

## Key comparison BIPM.RI(I)-K3 of the air-kerma standards of the GUM, Poland, and the BIPM in medium-energy x-rays

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**Abstract** A key comparison has been made between the air-kerma standards of the GUM and the BIPM in the medium-energy x-ray range. The results show the standards to be in agreement at the level of the expanded uncertainty of the comparison of 6.0 parts in 10<sup>3</sup>. The results are analysed and presented in terms of degrees of equivalence, suitable for entry in the BIPM key comparison database.

### 1. Introduction

An indirect comparison has been made between the air-kerma standards of the Główny Urząd Miar (GUM), Poland, and the Bureau International des Poids et Mesures (BIPM) in the x-ray range from 100 kV to 250 kV. Two cavity ionization chambers were used as transfer instruments. The measurements at the BIPM took place in June 2020 using the reference conditions recommended by the CCRI (CCEMRI 1972). The comparison was carried out after the implementation of the recommendations of ICRU Report 90 (ICRU 2016) at both laboratories. Final results were received from the GUM in March 2021.

### 2. Determination of the air-kerma rate

For a free-air ionization chamber standard with measuring volume  $V$ , the air-kerma rate is determined by the relation

$$\dot{K} = \frac{I}{\rho_{\text{air}} V} \frac{W_{\text{air}}}{e} \frac{1}{1 - g_{\text{air}}} \prod_i k_i \quad (1)$$

where  $\rho_{\text{air}}$  is the density of air under reference conditions,  $I$  is the ionization current under the same conditions,  $W_{\text{air}}$  is the mean energy expended by an electron of charge  $e$  to produce an ion pair in air,  $g_{\text{air}}$  is the fraction of the initial electron energy lost through radiative processes in air, and  $\prod k_i$  is the product of the correction factors to be applied to the standard.

The value used for  $\rho_{\text{air}}$  at each laboratory is given in Table 1. For use with this dry-air value for  $\rho_{\text{air}}$ , the ionization current  $I$  must be corrected for humidity and for the difference between the density of the air of the measuring volume at the time of measurement and the value given in the table<sup>1</sup>. The value used for  $W_{\text{air}}/e$  is that recommended in ICRU Report 90 (ICRU 2016), also given in Table 1.

### 3. Details of the standards

Both free-air chamber standards are of the conventional parallel-plate design. The BIPM air-kerma standard is described in Boutillon (1978) and the changes made to certain correction factors are

<sup>1</sup> For an air temperature  $T \sim 293$  K, pressure  $P$  and relative humidity  $\sim 50$  % in the measuring volume, the correction for air density involves a temperature correction  $T/T_0$ , a pressure correction  $P_0/P$  and the dry-air humidity correction  $k_h = 0.9980$ . At the BIPM, the factor 1.0002 is also included to account for the compressibility of dry air between  $T \sim 293$  K and  $T_0 = 273.15$  K.

given in Burns (2004) and Burns *et al.* (2009). The changes made to the standard following the recommendations of ICRU Report 90 are given in Burns (2018). The GUM standard is described in Boutillon *et al.* (1996) and the changes made to certain correction factors described in Knyziak (2017). Changes made following the recommendations of ICRU Report 90 are reported in Knyziak (2019). The GUM standard was previously compared with the BIPM standard in an indirect comparison carried out in 2010, the results of which are reported in Burns *et al.* (2013). The main dimensions, the measuring volume and the polarizing voltage for each standard are shown in Table 2.

**Table 1. Physical constants used in the determination of the air-kerma rate**

| Constant                                | Value                     | $u_i$ <sup>a</sup> |
|---|---------------------------|--------------------|
| $\rho_{\text{air}}$ <sup>b</sup> (BIPM) | 1.2930 kg m <sup>-3</sup> | 0.0001             |
| $\rho_{\text{air}}$ <sup>c</sup> (GUM)  | 1.2045 kg m <sup>-3</sup> | 0.0001             |
| $W_{\text{air}} / e$                    | 33.97 J C <sup>-1</sup>   | 0.0035             |

<sup>a</sup>  $u_i$  is the relative standard uncertainty.

<sup>b</sup> Density of dry air at  $T_0 = 273.15$  K and  $P_0 = 101.325$  kPa.

<sup>c</sup> Density of dry air at  $T_0 = 293.15$  K and  $P_0 = 101.325$  kPa.

