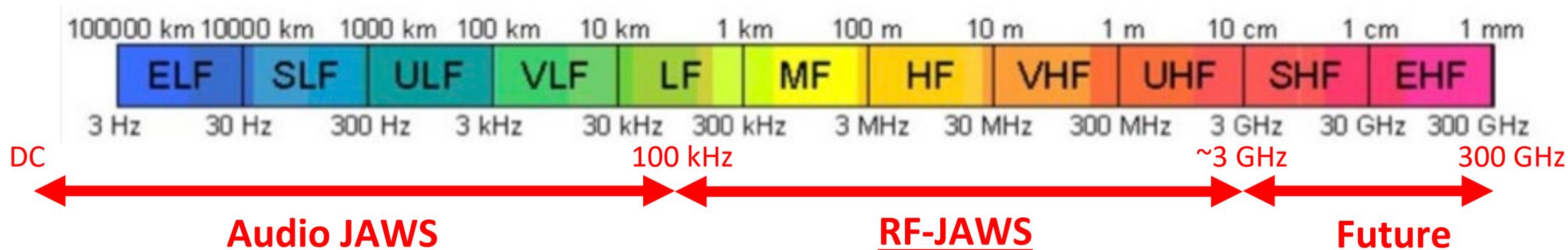


# RF Josephson Arbitrary Waveform Synthesizer: JAWS up to 3 GHz and beyond

**Paul Hale**

RF Technology Division  
Boulder, Colorado, USA

**Nathan Flowers-Jacobs, J.A. Brevik, A.A. Babenko, A.E. Fox, A.S. Boaventura, P.F. Hopkins, P.D. Dresselhaus, D.F. Williams, and S.P. Benz**

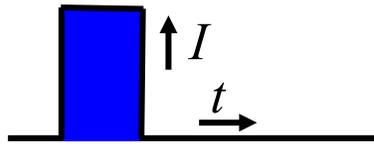


**Goal:** Create a programmable **quantum-based RF source** for signal & power metrology

## Points of emphasis:

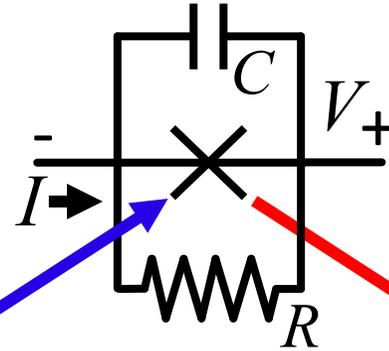
- Calculable, quantum-based SI-traceable signal accuracy
- Quantum Locking Range: stable, reproducible, location-independent
- Arbitrary waveform synthesis using “3-level DAC” → calculable out-of-band signal
- Typical -48 dBm at cryogenic reference plane; demonstrated up to -28 dBm

apply input current bias pulse  
(imprecise & not quantized)



rotates  $\varphi$  (superconducting phase across JJ) by  $2\pi$

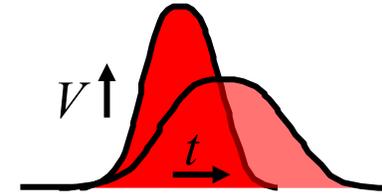
$$I = I_c \sin(\varphi)$$



overdamped JJs

$$V = \frac{\hbar}{2e} \frac{d\varphi}{dt}$$

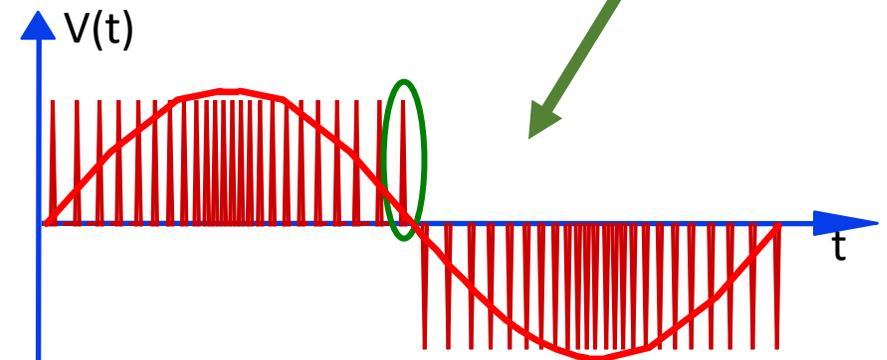
outputs voltage pulse  
(quantized area)



**Basis of JAWS\* Voltage Standard!**

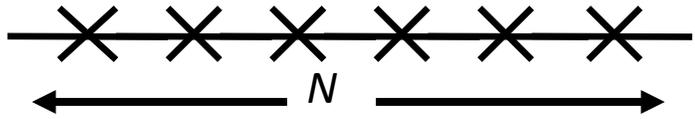
$$\int V(t) dt = \frac{h}{2e}$$

- Only 20  $\mu\text{V}/\text{JJ}$  for 10 Gpulses/sec  
→ need long JJ arrays & fast pulses
- Sequence of pulses generates ac waveform
  - determine sequence using delta-sigma algorithm
  - quantized area → calculable spectrum



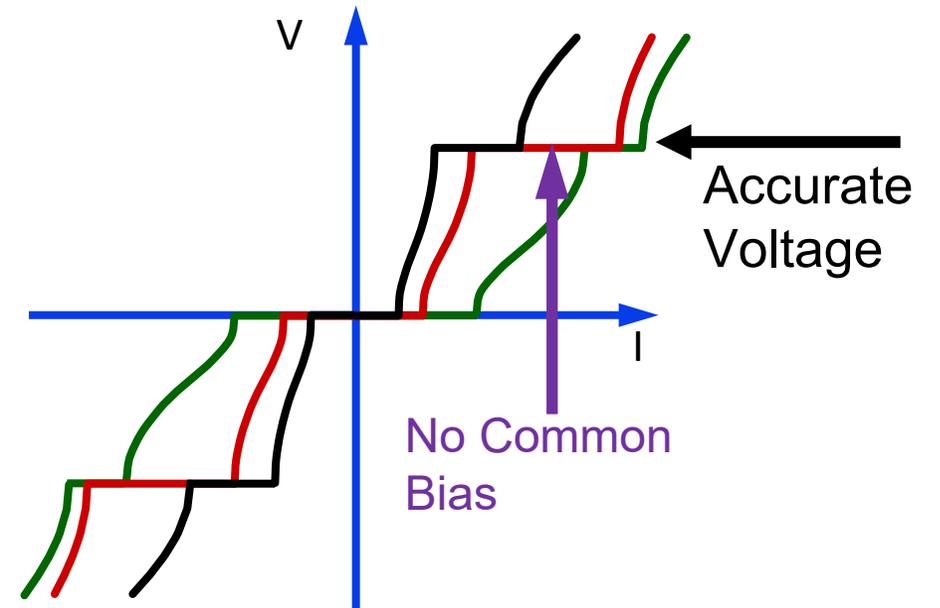
\*Co-invented by Przybysz, Worsham, Hamilton and Benz in 1995

