i>i</i>	↓		Lab <i>j</i>		→																
	$D_i$	$U_i$																			
	/ $10^{-2}$	/ $10^{-2}$	$D_{ij}$	$U_{ij}$	/ $10^{-2}$	/ $10^{-2}$	$D_{ij}$	$U_{ij}$	/ $10^{-2}$												
LNE-INM	-0.80	0.57			-1.18	0.86	-0.89	0.71		-0.45	0.86	0.01	0.79	-2.90	0.86	-0.93	0.66				
IFA	0.38	0.61			1.18	0.86	0.29	0.74		0.73	0.89	1.19	0.82	-1.72	0.89	0.25	0.69				
*NMIA	0.09	0.39			0.89	0.71	-0.29	0.74		0.44	0.74	0.90	0.67	-2.01	0.74	-0.04	0.50				
HUT	-0.35	0.61			0.45	0.86	-0.73	0.89	-0.44	0.74				0.46	0.82	-2.45	0.89	-0.48	0.69		
MSL	-0.81	0.51			-0.01	0.79	-1.19	0.82	-0.90	0.67	-0.46	0.82			-2.91	0.82	-0.94	0.61			
(KRISS)	2.10	0.64			2.90	0.86	1.72	0.89	2.01	0.74	2.45	0.89	2.91	0.82			1.97	0.69			
*NIM	0.13	0.30			0.93	0.66	-0.25	0.69	0.04	0.50	0.48	0.69	0.94	0.61	-1.97	0.69					
NIST	-0.15	0.42			0.65	0.73	-0.53	0.76	-0.24	0.60	0.20	0.76	0.66	0.69	-2.25	0.76	-0.28	0.53			
*NPL	-0.03	0.39			0.77	0.71	-0.41	0.74	-0.12	0.57	0.32	0.74	0.78	0.67	-2.13	0.74	-0.16	0.50			
NRC	0.00	1.01			0.80	1.17	-0.38	1.19	-0.09	1.09	0.35	1.19	0.81	1.15	-2.10	1.19	-0.13	1.06			
METAS	1.02	0.51			1.82	0.79	0.64	0.82	0.93	0.67	1.37	0.82	1.83	0.75	-1.08	0.82	0.89	0.61			
OMH	-0.37	0.57			0.43	0.83	-0.75	0.86	-0.46	0.71	-0.02	0.86	0.44	0.79	-2.47	0.86	-0.50	0.66			
*PTB	0.35	0.37			1.15	0.70	-0.03	0.74	0.26	0.56	0.70	0.74	1.16	0.66	-1.75	0.74	0.22	0.49			
SMU	-0.24	1.54			0.56	1.66	-0.62	1.67	-0.33	1.60	0.11	1.67	0.57	1.64	-2.34	1.67	-0.37	1.58			
VNIIOFI	0.30	0.49			1.10	0.78	-0.08	0.81	0.21	0.65	0.65	0.81	1.11	0.74	-1.80	0.81	0.17	0.59			
BIPM	-0.16	0.51			0.64	0.79	-0.54	0.82	-0.25	0.67	0.19	0.82	0.65	0.75	-2.26	0.82	-0.29	0.61			
MSL	0.15	0.52			0.95	0.80	-0.23	0.83	0.06	0.67	0.50	0.83	0.96	0.08	-1.95	0.83	0.02	0.62			
CMS/ITRI	1.3	1.4			2.1	1.6	0.9	1.5	1.2	1.4	1.7	1.5	2.1	1.6			1.2	1.4			
KRISS	-1.3	0.8			-0.5	1.0	-1.7	1.0	-1.3	0.6	-1.0	1.0	-0.5	0.8			-1.4	0.9			
NPLI	1.4	2.6			2.2	2.7	1.0	2.7	1.4	2.5	1.8	2.7	2.2	2.6			1.3	2.6			
SPRING Singapore	-0.3	1.2			0.5	1.3	-0.7	1.3	-0.3	1.1	0.1	1.3	0.6	1.2			-0.4	1.2			
KRISS	-0.53	0.60			0.27	0.84	-0.91	0.87	-0.62	0.72	-0.18	0.87	0.28	0.80			-0.66	0.67			
SPRING Singapore	0.17	0.30			-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-
UME	0.41	0.63			1.21	0.85	0.03	0.87	0.32	0.73	0.76	0.87	1.22	0.81	-	-	0.28	0.68			

