

**EURAMET Project 1787**

**Technical Protocol for**

**Bilateral Key Comparison on hydrometers calibration**

**from 1 000 kg/m<sup>3</sup> to 2 000 kg/m<sup>3</sup>**

- Pilot laboratory: Istituto Nazionale di Ricerca Metrologica (INRIM)  
Andrea Malengo

The following document is a similar version of the original technical protocol for the comparison EURAMET MD-K4. 2020, written by Andrea Malengo. The main changes are: the list of the participants (Appendix A), the schedule (Appendix C) and the chapter 4 Test Procedure.

## **1. Outline**

A CIPM key comparison concerning the calibration of hydrometers was proposed during the meeting of the Working Group on Density (WG-Density) of the Consultative Committee for Mass and Related Quantities (CCM) held on April 22<sup>nd</sup>, 2008 at the BIPM with the purpose of linking the regional comparisons previously performed under the auspices of the Regional Metrology Organizations APMP, EURAMET and SIM.

The CIPM key comparison, designated as CCM.D-K4, was coordinated by the Istituto Nazionale di Ricerca Metrologica (INRIM, Italy). January 2011 to April 2012.

Each laboratory, belonging to an individual petal, determined the corrections to be applied to three stated scale readings at 20 °C of different transfer standards in the density range between 600 kg/m<sup>3</sup> to 2 000 kg/m<sup>3</sup>.

The linking laboratories were INRIM, CENAM and PTB, they calibrated all transfer standards involved in the comparison: four hydrometers in the range between 600 kg/m<sup>3</sup> to 2 000 kg/m<sup>3</sup>.

The INRIM carried out the measurement at the beginning and at the end of the comparison.

The measurements were performed from January 2011 to April 2012, the Final Report has been published in 2016 [1].

This comparison is a EURAMET Regional Bilateral Key Comparison between INRIM and IPQ, which will be linked to the CCM.D-K4 comparison. The comparison will be performed in a restricted range compared to the CCM.D-K4, between 1 000 kg/m<sup>3</sup> and 2 000 kg/m<sup>3</sup>. The TC-M agreed that INRIM will organize this bilateral key comparison as pilot laboratory. This comparison will be running in 2026.

## 2. Purpose of this document

The purpose of this document is to provide the participating laboratories with instructions for handling the transfer standards (hydrometers) and to report on the measurement results, the measuring procedure and the apparatus.

It is important that all instructions given in this document are followed. This will ensure that the measurement data are obtained under comparable conditions and presented in the same format. Any deviation from the instructions has to be reported to the pilot laboratory.

## 3. Transfer Standards

For the comparison INRIM and IPQ provide a set composed of three transfer standards, details are shown in the following table:

Table 1. Hydrometers of the comparison

Range	Resolution	Serial Number
0.990 - 1.000 g/cm <sup>3</sup>	0.1 g/cm <sup>3</sup>	19726673
1.480 - 1.500 g/cm <sup>3</sup>	0.2 g/cm <sup>3</sup>	17658983
1.980 - 2.000 g/cm <sup>3</sup>	0.2 g/cm <sup>3</sup>	17674615

## 4. Test Procedure

The measurand is the correction  $C$  to be evaluated at each calibration point

$$C = \rho_x - \rho_r$$

where  $\rho_x$  is the density of the buoyant liquid in which the hydrometer would freely float at the scale mark  $\rho_r$ .

The results have to be given at the reference temperature of 20 °C, the cubic expansion coefficient for all hydrometers was assumed to be  $25 \cdot 10^{-6} \text{ }^{\circ}\text{C}^{-1}$ , with an uncertainty of  $1,2 \cdot 10^{-6} \text{ }^{\circ}\text{C}^{-1}$ .

Participating laboratories should use their routine calibration procedure based on the Cuckow's method.

In Table 2 the calibration points and the reference surface tension of the liquid, in which each hydrometer was intended to be used, are shown.

Table 2. Calibration points and reference surface tensions

Range	Reading scale/ g/cm <sup>3</sup>	Ref. surface tension/ mN/m
0.990 - 1.000 g/cm <sup>3</sup>	0.991 0	35.0
	0.995 0	35.0
	0.999 0	35.0
1.480 - 1500 g/cm <sup>3</sup>	1.481 0	75.0
	1.490 0	75.0
	1.499 0	75.0
1.980 - 2.000 g/cm <sup>3</sup>	1.981 0	75.0
	1.990 0	75.0
	1.999 0	75.0