# Practical Voltages Require Series Arrays

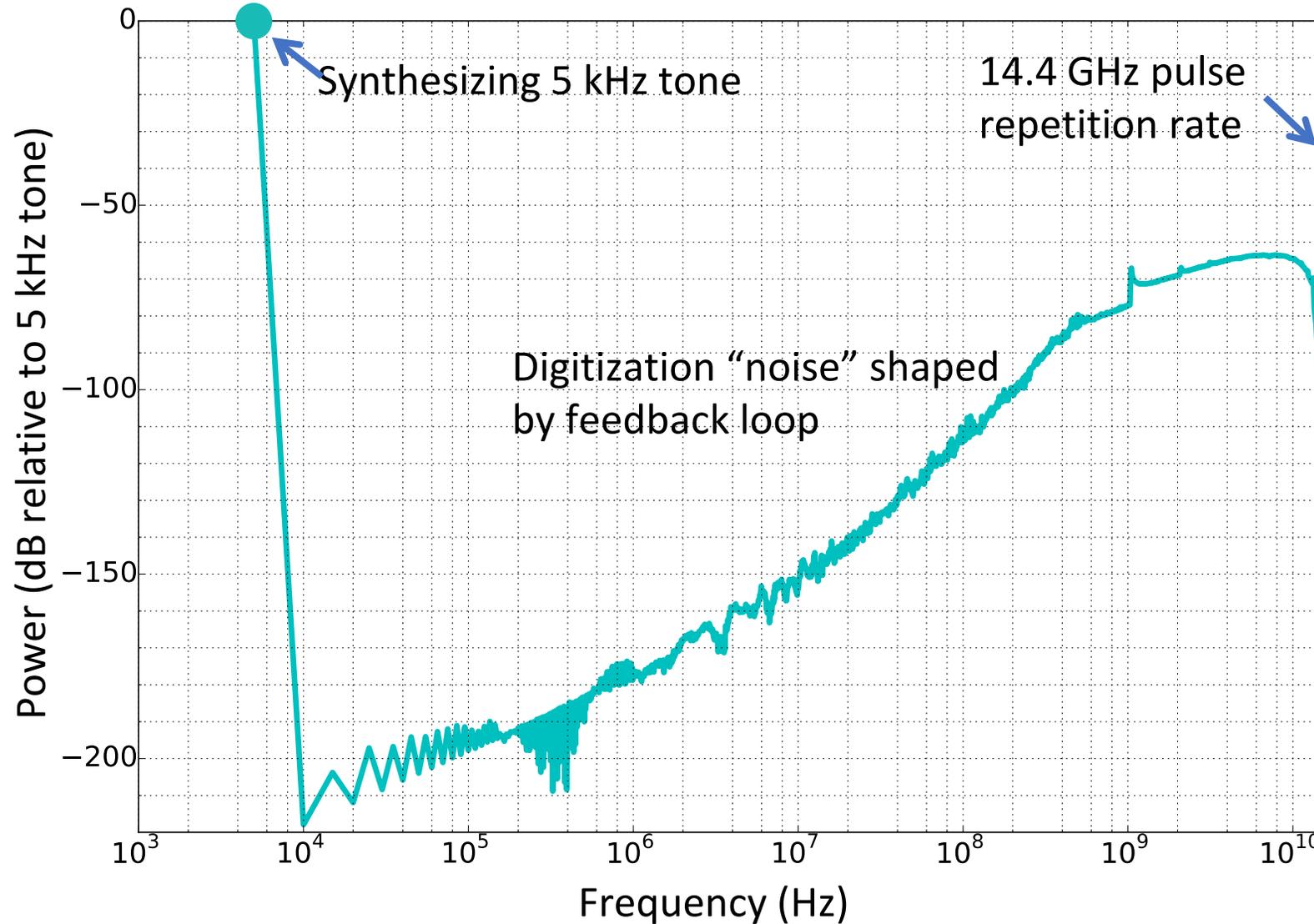


$$V_{n,N} = \frac{h}{2e} nNf$$

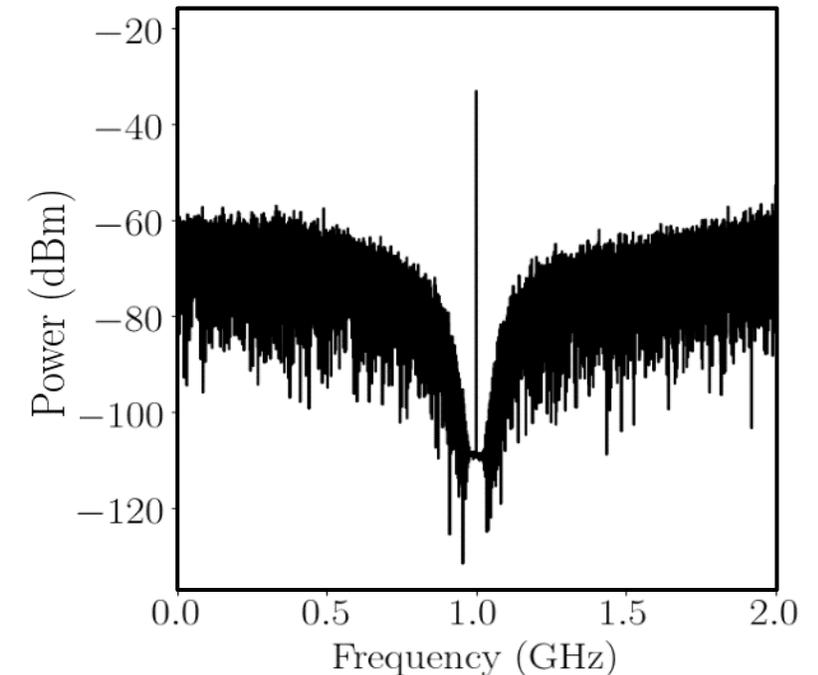
- Common bias requires
  - Uniform junctions
  - Uniform microwave power
  - Excellent microwave designs