- \* Lab (Lab) KRISS result not used in the calculation of the key comparison reference value corresponds to the cutoff uncertainty  
 MSL amended scale of MSL  
 KRISS participant laboratory in CCPR-K3.b.2  
 SPRING Singapore participant laboratory in CCPR-K3.b.1  
 UME participant laboratory in EUROMET.PR-K3.b.1

## Matrix of equivalence (Continued)

Lab <i>i</i>			NIST		*NPL		NRC		METAS		OMH		*PTB		SMU	
	$D_i$ / $10^{-2}$	$U_i$ / $10^{-2}$	$D_{ij}$ / $10^{-2}$	$U_{ij}$ / $10^{-2}$												
LNE-INM	-0.80	0.57	-0.65	0.73	-0.77	0.71	-0.80	1.17	-1.82	0.79	-0.43	0.83	-1.15	0.70	-0.56	1.66
IFA	0.38	0.61	0.53	0.76	0.41	0.74	0.38	1.19	-0.64	0.82	0.75	0.86	0.03	0.74	0.62	1.67
*NMIA	0.09	0.39	0.24	0.60	0.12	0.57	0.09	1.09	-0.93	0.67	0.46	0.71	-0.26	0.56	0.33	1.60
HUT	-0.35	0.61	-0.20	0.76	-0.32	0.74	-0.35	1.19	-1.37	0.82	0.02	0.86	-0.70	0.74	-0.11	1.67
MSL	-0.81	0.51	-0.66	0.69	-0.78	0.67	-0.81	1.15	-1.83	0.75	-0.44	0.79	-1.16	0.66	-0.57	1.64
(KRISS)	2.10	0.64	2.25	0.76	2.13	0.74	2.10	1.19	1.08	0.82	2.47	0.86	1.75	0.74	2.34	1.67
*NIM	0.13	0.30	0.28	0.53	0.16	0.50	0.13	1.06	-0.89	0.61	0.50	0.66	-0.22	0.49	0.37	1.58
NIST	-0.15	0.42			-0.12	0.60	-0.15	1.11	-1.17	0.69	0.22	0.73	-0.50	0.58	0.09	1.61
*NPL	-0.03	0.39	0.12	0.60			-0.03	1.09	-1.05	0.67	0.34	0.71	-0.38	0.56	0.21	1.60
NRC	0.00	1.01	0.15	1.11	0.03	1.09			-1.02	1.15	0.37	1.17	-0.35	1.09	0.24	1.85
METAS	1.02	0.51	1.17	0.69	1.05	0.67	1.02	1.15			1.39	0.79	0.67	0.66	1.26	1.64
OMH	-0.37	0.57	-0.22	0.73	-0.34	0.71	-0.37	1.17	-1.39	0.79			-0.72	0.70	-0.13	1.66
*PTB	0.35	0.37	0.50	0.58	0.38	0.56	0.35	1.09	-0.67	0.66	0.72	0.70		0.59	1.60	
SMU	-0.24	1.54	-0.09	1.61	-0.21	1.60	-0.24	1.85	-1.26	1.64	0.13	1.66	-0.59	1.60		
VNIIOFI	0.30	0.49	0.45	0.67	0.33	0.65	0.30	1.14	-0.72	0.74	0.67	0.78	-0.05	0.64	0.54	1.63
BIPM	-0.16	0.51	-0.01	0.69	-0.13	0.67	-0.16	1.15	-1.18	0.75	0.21	0.79	-0.51	0.66	0.08	1.64
MSL	0.15	0.52	0.30	0.69	0.18	0.67	0.15	1.15	-0.87	0.76	0.52	0.80	-0.20	0.66	0.39	1.64
CMS/ITRI	1.3	1.4	1.5	1.5	1.3	1.4	1.3	1.7	0.3	1.5	1.7	1.5	1.0	1.4	1.5	2.1
KRISS	-1.3	0.8	-1.2	0.9	-1.3	0.9	-1.3	1.3	-2.3	1.0	-0.9	1.0	-1.7	0.9	-1.1	1.7
NPLI	1.4	2.6	1.6	2.6	1.4	2.6	1.4	2.8	0.4	2.7	1.8	2.7	1.1	2.6	1.6	3.0
SPRING Singapore	-0.3	1.2	-0.2	1.3	-0.3	1.3	-0.3	1.6	-1.3	1.3	0.1	1.3	-0.7	1.3	-0.1	2.0
KRISS	-0.53	0.60	-0.38	0.74	-0.50	0.72	-0.53	1.18	-1.55	0.80	-0.16	0.84	-0.88	0.71	-0.29	1.66
SPRING Singapore	0.17	0.30	-	-	-	-	-	-	-	-	-	-	-	-	-	-
UME	0.41	0.63	0.56	0.75	0.44	0.73	0.41	1.18	-0.61	0.81	0.78	0.85	0.06	0.72	0.65	1.67