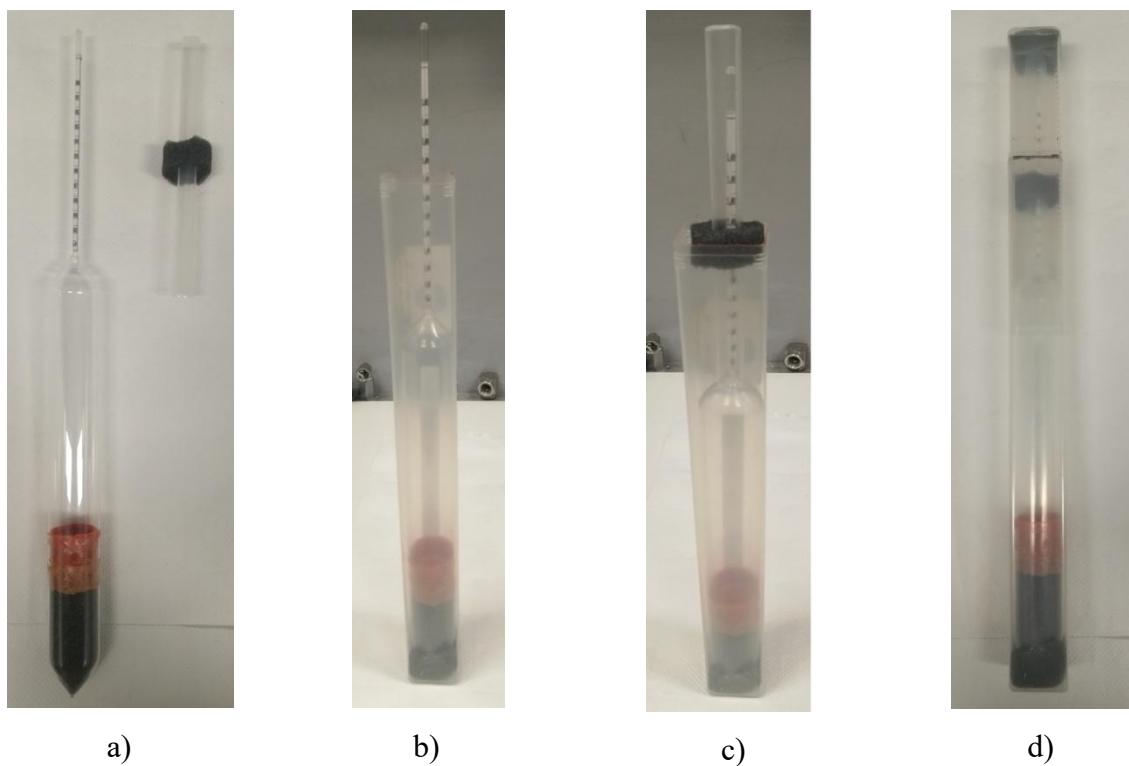


Figure 1. The system of packaging: a) hydrometer with the stem protector, b) hydrometer into the container, c) position the stem protector, d) close the container firmly.

## 5. Cautions

The stem of the hydrometers used in this comparison are very fragile, so care must be taken when handling them.

- When not under calibration, the hydrometers should be stored in their storage container.
- When possible, handle the hydrometer by the bulb.
- Take the hydrometer for the stem only when it is in the vertical position.
- Extract the hydrometer from the container keeping the container in a perfectly vertical position, or extract the hydrometer by placing the container horizontally on a table.
- Insert the hydrometer in the container keeping the container in a perfectly vertical position.
- Take great care in preparing the hooking system for the hydrostatic weighing
- Before calibration, the hydrometers should be cleaned (e.g with ethanol) and then kept in the laboratory for an appropriate time for temperature stabilization.
- After calibration, the hydrometers should be cleaned.
- Before sending the hydrometers, they must be carefully placed in their storage container (see Figure 1), other types of containers are not allowed.

## 6. Circulation of the Artefacts

Each participating laboratory (Appendix A), as soon as calibrated, will send to the next laboratory the set of the four assigned hydrometers, according to the circulation scheme (Appendix C), informing the receiving laboratory and the pilot laboratory (Appendix E).

Each travelling standard is placed in the appropriate container, provided by the pilot laboratory. The packaging system is shown in the Figure 1, other methods are not allowed.

The three hydrometers must be placed in a suitcase with packaging material, provided by the pilot laboratory. The total weight of the transportation case together with the travelling standards is about 4 kg in total, dimension is about 57 cm x 47 cm x 13 cm.

It should be ensured by the sending institute that the travelling standards will be delivered to the next participating institute on time according to the planned schedule given in Appendix C.

The package will be transported by courier or directly by hand by the laboratory staff.

The package will be equipped with a warning: To be opened only by laboratory staff.