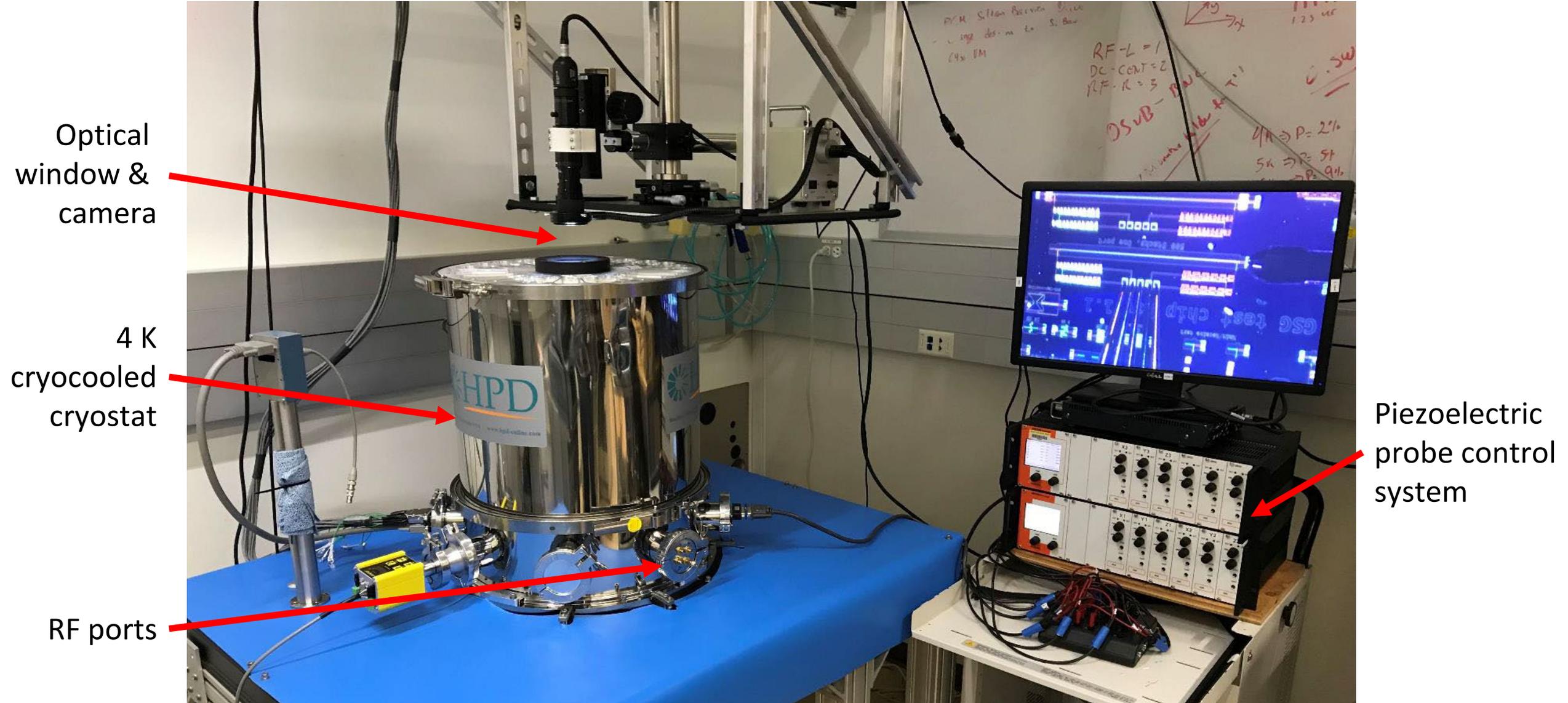
# Example calculated spectrum



- Delta-sigma algorithm
  - feedback with loop filter
  - RF-JAWS uses bandpass loop filter
- Very small background
  - In filter bandwidth
- Calculation assumes:  $\int V(t)dt = \frac{h}{2e}$ 
  - $\delta$ -function JJ pulse shape
  - no feedthrough of bias pulses



