
BIPM.RI(I)-K2 (ENEA-INMRI 2025)

Measurement of air kerma for low energy x-rays

KEY COMPARISON

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A. Villevalde *et al* 2026 CIPM MRA Comparison reports 06011

<https://doi.org/10.59161/YIMO7019>

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Key comparison BIPM.RI(I)-K2 of the air-kerma standards of the ENEA-INMRI, Italy, and the BIPM in low-energy x-rays

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Abstract A new key comparison has been made between the air-kerma standards of the ENEA-INMRI, Italy, and the BIPM in the low-energy x-ray range. The results show the standards to agree at the level of the expanded uncertainty of the comparison of 8.8 parts in 10³. The results are analysed and presented in terms of degrees of equivalence, suitable for entry in the BIPM key comparison database.

1. Introduction

An indirect comparison has been made between the air-kerma standards of the Istituto Nazionale di Metrologia delle Radiazioni Ionizzanti (INMRI) of the Agenzia Nazionale per le Nuove Tecnologie, l'Energia e lo Sviluppo Economico Sostenibile (ENEA), Italy, and the Bureau International des Poids et Mesures (BIPM) in the x-ray range from 10 kV to 50 kV to update the previous comparison result of 2011 (Burns *et al.* 2011) published in the BIPM key comparison database (KCDB 2026) under the reference BIPM.RI(I)-K2. Three thin-window parallel-plate ionization chambers were used as transfer instruments. The measurements at the BIPM took place in March 2025 using the reference conditions recommended by the CCRI as described in Kessler and Burns (2024). Final data for the evaluation of the comparison results were received from the ENEA-INMRI in June 2025 and the final version of the report in April 2026.

2. Determination of the air-kerma rate

For a free-air ionization chamber standard with measuring volume V , the air-kerma rate is determined by the relation

$$\dot{K} = \frac{I}{\rho_{\text{air}} V} \frac{W_{\text{air}}}{e} \frac{1}{1 - g_{\text{air}}} \prod_i k_i \quad (1)$$

where ρ_{air} is the density of air under reference conditions, I is the ionization current under the same conditions, W_{air} is the mean energy expended by an electron of charge e to produce an ion pair in air, g_{air} is the fraction of the initial electron energy lost through radiative processes in air, and $\prod k_i$ is the product of the correction factors to be applied to the standard.

The value used for ρ_{air} at both laboratories is given in Table 1. For use with this dry-air value, the ionization current measured for the standard must be corrected for humidity and for the difference between the density of the air of the measuring volume at the time of measurement and the value given in the table¹. The value used for W_{air}/e is that recommended in ICRU Report 90 (ICRU 2016) for dry air, also given in Table 1.

¹ For an air temperature $T \sim 293$ K, pressure P and relative humidity ~ 50 % in the measuring volume, the correction for air density for the standard involves a temperature correction T/T_0 , a pressure correction P_0/P and a humidity correction $k_h = 0.9980$.

3. Details of the standards

Both free-air chamber standards are of the conventional parallel-plate design. The BIPM air-kerma standard is described in Boutillon *et al.* (1969) and the changes made to certain correction factors are given in Burns (2004), Burns and Kessler (2009) and Burns *et al.* (2009). Implementation of the recommendations of ICRU Report 90 (ICRU 2016) is reported in Burns and Kessler (2018). The ENEA-INMRI standard is described in the reports of previous comparisons with the BIPM (Burns *et al.* 1999, Burns *et al.* 2011), and the changes made to certain correction factors are given in Laitano *et al.* (2005). The changes implemented following the recommendations of the ICRU Report 90 were applied in April 2021 and reported to the CCRI(I) at the meeting in June 2021. The main dimensions, the measuring volume and the polarizing voltage for each standard are shown in Table 2.

Table 1. Physical constants used in the determination of the air-kerma rate

Constant	Value	u_i ^a
ρ_{air} ^b	1.2045 kg m ⁻³	0.0001
W_{air} / e	33.97 J C ⁻¹	0.0035

^a u_i is the relative standard uncertainty.

^b Density of dry air at $T_0 = 293.15$ K and $P_0 = 101.325$ kPa adopted at the BIPM and at the ENEA-INMRI.

Table 2. Main characteristics of the standards

Standard	BIPM L-01	ENEA-INMRI
Aperture diameter / mm	9.941	8.014
Air path length / mm	100.0	65.12
Collecting length / mm	15.466	40.738
Electrode separation / mm	70	60
Collector width / mm	71	60
Measuring volume / mm ³	1200.4	2054.9
Polarizing voltage / V	1500	1600

4. The transfer instruments

4.1 Determination of the calibration coefficient for a transfer instrument

The air-kerma calibration coefficient N_K for a transfer instrument is given by the relation

$$N_K = \frac{\dot{K}}{I_{\text{tr}}} \quad (2)$$

where $\dot{K}$ is the air-kerma rate determined by the standard using Equation (1) and I_{tr} is the ionization current measured by the transfer instrument and the associated current-measuring system. The current I_{tr} is corrected to the standard conditions of air temperature, pressure and relative humidity chosen for the comparison ($T = 293.15$ K, $P = 101.325$ kPa, $RH = 50$ %). No humidity correction is applied to the current measured using transfer instruments, on the basis that the BIPM laboratory

is maintained with a relative humidity in the range from 40 % to 55 % and the ENEA-INMRI laboratory remained in the range from 45 % to 55 %.