After the arrival of the package, the laboratory will inform without delay the pilot laboratory indicating the date of arrival, the status of the package and its contents (Appendix D).

The participating laboratory bears the costs for the transportation of the travelling standards to the next laboratory excluding possible customs charges. The participants are responsible for completing the local customs formalities.

If some hydrometer should break, it can be replaced using a new hydrometer.

## 7. Measurements required

### *Mass measurement*

At least five weighing sequences in air shall be performed to determine the weight of each hydrometer and to evaluate the experimental standard deviation.

The averages of the parameters contributing to the evaluation of air density shall be recorded, the measurements shall be carried out under laboratory ambient conditions at a temperature close to 20 °C. For the calculation of air density, the CIPM 2007 formula [2] shall be used.

### *Hydrostatic weighing*

After the mass measurement, the hydrostatic weighing has to be carried out.

The measurements should be made close to 20 °C.

At least five weighing sequences have to be carried out for the weight determination at each of the three scale readings stated in Table 2, and to evaluate the experimental standard deviation. Adjustment of the scale readings to the liquid level should be made when the middle of the line is aligned with the horizontal plane of liquid (Figure 2).

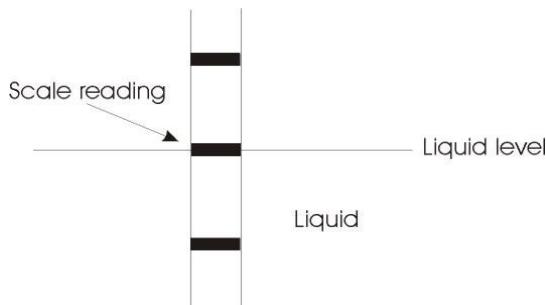


Figure 2. Alignment of the stated scale reading with the horizontal plane of liquid.

## 8. Reports

As soon as the measurements are completed, each laboratory will send the pilot laboratory a summary of the procedure used and a description of the apparatus (Appendix F). In addition, information and results should be compiled using the Excel Report Form, provided by the pilot laboratory.

The Excel Report Form consists of two parts:

### *Report Form I*

It concerns information about the instrumentation used in the project. Please add any additional information to your measurements.

For the balance/s used to determine the weighing value in air/liquid, the following information have to be given:

- a) Manufacturer and type of balance.
- b) Maximum capacity, electronic range, resolution.
- c) Standard deviation, maximum non-linearity, out-of-centre error.
- d) Calibration uncertainty, method and frequency.

If mass standards are used as "substitutional weights" for the comparison of mass of hydrometer to the mass of weights, the following information is to be given:

- a) Manufacturer, type and material of the weights.

b) Identification of weights, their values and standard uncertainties.

c) Date of last calibration and traceability.

For the thermostat system used to stabilize the temperature of the buoyant liquid, the following information have to be given:

a) Manufacturer and type of thermostat.

b) Capacity.

c) Temperature stability and uniformity at 20 °C.

For the alignment system used for alignment the scale readings, the following information is to be given:

a) Type of magnifier.

b) Method of alignment.

c) Uncertainty of alignment.

For the instruments used for the determination of the density of air (air pressure, temperature, humidity and CO<sub>2</sub> content), the following information have to be given:

a) Manufacturer, type.

b) Resolution.

c) Frequency of measurement.

d) Calibration uncertainty, date of last calibration and traceability.

For the instruments used for the measurement of the liquid temperature, the following information is to be given:

a) Manufacturer and type of sensor.

b) Manufacturer and type of resistance bridge and standard resistor (if applicable).

c) Resolution of temperature measurement.

d) Calibration uncertainty, date of last calibration and traceability of thermometer (whole temperature range).

For the apparatus used for determining the surface tension of the buoyant liquid, the following information is to be given:

a) Manufacturer and measuring method,

b) Calibration uncertainty and traceability.

For the reference buoyant liquid the following information is to be given:

a) Manufacturer.

b) product name.

c) molecular formula and assay.

*Report Form 2(ID Hydrometer)*

For each hydrometer, general information and results of measurements have to be given.

General information have to be given in:

***Table 1-1: Movement of the travelling standard***

- a) Date of arrival of the hydrometer at the laboratory.
- b) Condition of package and of the individual hydrometer.
- c) Date of shipment of hydrometers.
- d) Company responsible for transportation.

***Table 1-2: Measurement period***

- a) Date for hydrometer mass measurement.
- b) Date for hydrostatic weighing.

Measurement information have to be given in:

***Table 1-3: Mass determination***

- a) Substitutional weights, if they are used, and mean value of the hydrometer mass for five weights in air and its standard deviation of the mean.
- b) Ambient conditions during mass measurements including data about air density, air temperature, air pressure, humidity and CO<sub>2</sub> content.