# Cryogenic Probe Station



Optical window & camera

4 K cryocooled cryostat

RF ports

Piezoelectric probe control system

# 4 K Stage with JJ Devices & Standards

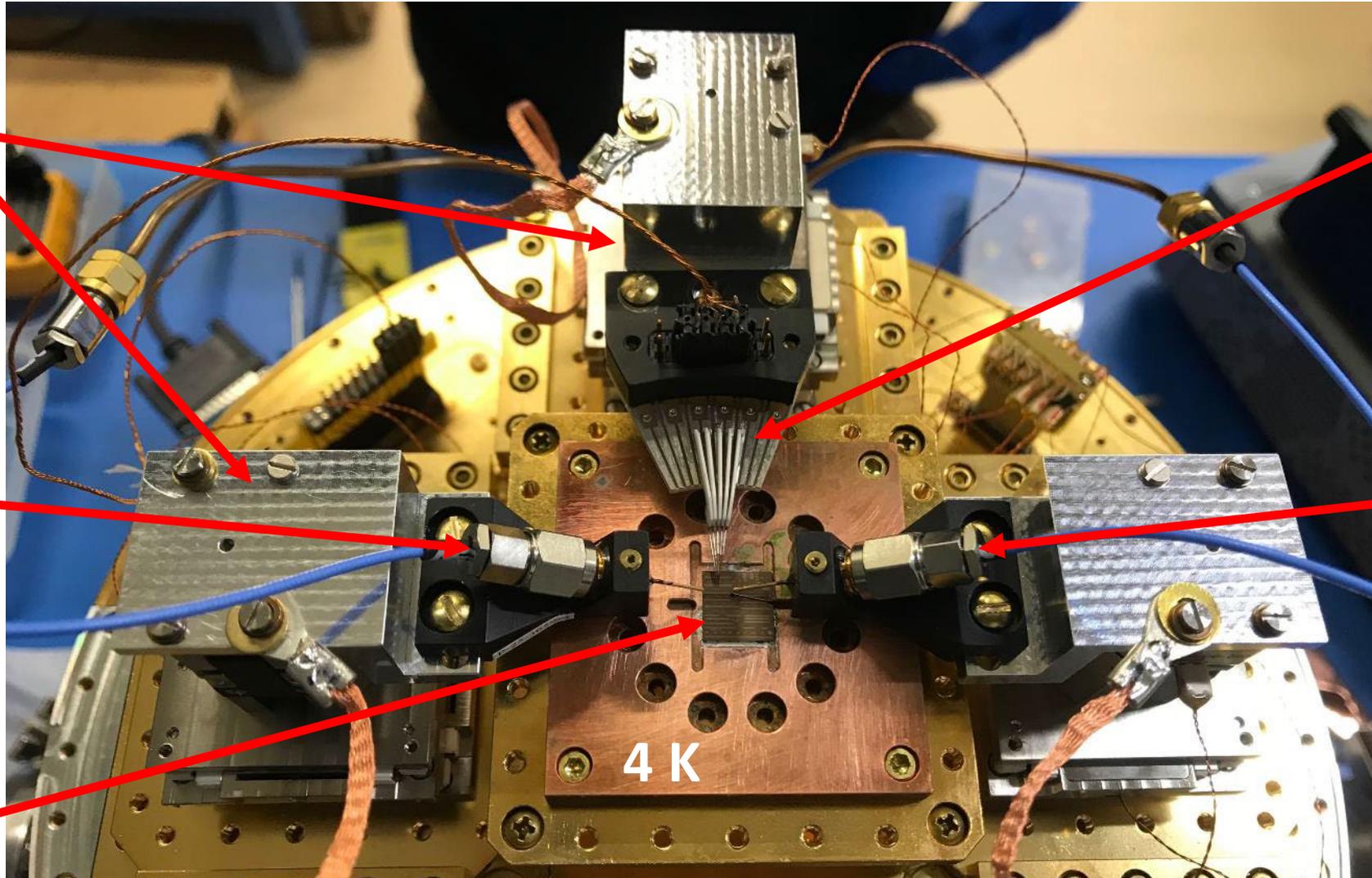