To derive a comparison result from the calibration coefficients $N_{K,BIPM}$ and $N_{K,NMI}$ measured, respectively, at the BIPM and at a national metrology institute (NMI), differences in the radiation qualities must be taken into account. Normally, each quality used for the comparison has the same nominal generating potential and similar filtration at each institute, but the half-value layers (HVLs) can differ appreciably. A radiation quality correction factor k_Q is derived for each comparison quality Q . This corrects the calibration coefficient $N_{K,NMI}$ determined at the NMI into one that applies at the ‘equivalent’ BIPM quality and is derived from a fit to the $N_{K,NMI}$ values in terms of $\log(\text{HVL})$. The comparison result at each quality is then taken as

$$R_K = \frac{k_Q N_{K,NMI}}{N_{K,BIPM}}. \quad (3)$$

In practice, the half-value layers normally differ by only a small amount and k_Q is close to unity. For the present comparison, this is discussed in section 7.2.

4.2 Details of the transfer instruments

Three thin-window parallel-plate ionization chambers belonging to the ENEA-INMRI, two of type Radcal RC6M, serial numbers 10206 and 10279, and one type Exradin Magna A650, serial number D222221, were used as transfer instruments for the comparison. Their main characteristics are given in Table 3. For positioning the chambers at the reference distance, the red line around the casing of the Radcal chambers (8.4 mm and 8.3 mm from the front of the casing for the 10206 and 10279 chambers, respectively) was positioned in the reference plane. Similarly, the black line engraved around the casing of the Exradin Magna A650 chamber (4.0 mm from the front of the casing) was positioned in the reference plane.

Table 3. Main characteristics of the transfer chambers

Chamber type	Radcal RC6M	Exradin Magna A650
Window material	metallized polyester	Kapton
Window thickness / mg cm^{-2}	0.7	3.86
Nominal volume / cm^3	6	3.46
Collector diameter / mm	30 ^a	21.9
Cavity height / mm	8 ^a	7.95
External diameter / mm	43.8	53.4
Polarizing potential ^b / V	300	300

^a The Radcal RC6M cavity dimensions are not clearly stated by the manufacturer. From radiographic measurements, the collector diameter is known to be close to 30 mm, and ionometric measurements indicate a cavity volume of about 5.8 cm^3 , consistent with the value 6 cm^3 stated by the manufacturer. From these, the cavity height is deduced to be around 8.2 mm, which would position the collector close to the red line around the chamber casing.

^b At both laboratories, a positive polarizing potential was applied to the chamber window.

5. Calibration at the BIPM

5.1 The BIPM irradiation facility and reference radiation qualities

The BIPM low-energy x-ray laboratory houses a high-stability generator and a tungsten-anode x-ray tube with an inherent filtration of 1 mm beryllium. A beryllium filter of thickness 2.16 mm is added for all radiation qualities to compensate for the decrease in filtration that occurred when the original BIPM x-ray tube (with a beryllium window of approximately 3 mm) was replaced in 2000; the added thickness was determined experimentally to give a half-value layer (HVL) at 10 kV matching that of the original x-ray tube. A voltage divider is used to measure the generating potential, which is stabilized using an additional feedback system of the BIPM. Rather than using a transmission monitor, which might introduce its own variability, the anode current is measured and the ionization chamber current is normalized for any deviation from the reference anode current. The standard deviation of repeat air-kerma rate determinations over many months is typically 3 parts in 10^4 . The radiation qualities used in the range from 10 kV to 50 kV are those recommended by the CCRI and are given in Table 4 in ascending HVL from left to right.

At the BIPM, the reference distance is 500 mm from the exit window of the W-anode x-ray tube, with a beam diameter of 84 mm. However, since the calibration of the Radcal RC6M and Exradin Magna A650 chambers were performed at the ENEA-INMRI at 500 mm distance from the radiation source with a beam diameter of 50 mm, and at 1000 mm distance from the radiation source with a beam diameter of 100 mm, respectively, similar measurement conditions were used at the BIPM, as explained in sections 5.2 and 6.2.

The irradiation area is temperature controlled at around 20 °C and is stable over the duration of a calibration to better than 0.1 °C. Two calibrated thermistors measure the temperature of the ambient air and the air inside the BIPM standard. Air pressure is measured by means of a calibrated barometer.

Table 4. Characteristics of the BIPM reference radiation qualities

Radiation quality	10 kV	30 kV	25 kV	50 kVb	50 kVa
Generating potential / kV	10	30	25	50	50
Additional Al filtration / mm	0	0.208	0.372	1.008	3.989
Al HVL / mm (0.5 m)	0.037	0.169	0.242	1.017	2.262
Al HVL ^a / mm (1 m)	0.045	0.195	0.265	1.041	2.274
$(\mu/\rho)_{\text{air}}^b / \text{cm}^2 \text{g}^{-1}$ (0.5 m)	14.84	3.662	2.604	0.754	0.379
$(\mu/\rho)_{\text{air}}^{a, b} / \text{cm}^2 \text{g}^{-1}$ (1 m)	12.05	3.283	2.408	0.735	0.399
$\dot{K}_{\text{BIPM}} / \text{mGy s}^{-1}$ (0.5 m)	1.00	1.00	1.00	1.00	1.00
$\dot{K}_{\text{BIPM}} / \text{mGy s}^{-1}$ (1 m)	0.26	0.21	0.22	0.25	0.25

^a Measured at 1 m as described in Villevalde *et al.* (2020).

^b Measured for an equivalent air-path length of 100 mm using a variable-pressure tube.