***Table 1-4: Hydrostatic weighing***

- a) Value of the additional weight (ballast) if a stainless steel weight is added to the hydrometer to cause it to sink, measurement correction and uncertainty.
- b) Mean values of the hydrometer weighing value at the indicated scale reading. The standard deviation for the mean and the temperature and density of buoyant liquid during the hydrostatic weighing.
- c) Ambient conditions during hydrostatic weighing, including data about air density, air temperature, air pressure, humidity and CO<sub>2</sub> content.

***Table 1-5: Results***

- a) Corrections at each scale reading as determined at 20 °C. In the last column the reference surface tension is given.

***Table 1-6: Uncertainty budget for the hydrometer corrections***

A list of main components of the uncertainty budget is given. Please add any additional component occurring in your measurements.

The uncertainty evaluation should include a list of all influence quantities, values, their degrees of freedom and their combined standard uncertainty. This is obtained by combining the individual standard uncertainties obtained from Type A and Type B evaluations, according to ISO "Guide to the Expression of Uncertainty in Measurement" [3].

A pooled experimental standard deviation characterizing the hydrometer weighing value in buoyant liquid have to be given [3 (H.3.6)].

***Table 1-7: Uncertainty of the hydrometer corrections***

The uncertainty of measurement for the corrections is calculated with the Excel sheet from the above given data, as well as the effective degrees of freedom  $v_{\text{eff}}$  of the combined standard uncertainty  $u_c$ , the t-factor  $t_{95}(v_{\text{eff}})$  taken from the t-distribution for a 95% confidence level and the expanded uncertainty for the corrections as  $U_{95} = t_{95}(v_{\text{eff}}) \cdot u_c$ .

The reports are to be sent to the pilot laboratory as soon as possible but six weeks after the measurements are completed at the latest. A result will not be considered complete unless an associated uncertainty supported by a complete uncertainty budget is given. The results are confidential until all the participants have completed their measurements and all the results have been received (or until the deadline for receipt the results).

## 9. Reference

- [1] S. Lorefice et al "CCM key comparison CCM.D-K4 'Hydrometer'", Metrologia, 2016, 53 07003
- [2] A. Picard, R.S. Davis, M. Glaser, and K. Fujii : "Revised formula for the density of moist air (CIPM 2007)," Metrologia, 2008, 45, pp. 149 - 155.
- [3] "Guide to the Expression of Uncertainty in Measurement," International Organization for Standardization (ISO), 1995.

## Appendices

### A. Participants

List of Participants				
NMI	Country	Contact Person	E-mail	Address
INRIM	Italy	Andrea Malengo	a.malengo@inrim.it	Istituto Nazionale di Ricerca Metrologica (INRIM) Strada delle Cacce, 91 10135 Torino Italy
IPQ	Portugal	Sara Moura	smoura@ipq.pt	Instituto Português da Qualidade (IPQ) Rua António Gião, 2 2829-513 Caparica Portugal

### B. Timetable for the comparison

January 2026	Start of measurements (pilot laboratory)
February 2026	Measurements by all participants and Reports from all participants
March 2026	Draft A of the comparison
March 2026	Draft B of the comparison: end of the comparison

### C. Circulation scheme for the comparison

Circulation scheme		
12th January	23th January	INRIM
2nd February	13th February	IPQ
23th February	27th February	INRIM

### D. Receipt of the standards

To monitor the progress of the comparison, it is required, upon receipt of the package, to kindly send an e-mail to:

- pilot laboratory

Andrea Malengo

e-mail: a.malengo@inrim.it

Object: EURAMET comparison 1787 on hydrometers

This e-mail should contain the information about the status of the hydrometers and their packaging.

## **E. End of measurements and shipping**

To monitor the progress of the comparison, it is required, upon completion of the measures, before shipment, to kindly send an e-mail to:

- pilot laboratory

Andrea Malengo

e-mail: [a.malengo@inrim.it](mailto:a.malengo@inrim.it)

- the contact person of the next laboratory

Object: EURAMET comparison 1787 on hydrometer

This e-mail should contain the following information:

- date of the end of measurements

- shipping date and tracking number (if possible)

## **F. Results**

Calibration results should be sent within three weeks (six weeks at the latest) after the end of the measurements. It is required to kindly send an e-mail to:

- pilot laboratory

Andrea Malengo

e-mail: [a.malengo@inrim.it](mailto:a.malengo@inrim.it)

Object: EURAMET comparison 1787 on hydrometer

This e-mail should contain the following information:

- Calibration results (Excel Report Form)

- A summary of the procedure used and a description of the apparatus