Attocube  
3-axis  
positioners

DC probe

RF probe  
port 1

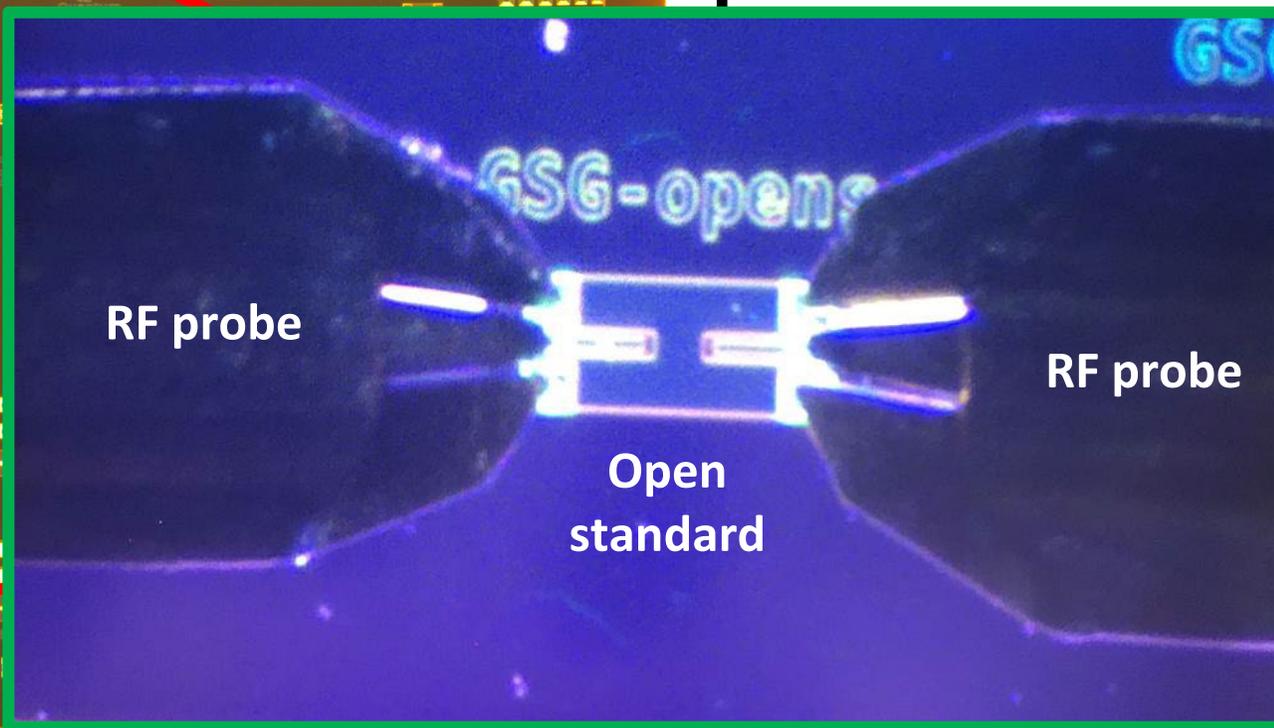
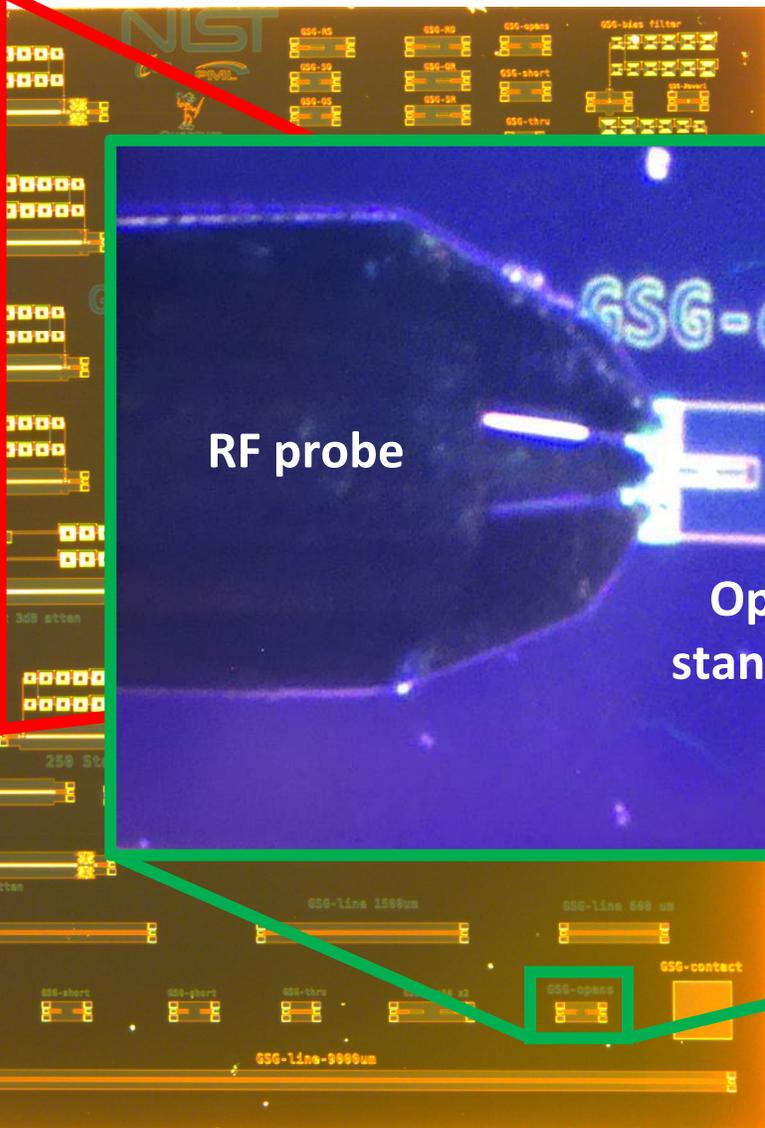
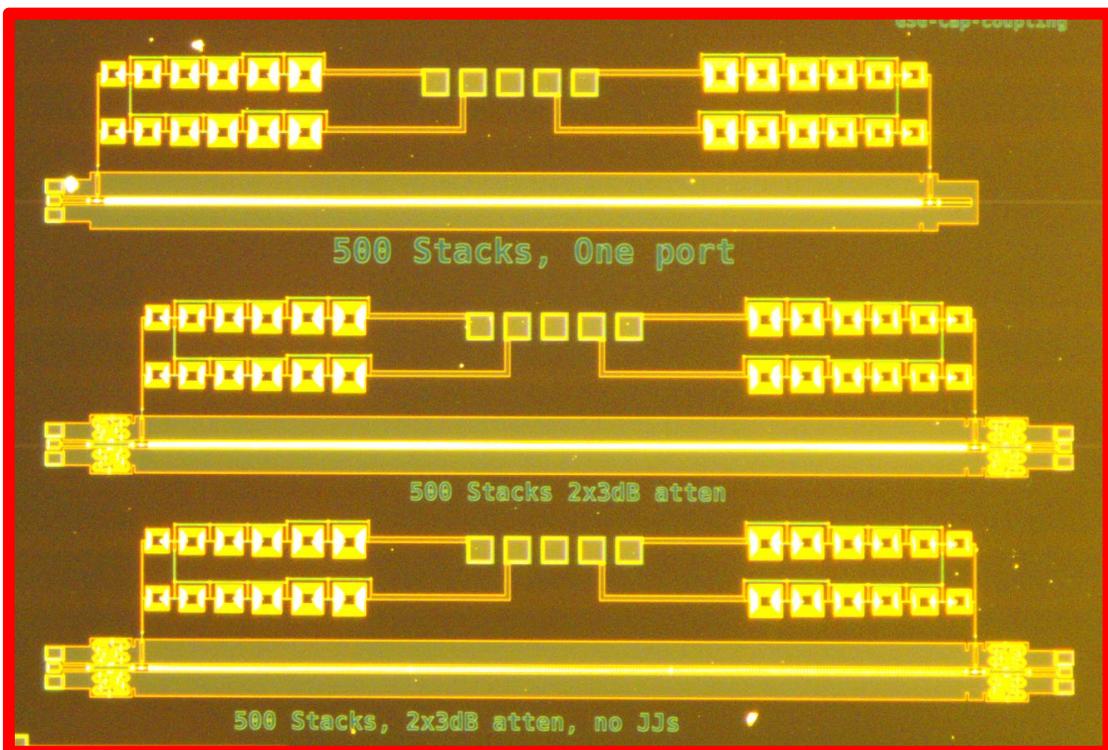
RF probe  
port 2