5.2 BIPM standard and correction factors

As mentioned above, for the present comparison the reference plane for the BIPM standard was positioned at 500 mm and at 1000 mm from the exit window of the x-ray tube for the calibration of the Radcal RC6M chambers and the Exradin Magna A650 chamber, respectively, with a

reproducibility of 0.03 mm. The standard was aligned on the beam axis to an estimated uncertainty of 0.1 mm. For these measurements, an additional tungsten collimator was used to give a beam diameter of around 50 mm at the reference distance of 500 mm and around 100 mm at the distance of 1000 mm for all radiation qualities to reproduce the ENEA measurement conditions.

For the calibration of the transfer chambers, measurements using the BIPM standard were made using positive polarity only. A correction factor of 1.0005 is applied to correct for the known polarity effect in the standard (see Table 5). The leakage current for the BIPM standard relative to the ionization current was measured to be less than 1 part in 10^4 .

The correction factors applied to the ionization current measured at each radiation quality using the BIPM standard, together with their associated standard uncertainties, are given in Table 5.

The largest correction is that due to the attenuation of the x-ray fluence along the air path between the reference plane and the centre of the collecting volume. The corresponding correction factor k_a is evaluated using the measured mass attenuation coefficients for air $(\mu/\rho)_{\text{air}}$ given in Table 4 for both distances. In practice, the values used for k_a take account of the temperature and pressure of the air in the standard.

Table 5. Correction factors and uncertainties for the BIPM standard

Radiation quality	10 kV	30 kV	25 kV	50 kVb	50 kVa	u_{iA}	u_{iB}
Air attenuation k_a^a (0.5 m)	1.1956	1.0451	1.0319	1.0091	1.0046	0.0002	0.0001
Air attenuation k_a^a (1 m)	1.1563	1.0403	1.0294	1.0089	1.0048	0.0002	0.0001
Photon scatter k_{sc}	0.9962	0.9972	0.9973	0.9977	0.9979	-	0.0003
Fluorescence k_{fl}	0.9952	0.9971	0.9969	0.9980	0.9985	-	0.0005
Electron loss k_e	1.0000	1.0000	1.0000	1.0000	1.0000	-	0.0001
Initial ionization k_{ii}^b	0.9953	0.9968	0.9969	0.9977	0.9980	-	0.0012
Energy dependence of $W_{\text{air}} k_W^b$							
Ion recombination k_s (0.5 m)	1.0006	1.0007	1.0007	1.0007	1.0007	0.0001	0.0001
Ion recombination k_s (1 m)	1.0003	1.0004	1.0004	1.0004	1.0004	0.0001	0.0001
Polarity k_{pol}	1.0005	1.0005	1.0005	1.0005	1.0005	0.0001	-
Field distortion k_d	1.0000	1.0000	1.0000	1.0000	1.0000	-	0.0007
Diaphragm effects k_{dia}	0.9999	0.9995	0.9996	0.9989	0.9984	-	0.0003
Wall transmission k_p	1.0000	1.0000	1.0000	1.0000	1.0000	0.0001	-
Humidity k_h	0.9980	0.9980	0.9980	0.9980	0.9980	-	0.0003
$1 - g_{\text{air}}$	1.0000	1.0000	1.0000	1.0000	1.0000	-	0.0001

^a Values for 293.15 K and 101.325 kPa; each measurement is corrected using the air density measured at the time.

^b The stated values are for the product $k_{ii}k_W$, as presented in Burns and Kessler (2018).

5.3 Transfer chamber positioning and calibration at the BIPM

The reference point for each chamber was positioned in the reference plane with a reproducibility of 0.03 mm. Each transfer chamber was aligned laterally on the beam axis to an estimated uncertainty of 0.1 mm. The leakage current was measured before and after each series of ionization current measurements and a correction made using the mean value. The leakage current relative to the ionization current for each chamber was less than 1 part in 10^4 .

The calibration procedure involves measurements with a transfer chamber and with the standard at a given radiation quality before proceeding to the next quality, with a period of typically 10 minutes following a change of quality to allow the generator and tube to stabilize (longer for the 50 kVa quality). For each of the transfer chambers at each radiation quality, the relative standard uncertainty of the mean ionization current was below 3 parts in 10^4 . Based on the results of repeat calibrations including chamber repositioning and on long-term experience of calibrations in these beams, an uncertainty component of 5 parts in 10^4 is included in Table 12 for the short-term reproducibility of the calibration coefficients determined at the BIPM.

6. Calibration at the ENEA-INMRI

6.1 ENEA-INMRI irradiation facility and reference radiation qualities

The low-energy x-ray facility at the ENEA-INMRI uses a constant-potential generator and a tungsten-anode tube with an inherent filtration of 0.8 mm beryllium. The x-ray output is monitored by means of a free-air, custom-made monitor ionization chamber. The standard deviation of repeated determinations of the air-kerma rate at either 500 mm or 1000 mm distance from the radiation source, on average across all qualities, over the period of a transfer chamber calibration, is less than 3 parts in 10^3 . The generating potential is measured invasively with a voltage divider.

To determine the chamber calibration coefficient, sequential measurements were carried out using the primary standard and the transfer ionization chamber, without applying monitor chamber normalization.

The characteristics of the ENEA-INMRI radiation qualities are given in Table 6.