- \* Lab (Lab) KRISS result not used in the calculation of the key comparison reference value due to a problem with its reference standard  
 MSL amended scale of MSL  
 KRISS participant laboratory in CCPR-K3.b.2  
 SPRING Singapore participant laboratory in CCPR-K3.b.1  
 UME participant laboratory in EUROMET.PR-K3.b.1

## Matrix of equivalence (Continued)

Lab <i>i</i>			VNIIIFI		BIPM		MSL		CMS/ITRI		KRISS		NPLI		SPRING		
	$D_i$	$U_i$	$D_{ij}$	$U_{ij}$													
	/ $10^{-2}$	/ $10^{-2}$	/ $10^{-2}$	/ $10^{-2}$	/ $10^{-2}$	/ $10^{-2}$	/ $10^{-2}$	/ $10^{-2}$	/ $10^{-2}$	/ $10^{-2}$	/ $10^{-2}$	/ $10^{-2}$	/ $10^{-2}$	/ $10^{-2}$	/ $10^{-2}$	/ $10^{-2}$	
LNE-INM	-0.80	0.57	-1.10	0.78	-0.64	0.79	-0.95	0.80	-2.1	1.6	0.5	1.0	-2.2	2.7	-0.5	1.3	
IFA	0.38	0.61	0.08	0.81	0.54	0.82	0.23	0.83	-0.9	1.5	1.7	1.0	-1.0	2.7	0.7	1.3	
*NMIA	0.09	0.39	-0.21	0.65	0.25	0.67	-0.06	0.67	-1.2	1.4	1.3	0.6	-1.4	2.5	0.3	1.1	
HUT	-0.35	0.61	-0.65	0.81	-0.19	0.82	-0.50	0.83	-1.7	1.5	1.0	1.0	-1.8	2.7	-0.1	1.3	
MSL	-0.81	0.51	-1.11	0.74	-0.65	0.75	-0.96	0.08	-2.1	1.6	0.5	0.8	-2.2	2.6	-0.6	1.2	
(KRISS)	2.10	0.64	1.80	0.81	2.26	0.82	1.95	0.83									
*NIM	0.13	0.30	-0.17	0.59	0.29	0.61	-0.02	0.62	-1.2	1.4	1.4	0.9	-1.3	2.6	0.4	1.2	
NIST	-0.15	0.42	-0.45	0.67	0.01	0.69	-0.30	0.69	-1.5	1.5	1.2	0.9	-1.6	2.6	0.2	1.3	
*NPL	-0.03	0.39	-0.33	0.65	0.13	0.67	-0.18	0.67	-1.3	1.4	1.3	0.9	-1.4	2.6	0.3	1.3	
NRC	0.00	1.01	-0.30	1.14	0.16	1.15	-0.15	1.15	-1.3	1.7	1.3	1.3	-1.4	2.8	0.3	1.6	
METAS	1.02	0.51	0.72	0.74	1.18	0.75	0.87	0.76	-0.3	1.5	2.3	1.0	-0.4	2.7	1.3	1.3	
OMH	-0.37	0.57	-0.67	0.78	-0.21	0.79	-0.52	0.80	-1.7	1.5	0.9	1.0	-1.8	2.7	-0.1	1.3	
*PTB	0.35	0.37	0.05	0.64	0.51	0.66	0.20	0.66	-1.0	1.4	1.7	0.9	-1.1	2.6	0.7	1.3	
SMU	-0.24	1.54	-0.54	1.63	-0.08	1.64	-0.39	1.64	-1.5	2.1	1.1	1.7	-1.6	3.0	0.1	2.0	
VNIIIFI	0.30	0.49			0.46	0.74	0.15	0.74	-1.0	1.5	1.6	0.9	-1.1	2.6	0.6	1.3	
BIPM	-0.16	0.51	-0.46	0.74			-0.31	0.76	-1.5	1.5	1.1	1.0	-1.6	2.7	0.1	1.3	
MSL	0.15	0.52	-0.15	0.74	0.31	0.76			-1.1	1.6	1.5	0.8	-1.2	2.6	0.4	1.2	
CMS/ITRI	1.3	1.4	1.0	1.5	1.5	1.5	1.1	1.6			2.6	1.6	-0.1	3.0	1.5	1.8	
KRISS	-1.3	0.8	-1.6	0.9	-1.1	1.0	-1.5	0.8	-2.6	1.6			-2.7	2.6	-1.1	1.3	
NPLI	1.4	2.6	1.1	2.6	1.6	2.7	1.2	2.6	0.1	3.0	2.7	2.6			1.6	2.8	
SPRING Singapore	-0.3	1.2	-0.6	1.3	-0.1	1.3	-0.4	1.2	-1.5	1.8	1.1	1.3	-1.6	2.8			
KRISS	-0.53	0.60	-0.83	0.79	-0.37	0.80	-	-	-	-	-	-	-	-	-	-	
SPRING Singapore	0.17	0.30	-	-	-	-	-	-	-	-	-	-	-	-	-	-	
UME	0.41	0.63	0.11	0.80	0.57	0.81	-	-	-	-	-	-	-	-	-	-	