Device &  
standards  
chip



25 cm dia.

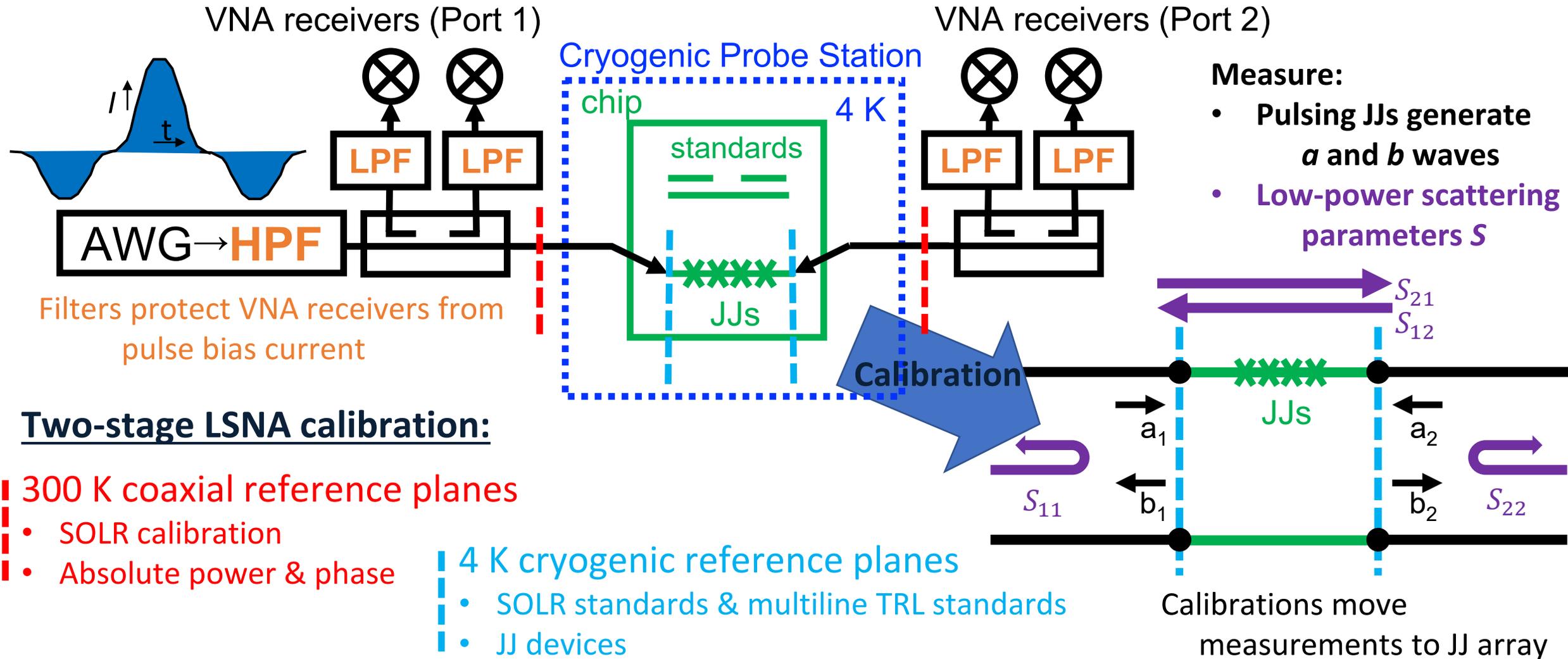
# Single Chip: JAWS and RF Standards

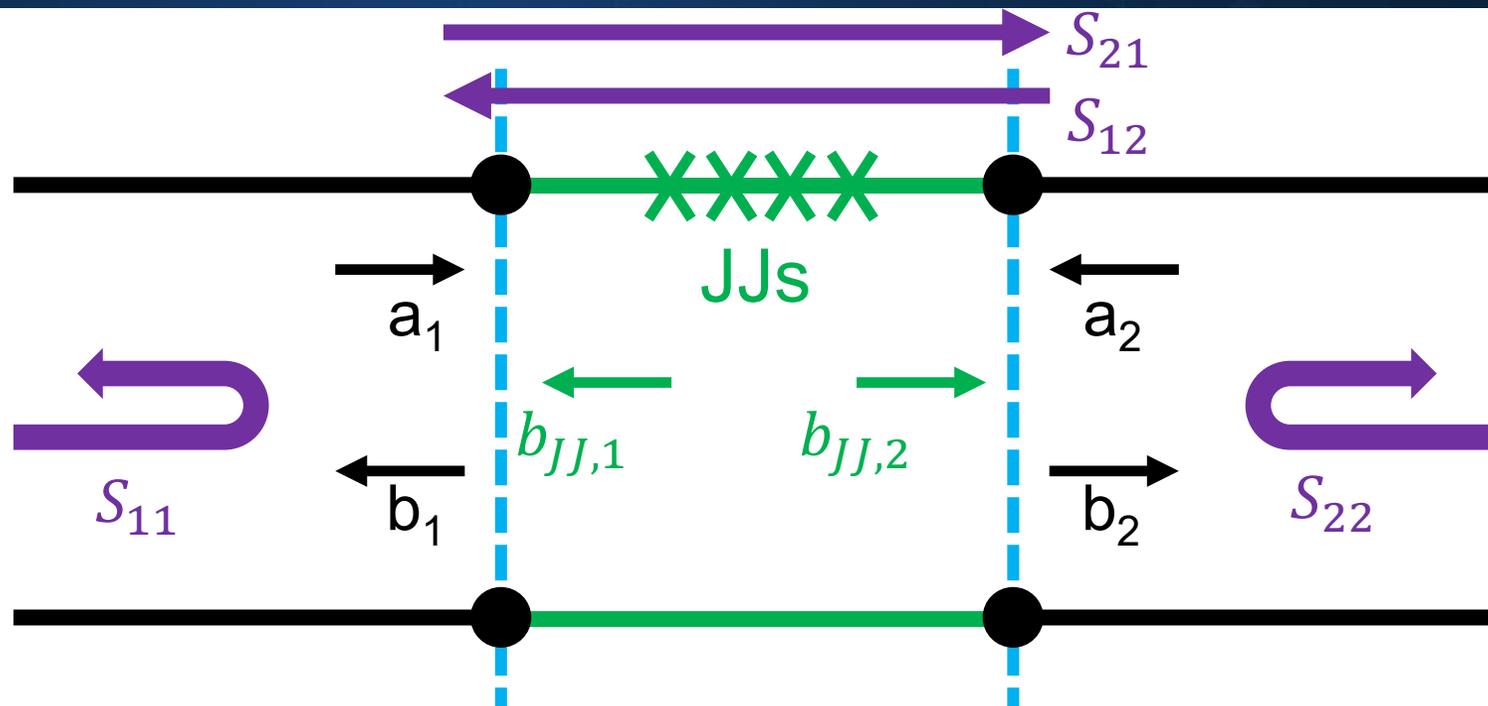


Calibration standards



# Calibrated RF measurement of JJ voltage





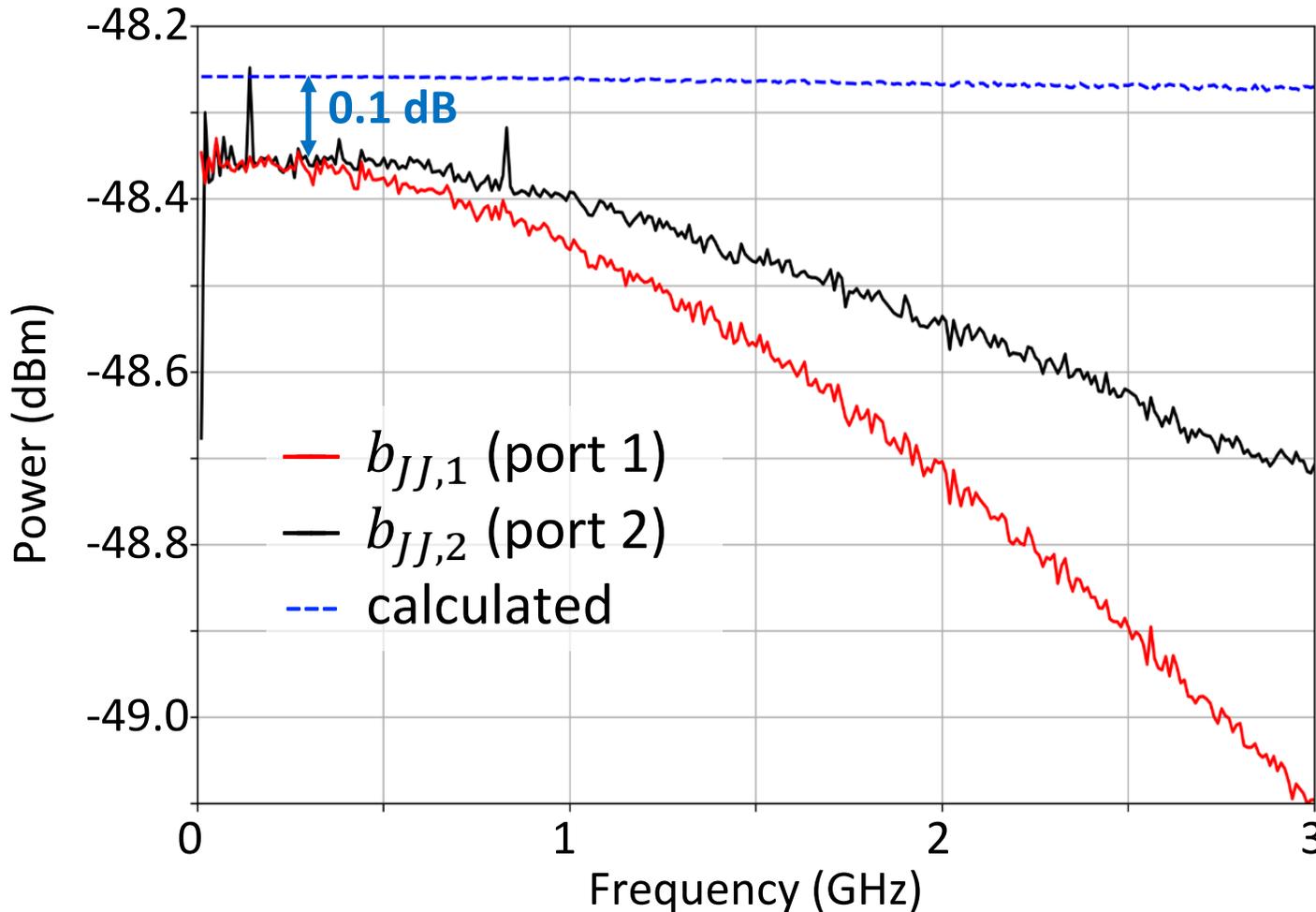
Determine measured JJ waves  $b_{JJ,1}$  and  $b_{JJ,2}$   
 from measured  $a$  and  $b$  waves and  $S$  scattering parameters

$$b_{JJ,1} = b_1 - a_2 * S_{12} - a_1 * S_{11} \quad b_{JJ,2} = b_2 - a_1 * S_{21} - a_2 * S_{22}$$