Table 6. Characteristics of the ENEA-INMRI reference radiation qualities

Radiation quality	10 kV	30 kV	25 kV	50 kVb	50 kVa
Generating potential / kV	10	30	25	50	50
Additional Al filtration / mm	0	0.25	0.39	1.01	4.05
Al HVL / mm (0.5 m)	0.031	0.169	0.236	1.021	2.282
Al HVL / mm (1 m)	0.039	0.204	0.254	1.046	2.282
$(\mu/\rho)_{\text{air}}^a / \text{cm}^2 \text{g}^{-1}$ (0.5 m)	17.99	3.700	2.760	0.823	0.426
$(\mu/\rho)_{\text{air}}^a / \text{cm}^2 \text{g}^{-1}$ (1 m)	13.68	3.300	2.550	0.798	0.393
$\dot{K}_{\text{ENEA-INMRI}} / \text{mGy s}^{-1}$ (0.5 m)	6.05	7.20	5.48	10.78	2.24
$\dot{K}_{\text{ENEA-INMRI}} / \text{mGy s}^{-1}$ (1 m)	0.60	3.05	1.21	2.67	0.57

^a Measured using a variable-pressure tube. The determination of the mass attenuation coefficient relies on a correction to account for the attenuation effects of the two 0.5 mm beryllium windows that act as walls of the tube.

The irradiation area is temperature controlled around 20 °C and is stable over the duration of a calibration to better than 0.5 °C. Two calibrated NTC type thermometers are used to measure air temperature, one positioned either inside the primary standard or near the transfer chamber under calibration, and the second located near the monitor chamber. The air pressure is measured using a calibrated barometer whose probe is positioned at approximately the same height as the beam central axis.

6.2 ENEA-INMRI standard and correction factors

At the ENEA-INMRI, the reference distance is 500 mm from the exit window of the x-ray tube, with a beam diameter of 50 mm. The Radcal chambers were calibrated using these reference conditions. However, the calibration of the Exradin Magna A650 chamber, due to its larger external diameter, was performed at 1000 mm from the exit window of the x-ray tube, where the beam diameter is 100 mm. The reference plane for the ENEA-INMRI standard was positioned at the mentioned distances with an uncertainty of about 0.1 mm and 1 mm, respectively. The standard was aligned laterally on the beam axis with an estimated uncertainty of about 0.2 mm.

Table 7. Correction factors and uncertainties for the ENEA-INMRI standard

Radiation quality	10 kV	30 kV	25 kV	50 kVb	50 kVa	u_{iA}	u_{iB}
Air attenuation k_a^a (0.5 m)	1.1515	1.0294	1.0219	1.0065	1.0033	0.0002	0.0010
Air attenuation k_a^a (1 m)	1.1133	1.0262	1.0202	1.0063	1.0031	0.0002	0.0010
Scattered radiation k_{sc}	0.9973	0.9981	0.9982	0.9985	0.9986	-	0.0006
Fluorescence k_f	0.9963	0.9976	0.9978	0.9986	0.9989	-	0.0006
Electron loss k_e	1.0000	1.0000	1.0000	1.0001	1.0003	-	0.0002
Initial ionization k_{ii}^b	0.9952	0.9968	0.9969	0.9977	0.9980	-	0.0012
Energy dependence of $W_{air} k_W^b$							
Ion recombination k_s (0.5 m)	1.0011	1.0014	1.0011	1.0019	1.0007	-	0.0005
Ion recombination k_s (1 m)	1.0005	1.0009	1.0006	1.0008	1.0005	-	0.0005
Polarity k_{pol}	0.9999	0.9999	0.9999	0.9999	0.9999	-	0.0006
Field distortion k_d	1.0000	1.0000	1.0000	1.0000	1.0000	-	0.0010
Aperture transmission k_l	1.0000	0.9997	0.9997	0.9992	0.9990	-	0.0004
Wall transmission k_p	1.0000	1.0000	1.0000	1.0000	1.0000	-	0.0005
Humidity k_h^c	0.9980	0.9980	0.9980	0.9980	0.9980	-	0.0003
$1 - g_{air}$	1.0000	1.0000	1.0000	1.0000	1.0000	-	0.0001

^a Values for 293.15 K and 101.325 kPa; each measurement is corrected using the air density measured at the time.

^b The stated values are for the product $k_{ii}k_W$ implemented according to ICRU Report 90 (ICRU 2016).

^c Each measurement is corrected using the relative partial vapor pressure calculated at the time of measurement, according to ICRU Report 31 (ICRU 1979).

During the calibration of the transfer chambers, measurements using the ENEA-INMRI standard were made using positive polarity only. A correction factor included in Table 7 is applied to correct for the known polarity effect in the standard. The leakage current for the ENEA-INMRI standard was below 0.8 pA (worst case), corresponding to less than 4 parts in 10^3 , relative to the ionization current.

The correction factors applied to the ionization current measured at each radiation quality using the ENEA-INMRI standard, together with their associated uncertainties, are given in Table 7.

The correction factors k_a are evaluated using the measured mass attenuation coefficients for air given in Table 6. In practice, the values used for k_a take account of the temperature and pressure of the air in the standard at the time of the measurements.

6.3 Transfer chamber positioning and calibration at the ENEA-INMRI

The reference point of the transfer chamber was positioned at 500 mm from the exit window of the x-ray tube for the Radcal RC6M chambers and at 1000 mm from the exit window of the x-ray tube for the Exradin Magna A650 chamber, with an uncertainty of around 0.1 mm and 1 mm, respectively. Each transfer chamber was aligned laterally on the beam axis to an estimated uncertainty of 0.2 mm. The leakage current was measured for each measurement series and a correction applied. The leakage current was typically below 0.3 pA (worst case), corresponding to less than 6 parts in 10^4 relative to the ionization current measured at the distance of 500 mm and was typically below 90 fA (worst case), corresponding to less than 1 part in 10^3 relative to the ionization current measured at 1000 mm.