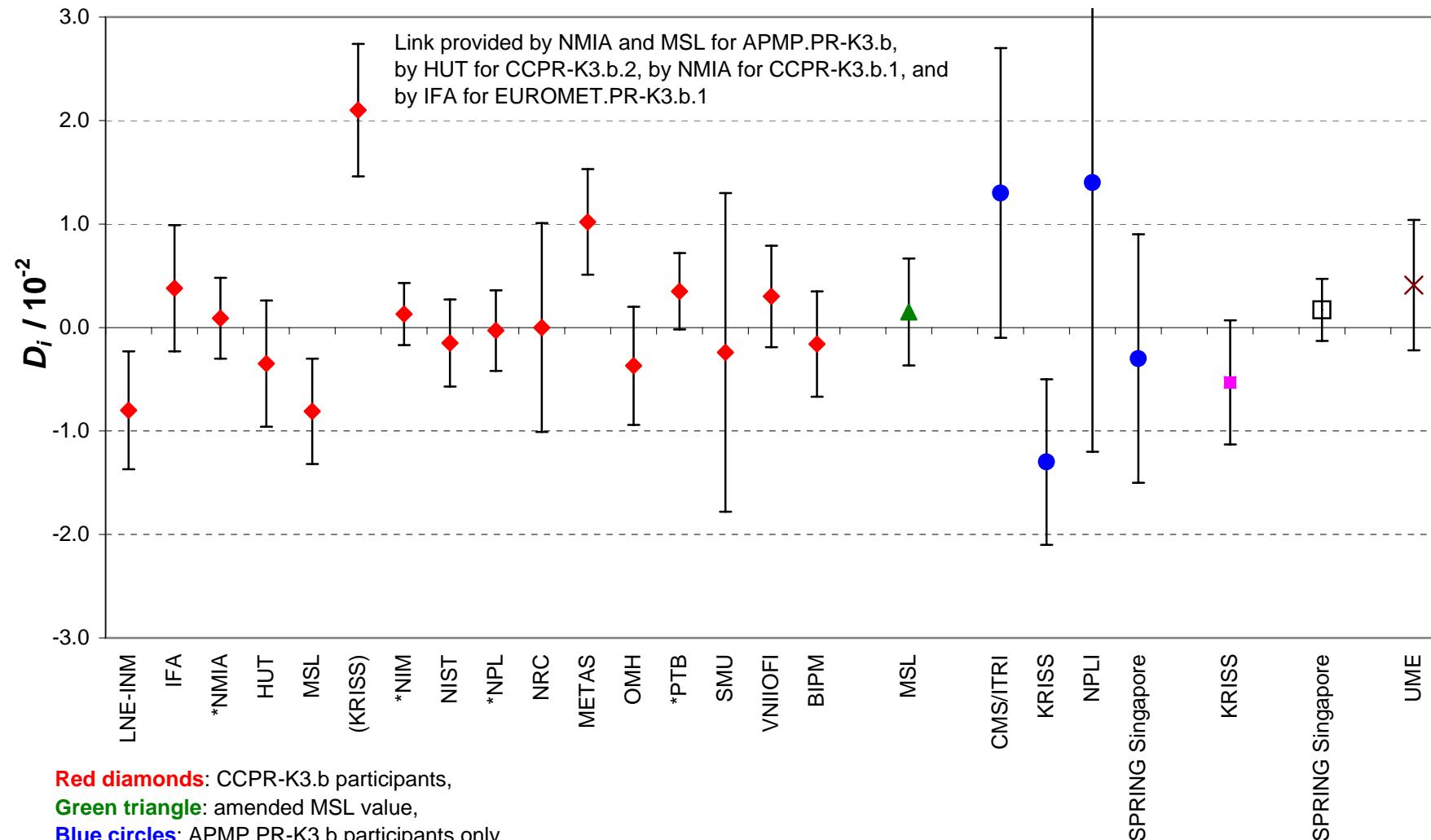
- \* Lab (Lab) KRISS result not used in the calculation of the key comparison reference value corresponds to the cutoff uncertainty  
 MSL amended scale of MSL  
 KRISS participant laboratory in CCPR-K3.b.2  
 SPRING Singapore participant laboratory in CCPR-K3.b.1  
 UME participant laboratory in EUROMET.PR-K3.b.1