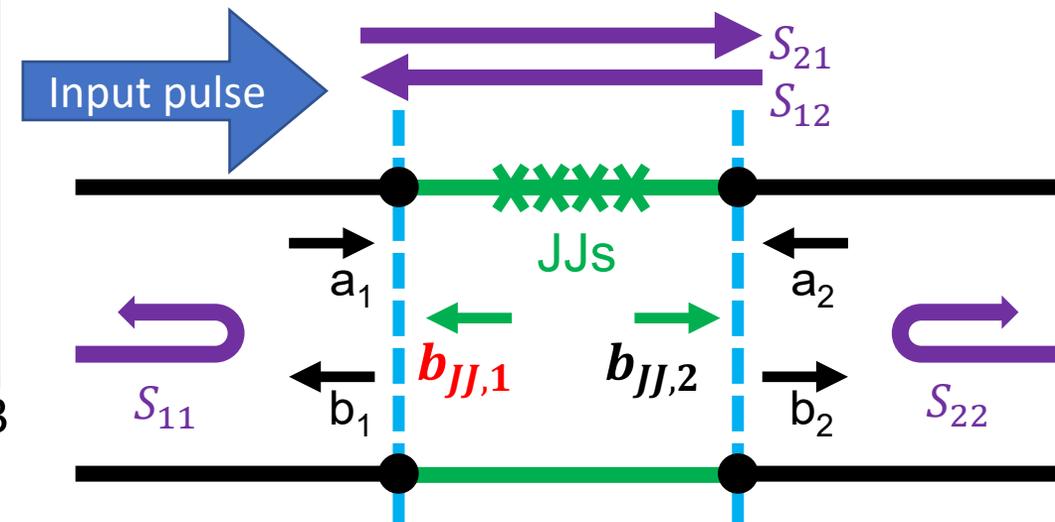
Compare measured/calibrated value to quantum-based calculation (FFT of pulse pattern)

# Preliminary Two Port Results

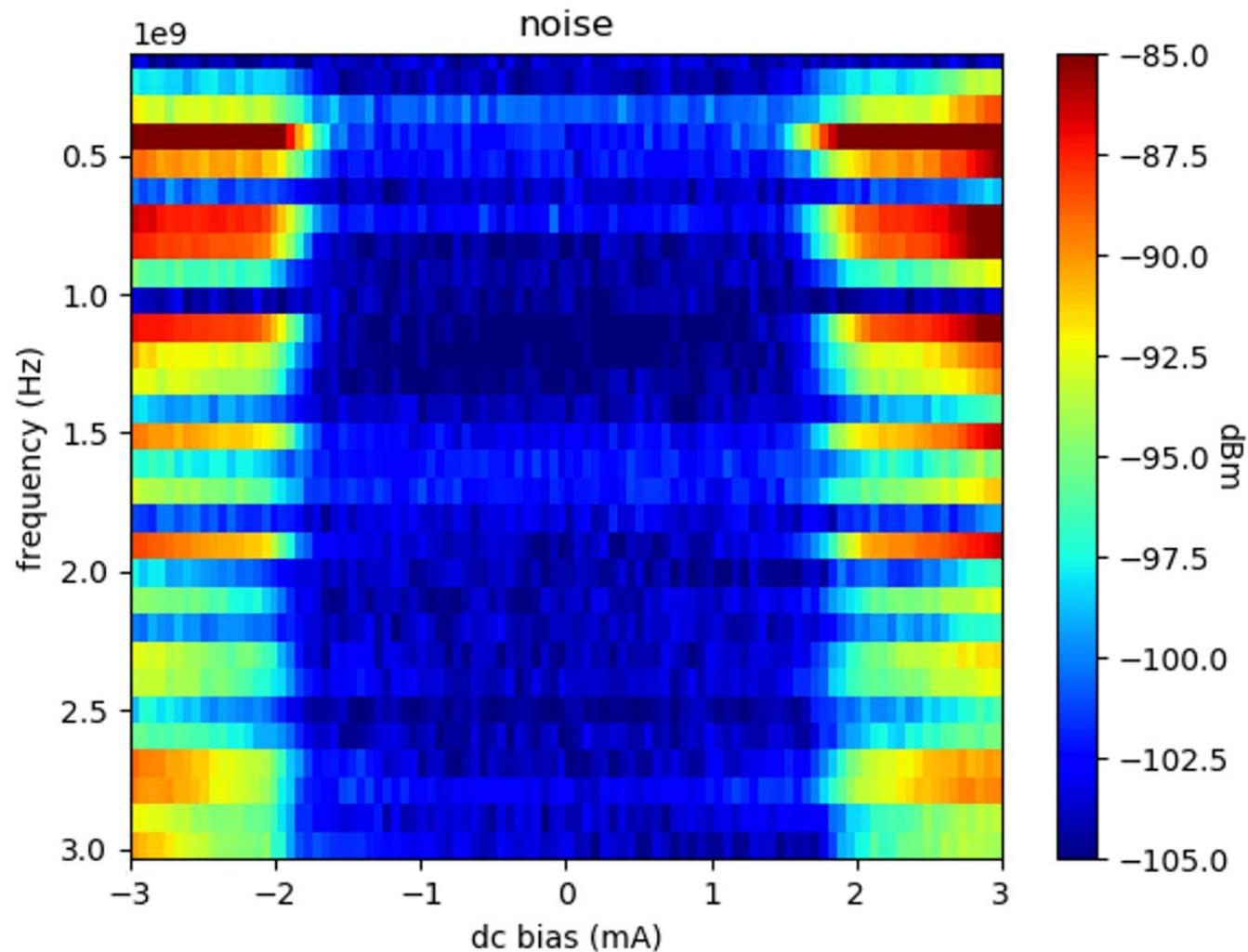
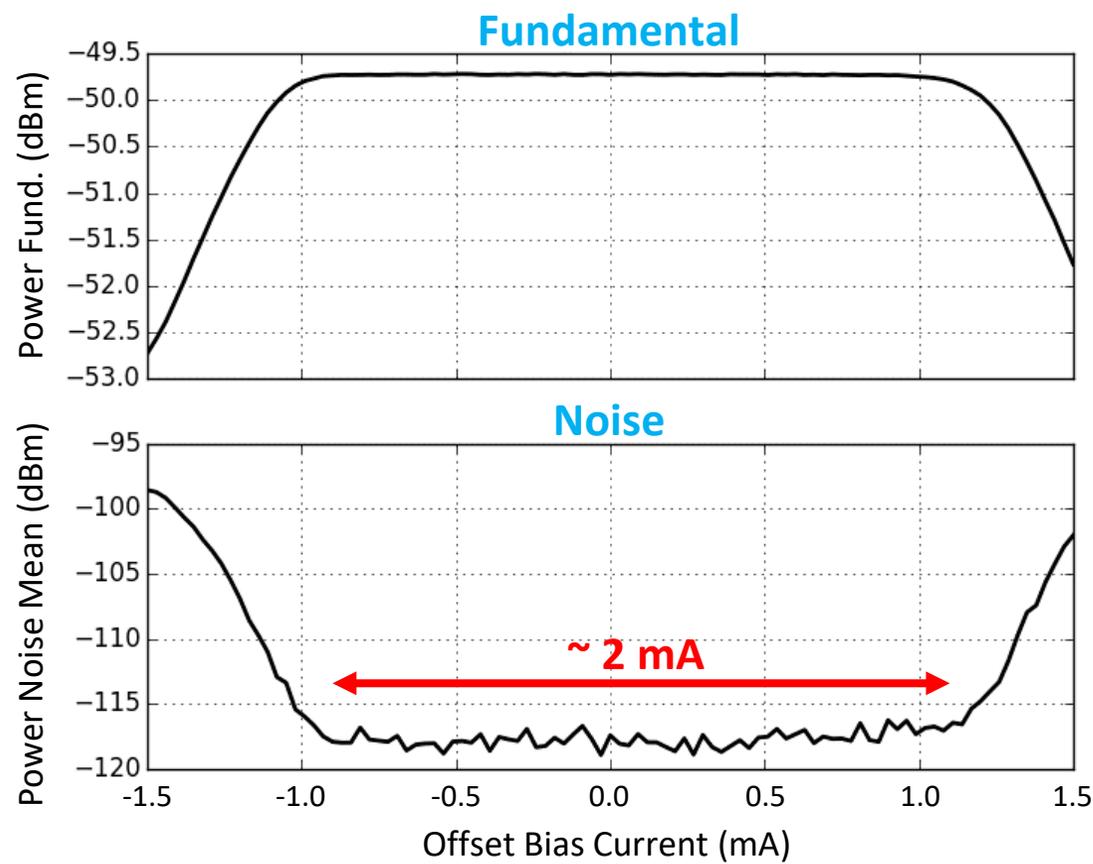
JAWS output at each port