For each transfer chamber at each radiation quality, four calibrations were made before the measurements at the BIPM and one following the return of the chambers to the ENEA-INMRI. The uncertainty arising from these repeat measurements is discussed in Section 8.

7. Additional considerations for transfer chamber calibrations

7.1 Ion recombination, polarity, radial non-uniformity, distance and field size

Ion recombination: As can be seen from Tables 4 and 6, the ENEA-INMRI and BIPM air-kerma rates differ significantly for both reference distances. The ENEA-INMRI applies a correction for ion recombination $k_{s,tr}$ calculated for each radiation quality as

$$k_{s,tr} = 1 + k_{init} + k_{vol} \times I \quad (4)$$

where k_{init} is the initial recombination and k_{vol} is the volume recombination determined using the Niatel method (Boutillon 1998). The values determined at the ENEA-INMRI for both transfer chamber types are given in Table 8.

For consistency, the BIPM results have been corrected by $k_{s,tr}$ using the ENEA-INMRI determination and a corresponding uncertainty for ion recombination is included in Table 13.

Table 8. Ion recombination for the transfer chambers determined at the ENEA-INMRI

Coefficient	Radcal RC6M	Exradin Magna A650
Initial recombination, k_{init}	0.00196	0.00032
Volume recombination, k_{vol} / A^{-1}	6.68×10^5	3.92×10^5

Polarity: Each transfer chamber was used with the same polarity at each laboratory and so no correction is applied for the polarity effect.

Radial non-uniformity: The ENEA-INMRI correction for the radial non-uniformity of the beam

was determined from measured beam profiles at the reference distances of 500 mm and 1000 mm. The correction for finite chamber dimensions was taken into account according to Kondo and Randolph (1960) and Bielajew (1990). For the Radcal RC6M chambers with a collector diameter of 30 mm, the resulting correction at 500 mm is 1.0021(11). For the Exradin Magna A650 chamber, with a collector diameter of 21.9 mm, the correction at 1000 mm is 1.0009(11). A similar correction was calculated for the BIPM beams. No correction $k_{m,tr}$ is applied at either laboratory for the radial non-uniformity of the radiation field and a relative standard uncertainty of 1 part in 10^3 is included in Table 13.

Distance: As the chambers were calibrated at the BIPM at the same distances as the ENEA (500 mm and 1000 mm for the Radcal RC6M and Exradin Magna A650 chambers, respectively), no correction for the distance effect is applied.

Field size: No correction is applied for field size as the BIPM field diameter was modified to match the ENEA-INMRI field size.

7.2 Radiation quality correction factors k_Q

As noted in Section 4.1, slight differences in the realizations of the CCRI radiation qualities at the ENEA-INMRI and the BIPM might require a correction factor k_Q . To derive a comparison result for the BIPM HVL values, quadratic fits were made to the ENEA-INMRI data sets for the Radcal RC6M chambers and a cubic fit for the Exradin Magna A650 chamber, as shown in Figure 1. From the fits, the values for correction factors k_Q given in Table 9 were obtained and applied to the ENEA-INMRI calibration coefficients according to Equation (3). The uncertainty of these corrections, estimated to be 3 parts in 10^4 , is included in Table 13.