## Matrix of equivalence (Continued)

Lab $i$	$\downarrow$	$D_i$ / $10^{-2}$	$U_i$ / $10^{-2}$	KRISS	SPRING	UME
		$D_{ij}$ / $10^{-2}$	$U_{ij}$ / $10^{-2}$	$D_{ij}$ / $10^{-2}$	$U_{ij}$ / $10^{-2}$	$D_{ij}$ / $10^{-2}$
LNE-INM		-0.80	0.57	-0.27	0.84	-1.21
IFA		0.38	0.61	0.91	0.87	-0.03
*NMIA		0.09	0.39	0.62	0.72	-0.32
HUT		-0.35	0.61	0.18	0.87	-0.76
MSL		-0.81	0.51	-0.28	0.80	-1.22
(KRISS)		2.10	0.64			
*NIM		0.13	0.30	0.66	0.67	-0.28
NIST		-0.15	0.42	0.38	0.74	-0.56
*NPL		-0.03	0.39	0.50	0.72	-0.44
NRC		0.00	1.01	0.53	1.18	-0.41
METAS		1.02	0.51	1.55	0.80	0.61
OMH		-0.37	0.57	0.16	0.84	-0.78
*PTB		0.35	0.37	0.88	0.71	-0.06
SMU		-0.24	1.54	0.29	1.66	-0.65
VNIIOFI		0.30	0.49	0.83	0.79	-0.11
BIPM		-0.16	0.51	0.37	0.80	-0.57
MSL		0.15	0.52	-	-	-
CMS/ITRI		1.3	1.4	-	-	-
KRISS		-1.3	0.8	-	-	-
NPLI		1.4	2.6	-	-	-
SPRING Singapore		-0.3	1.2	-	-	-
KRISS		-0.53	0.60		-	-
SPRING Singapore		0.17	0.30	-	-	-
UME		0.41	0.63	-	-	-

- \* Lab (Lab) KRISS result not used in the calculation of the key comparison reference value due to a problem with its reference standard
- MSL amended scale of MSL
- KRISS participant laboratory in CCPR-K3.b.2
- SPRING Singapore participant laboratory in CCPR-K3.b.1
- UME participant laboratory in EUROMET.PR-K3.b.1

**CCPR-K3.b, .1, .2, APMP.PR-K3.b, EUROMET.PR-K3.b.1 Luminous responsivity of photometers**  
**Degrees of equivalence:  $D_i$  and expanded uncertainty  $U_i$  ( $k = 2$ )**



**Red diamonds:** CCPR-K3.b participants,

**Green triangle:** amended MSL value,

**Blue circles:** APMP.PR-K3.b participants only,

**Pink square:** CCPR-K3.b.2

**Empty black square:** CCPR-K3.b.1

**Brown cross:** EUROMET.PR-K3.b.1

\* uncertainty cutoff (0.2%) applied in the calculation of  $x_R$ ,

(KRISS): laboratory excluded from the calculation of  $x_R$ .