- 0.1 dB low-frequency offset
  - Origin under investigation
- High-frequency roll-off:
  - $b_{JJ,2}$  → finite JJ pulse width
  - $b_{JJ,1}$  → additional time-of-flight broadening of JJ pulse width



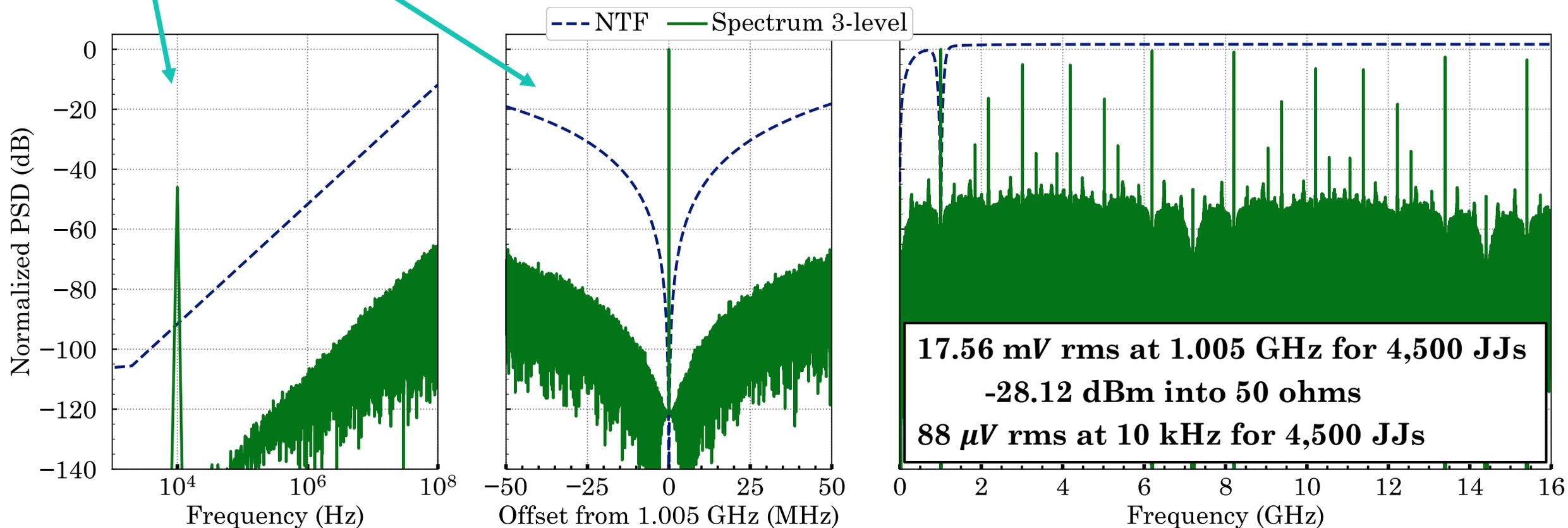
## Single Frequency QLR Sweep



Preliminary QLR measurements

# Two-Tone Delta-Sigma waveform

Low-pass and Band-pass delta-sigma modulators can be combined – NTFs are multiplied



Fast measurements at 10 kHz are used to verify and optimize 1.005 GHz synthesis

NTF – noise transfer function

# Conclusion

- JAWS is a quantum-based voltage source
  - Uses Josephson junctions to convert frequency -> voltage
  - Mature quantum-based DC voltage source (PJVS)
  - Young quantum-based low-frequency voltage source
  - We disseminate PJVS & LF-JAWS as NIST Standard Reference Instruments (SRI)
- Recently started RF-JAWS program: GHz quantum-based arbitrary signal source
  - Generate single-sines for power/phase calibrations
  - Generate multi-tones and pulses for measuring DUT non-linearities
  - Pulsed qubit control
  - Applications increase with frequency and power
- Currently focusing on step 1: Cryogenic probe station measurements
  - Comparing LSNA calibrated measurement to calculated value
  - 0.1 dB agreement at low frequencies and -48 dBm
    - qualitatively understood deviations <0.5 dB up to 3 GHz
- Working on faster JJs and faster pulses, higher frequencies and higher powers

$$\int V(t)dt = \frac{h}{2e}$$