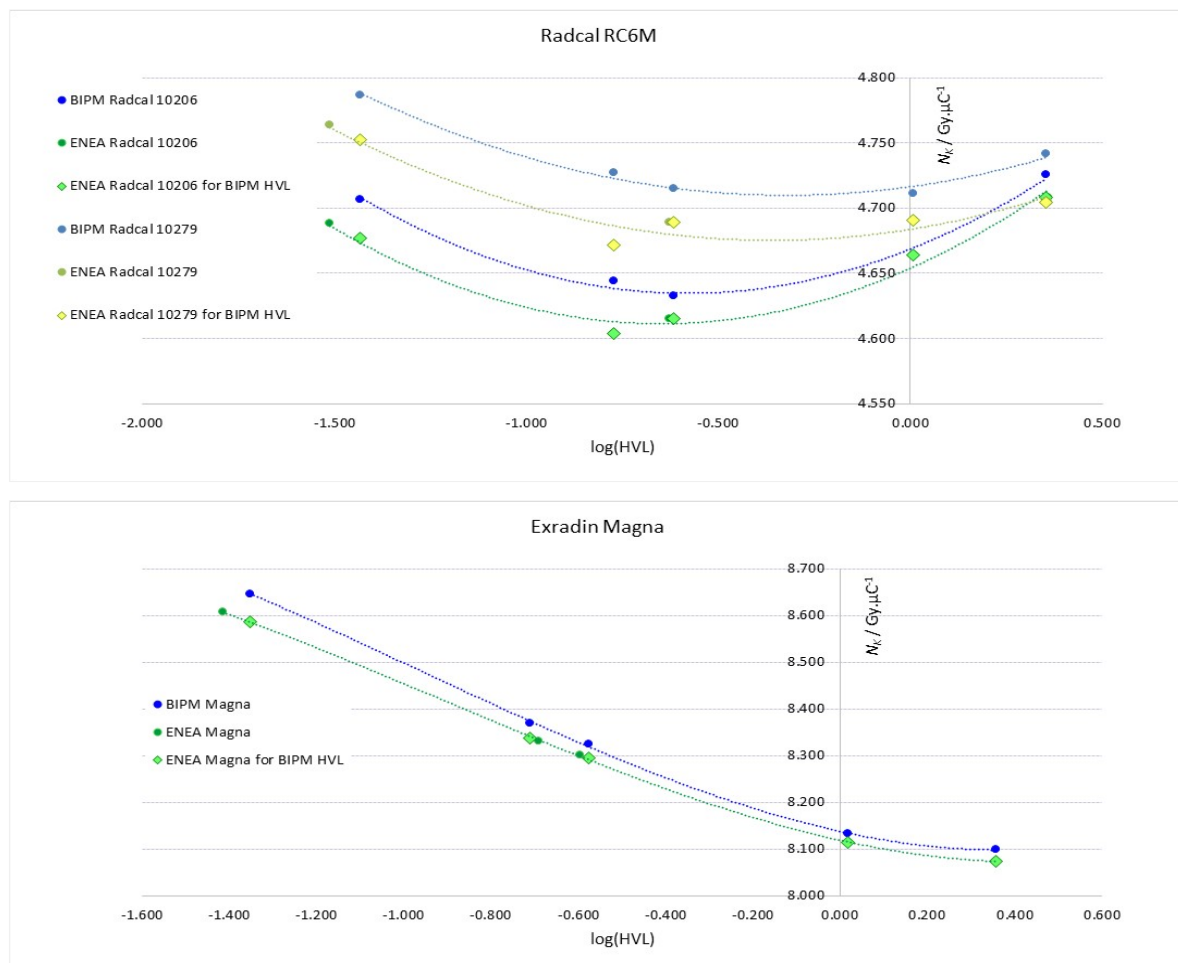


Figure 1. Calibration coefficients determined at the ENEA-INMRI and the BIPM

8. Comparison results

The calibration coefficients $N_{K,ENE\text{-}INMRI}$ and $N_{K,BIPM}$ for the transfer chambers are presented in Table 9. For each chamber at each radiation quality, the values $N_{K,ENE\text{-}INMRI}$ provided before and after the measurements at the BIPM give rise to the mean value used for the final comparison result and a relative standard uncertainty s_{stab} representing the chamber stability².

Table 9. Calibration coefficients for the transfer chambers

Radiation quality	10 kV	30 kV	25 kV	50 kVb	50 kVa
<i>Radcal RC6M-10206</i>					
$N_{K,ENE\text{-}INMRI}$ (pre-BIPM) / Gy μC^{-1}	4.699	4.613	4.618	4.677	4.708
$N_{K,ENE\text{-}INMRI}$ (post-BIPM) / Gy μC^{-1}	4.678	4.594	4.612	4.651	4.709
$s_{\text{stab},1}$	0.0041	0.0038	0.0012	0.0051	0.0002
k_Q for $N_{K,ENE\text{-}INMRI}$	0.9973	1.0000	1.0000	1.0000	0.9999
$N_{K,BIPM}$ / Gy μC^{-1}	4.707	4.644	4.633	4.664	4.726
<i>Radcal RC6M-10279</i>					
$N_{K,ENE\text{-}INMRI}$ (pre-BIPM) / Gy μC^{-1}	4.775	4.677	4.693	4.701	4.707
$N_{K,ENE\text{-}INMRI}$ (post-BIPM) / Gy μC^{-1}	4.753	4.667	4.686	4.681	4.702
$s_{\text{stab},2}$	0.0042	0.0020	0.0014	0.0039	0.0010
k_Q for $N_{K,ENE\text{-}INMRI}$	0.9977	1.0000	1.0000	1.0000	0.9999
$N_{K,BIPM}$ / Gy μC^{-1}	4.787	4.727	4.715	4.711	4.742
<i>Exradin Magna A650-D222221</i>					
$N_{K,ENE\text{-}INMRI}$ (pre-BIPM) / Gy μC^{-1}	8.595	8.315	8.287	8.097	8.059
$N_{K,ENE\text{-}INMRI}$ (post-BIPM) / Gy μC^{-1}	8.620	8.347	8.316	8.132	8.090
$s_{\text{stab},3}$	0.0027	0.0035	0.0032	0.0040	0.0035
k_Q for $N_{K,ENE\text{-}INMRI}$	0.9975	1.0009	0.9992	1.0001	1.0000
$N_{K,BIPM}$ / Gy μC^{-1}	8.647	8.369	8.325	8.133	8.099

The comparison results R_K are presented in Table 10, evaluated according to Equation (3). For each radiation quality the final comparison result is evaluated as the mean for the three transfer chambers. The uncertainty s_{tr} is the standard uncertainty of this mean, or taken as

$$s_{\text{tr}} = \sqrt{s_{\text{stab},1}^2 + s_{\text{stab},2}^2 + s_{\text{stab},3}^2} / 3 \quad (5)$$

² Because of the very small sample size, the modified standard uncertainty including the appropriate t -factor is used, which for $n = 2$ gives $s_{\text{stab}} = 1.8 s_{\text{dev},s} / \sqrt{2}$.

if this is larger (on the basis that the agreement between the comparison results for different transfer chambers should not, on average, be better than their combined stability estimated using $S_{\text{stab},1}$, $S_{\text{stab},2}$ and $S_{\text{stab},3}$ from Table 9). The root mean squared (rms) value of s_{tr} for the five qualities, $s_{\text{tr,comp}} = 0.0023$, is taken to represent the uncertainty arising from the transfer chambers and is included in Table 13.

Table 10. Combined comparison results

Radiation quality	10 kV	30 kV	25 kV	50 kVb	50 kVa
R_K using Radcal RC6M-10206	0.9934	0.9913	0.9961	1.0000	0.9962
R_K using Radcal RC6M-10279	0.9929	0.9884	0.9946	0.9958	0.9920
R_K using Exradin Magna A650-D222221	0.9929	0.9964	0.9964	0.9978	0.9970
s_{tr}	0.0022	0.0032	0.0012	0.0025	0.0021
Final R_K	0.9931	0.9920	0.9957	0.9979	0.9951
<i>Updated results of 2011</i>	0.9981	0.9972	0.9978	0.9977	0.9972

Also given in the final row of Table 10 are the results for the ENEA-INMRI from the previous comparison in 2011, revised for the changes made to the standards in the interim period (k_{sc} , k_{fl} , k_{e} , k_{l} and k_{ikw}).

9. Uncertainties

The uncertainties associated with the primary standards are listed in Table 11, and those for the transfer chamber calibrations in Table 12. The combined standard uncertainty u_c for the comparison results R_K is presented in Table 13.

Table 11. Uncertainties associated with the standards

Standard	BIPM L-01		ENEA-INMRI	
Relative standard uncertainty	u_{IA}	u_{IB}	u_{IA}	u_{IB}
Ionization current	0.0002	0.0002	0.0005	0.0016
Air density correction	-	-	0.0002	0.0004
Leakage	-	-	-	0.0005
Positioning	0.0001	0.0001	-	0.0002
Volume	0.0003	0.0005	-	0.0005
Correction factors (excl. k_{h})	0.0003	0.0015	0.0002	0.0023
Humidity k_{h}	-	0.0003	-	0.0003
Physical constants	-	0.0035	-	0.0035
$\dot{K}$	0.0005	0.0039	0.0006	0.0046

Table 12. Uncertainties associated with the calibration of the transfer chambers

Institute	BIPM		ENEA-INMRI	
Relative standard uncertainty	u_{iA}	u_{iB}	u_{iA}	u_{iB}
$\dot{K}$	0.0005	0.0039	0.0006	0.0046
I_{tr}	0.0002	0.0002	0.0010	0.0016
Humidity	-	-	-	0.0003
Positioning of transfer chamber	0.0001	-	-	0.0010
Reproducibility	0.0005	-	0.0020	-
N_K	0.0007	0.0039	0.0023	0.0050

Table 13. Uncertainties associated with the comparison results

Relative standard uncertainty	u_{iA}	u_{iB}
$N_{K,ENEA-INMRI} / N_{K,BIPM}$	0.0024	0.0027 ^a
Ion recombination	-	0.0005
Radial non-uniformity	-	0.0010
k_Q	-	0.0003
Transfer chambers $s_{tr,comp}$	0.0023	-
R_K	0.0033	0.0029 ^a
	$u_c = 0.0044a$	

^a Takes account of correlation in type B uncertainties.

The combined standard uncertainty of the comparison result takes into account correlation in the type B uncertainties associated with the physical constants, the humidity correction and the factor $k_{ij}k_W$. Correlation in the values for k_e , k_l , k_{sc} and k_{fl} , derived from Monte Carlo calculations in each laboratory, are taken into account in an approximate way by assuming half of the uncertainty value for each factor at each laboratory. This is consistent with the analysis of the results of BIPM comparisons in low-energy x-rays in terms of degrees of equivalence described in Burns (2003).

10. Discussion

The comparison results R_K show the ENEA-INMRI and BIPM standards to agree at the level of the expanded uncertainty of the comparison of 8.8 parts in 10^3 .

The results agree with the results of the direct comparison carried out in 2011 at the level of the expanded standard uncertainty of the comparisons. The differences for 10 kV and 30 kV radiation qualities are around 5 parts in 10^3 , while for other qualities they are typically around 2 parts in 10^3 .

11. Degrees of Equivalence

The analysis of the results of BIPM comparisons in low-energy x-rays in terms of degrees of equivalence is described in Burns (2003). Following a decision of the CCRI, the BIPM determination of the air-kerma rate is taken as the key comparison reference value, for each of the CCRI radiation qualities. It follows that for each laboratory i having a BIPM comparison result x_i with combined standard uncertainty u_i , the degree of equivalence with respect to the reference value is the relative difference $D_i = (\bar{K}_i - \bar{K}_{\text{BIPM},i}) / \bar{K}_{\text{BIPM},i} = x_i - 1$ and its expanded uncertainty $U_i = 2 u_i$. The results for D_i and U_i , expressed in mGy/Gy and including those of the present comparison, are shown in Table 14 and in Figure 2.

12. Conclusions

The key comparison BIPM.RI(I)-K2 for the determination of air-kerma in low-energy x-rays shows the standards of the ENEA-INMRI and the BIPM to agree at the level of the expanded uncertainty of the comparison of 8.8 parts in 10^3 .

Tables and a graph of degrees of equivalence, including those for the ENEA-INMRI, are presented for entry in the BIPM key comparison database. Note that these data, while correct at the time of publication of the present report, become out of date as laboratories make new comparisons. In accordance with the validity rules for comparison data agreed by the CCRI(I), results older than 15 years are considered no longer valid and have been removed from the KCDB. The formal results under the CIPM MRA are those available in the key comparison database (KCDB 2026).

Table 14. Degrees of equivalence

For each laboratory i , the degree of equivalence with respect to the key comparison reference value is the difference D_i and its expanded uncertainty U_i .

Lab i	Year	10 kV		30 kV		25 kV		50 kVb		50 kVa	
		D_i	U_i	D_i	U_i	D_i	U_i	D_i	U_i	D_i	U_i
		/(mGy/Gy)		/(mGy/Gy)		/(mGy/Gy)		/(mGy/Gy)		/(mGy/Gy)	
LNE-LNHB *	2009	-0.8	4.0	0.2	4.0	0.7	4.0	0.1	4.0	0.7	4.0
VNIM	2011	-3.2	5.3	-2.1	5.3	-2.2	5.3	-1.3	5.3	-0.7	5.3
VSL	2012	7.8	7.0	6.9	7.0	7.5	7.0	11.5	7.0	13.0	7.0
BEV	2014	-2.0	14	-0.8	9.8	-1.3	9.8	-0.8	9.8	-1.6	9.8
NMIJ	2014	3.2	6.5	1.0	6.5	-2.3	6.5	-0.9	6.5	-2.6	6.5
CMI	2015	5.5	7.4	3.9	7.4	4.5	7.4	4.2	7.4	4.4	7.4
KRISS	2017	-1.6	4.4	-2.4	4.4	-1.6	4.4	-1.8	4.4	-1.9	4.4
NPL	2017	-12.2	4.9	-11.4	4.9	-11.1	4.9	-10.1	4.9	-9.6	4.9
NRC	2018	0.3	7.1	-2.4	7.1	-1.4	7.1	0.6	7.1	0.4	7.1
NIM	2018	-2.3	7.7	-1.1	7.7	0.5	7.7	-2.5	7.7	-3.2	7.7
GUM	2021	-5.9	5.8	5.2	5.8	1.9	5.8	3.1	5.8	1.9	5.8
BFKH	2021			-4.3	6.8	-4.0	6.8	-0.4	6.8	0.1	6.8
ARPANSA	2022	11.2	22	-7.6	9.2			-5.4	9.2	-4.8	9.2
PTB	2024	0.2	8.0	-2.8	8.0	-1.1	8.0	-1.2	8.0	-5.4	8.0
ENEA	2025	-6.9	8.8	-8.0	8.8	-4.3	8.8	-2.1	8.8	-4.9	8.8

* Results older than 15 years; participation in the comparison is planned for 2026/2027.

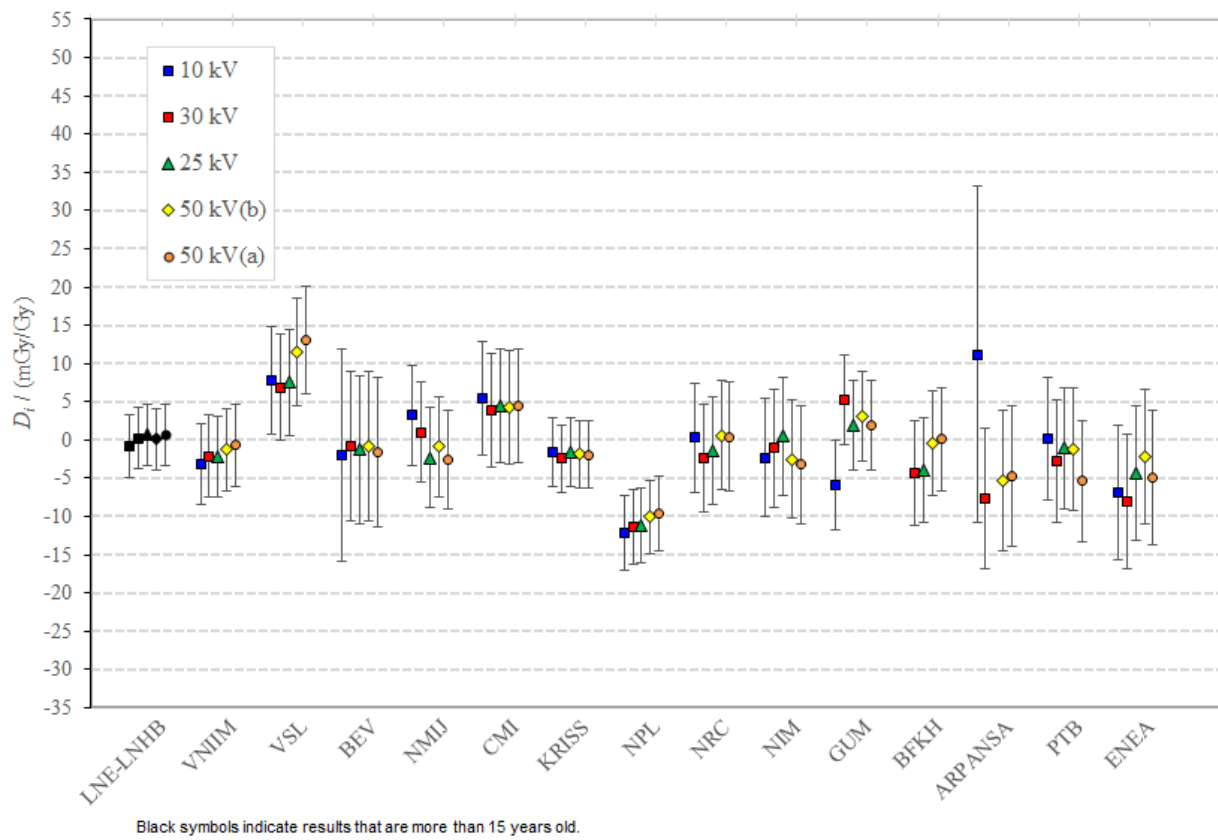


Figure 2. Degrees of equivalence for each laboratory i with respect to the key comparison reference value

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