**Table 2. Main characteristics of the standards**

| Standard                           | BIPM M-01 | GUM    |
|------------------------------------|-----------|--------|
| Aperture diameter / mm             | 9.939     | 10.278 |
| Air path length / mm               | 281.5     | 393.3  |
| Collecting length / mm             | 60.004    | 99.88  |
| Electrode separation / mm          | 180       | 239.9  |
| Collector width / mm               | 200       | 280.5  |
| Measuring volume / mm <sup>3</sup> | 4655.4    | 8286.8 |
| Polarizing voltage / V             | 4000      | 4000   |

## 4. The transfer instruments

### 4.1 Determination of the calibration coefficient for a transfer instrument

The air-kerma calibration coefficient  $N_K$  for a transfer instrument is given by the relation

$$N_K = \frac{\dot{K}}{I_{\text{tr}}} \quad (2)$$

where  $\dot{K}$  is the air-kerma rate determined by the standard using Equation (1) and  $I_{\text{tr}}$  is the ionization current measured by the transfer instrument and the associated current-measuring system. The current  $I_{\text{tr}}$  is corrected to the standard conditions of air temperature, pressure and relative humidity chosen for the comparison ( $T = 293.15$  K,  $P = 101.325$  kPa,  $RH = 50$  %). No

humidity correction has been applied to the current measured using the transfer instruments, on the basis that the BIPM laboratory is maintained with a relative humidity in the range from 40 % to 55 % and the GUM laboratory in the range from 30 % to 60 %.

To derive a comparison result from the calibration coefficients  $N_{K,BIPM}$  and  $N_{K,NMI}$  measured, respectively, at the BIPM and at a national metrology institute (NMI), differences in the radiation qualities must be taken into account. Normally, each quality used for the comparison has the same nominal generating potential at each institute, but the half-value layers (HVLs) may differ. A radiation quality correction factor  $k_Q$  is derived for each comparison quality  $Q$ . This corrects the calibration coefficient  $N_{K,NMI}$  determined at the NMI into one that applies at the ‘equivalent’ BIPM quality and is derived by interpolation of the  $N_{K,NMI}$  values in terms of  $\log(\text{HVL})$ . The comparison result at each quality is then taken as

$$R_{K,NMI} = \frac{k_Q N_{K,NMI}}{N_{K,BIPM}} \quad (3)$$

In practice, the half-value layers normally differ by only a small amount and  $k_Q$  is close to unity.

#### 4.2 Details of the transfer instruments

Two thimble-type cavity ionization chambers belonging to the GUM, an NE 2561 and an NE 2571, were used as transfer instruments for the comparison. The same NE 2561 chamber was also used during the 2010 comparison. The main characteristics of the chambers are given in Table 3. Each chamber, without build-up cap, was positioned with the stem perpendicular to the beam direction and with the line or engraved text on the stem facing the source. The reference point for the NE 2561 chamber is located 5 mm from the thimble tip and that for the NE 2571 chamber 13 mm from the tip.

**Table 3. Main characteristics of the transfer chambers**

| Chamber type                     | NE 2561           | NE 2571           |
|----------------------------------|-------------------|-------------------|
| Serial number                    | 301               | 2676              |
| Geometry                         | thimble           | thimble           |
| External diameter / mm           | 8.35              | 7.0               |
| Wall material                    | graphite          | graphite          |
| Wall thickness / mm              | 0.50              | 0.36              |
| Nominal volume / cm <sup>3</sup> | 0.3               | 0.7               |
| Polarizing potential / V         | +200 <sup>a</sup> | +300 <sup>a</sup> |

<sup>a</sup> At both laboratories the potential is applied to the outer wall of the chamber.

## 5. Calibration at the BIPM

### 5.1 The BIPM irradiation facility and reference radiation qualities

The BIPM medium-energy x-ray laboratory houses a high-stability generator and a tungsten-anode x-ray tube with a 3 mm beryllium window. In addition to the aluminium filter of thickness 1.203 mm used for the 100 kV quality, an aluminium filter of thickness 2.228 mm is added for all radiation qualities to compensate for the decrease in filtration that occurred when the original BIPM x-ray tube (with an aluminium window of approximately 3 mm) was replaced in June 2004. Two voltage dividers monitor the tube voltage and a voltage-to-frequency converter combined with data transfer by optical fibre measures the anode current. No transmission monitor is used. For a given radiation quality, the standard uncertainty of the distribution of repeat air-kerma rate determinations over many months is typically 3 parts in  $10^4$ . The radiation qualities used in the range from 100 kV to 250 kV are those recommended by the CCRI (CCEMRI 1972) and are given in Table 4.

The irradiation area is temperature controlled at around 20 °C and is stable over the duration of a calibration to typically 0.2 °C. Two calibrated thermistors measure the temperature of the ambient air and the air inside the BIPM standard (which is controlled at 25 °C). Air pressure is measured by means of a calibrated barometer.

**Table 4. Characteristics of the BIPM reference radiation qualities**

| Radiation quality                                       | 100 kV | 135 kV | 180 kV | 250 kV |
|---|--------|--------|--------|--------|
| Generating potential / kV                               | 100    | 135    | 180    | 250    |
| Inherent Be filtration / mm                             | 3      | 3      | 3      | 3      |
| Additional Al filtration / mm                           | 3.431  | 2.228  | 2.228  | 2.228  |
| Additional Cu filtration / mm                           | -      | 0.232  | 0.485  | 1.570  |
| Al HVL / mm   | 4.030  | -      | -      | -      |
| Cu HVL / mm   | 0.149  | 0.489  | 0.977  | 2.484  |
| $(\mu/\rho)_{\text{air}}^a / \text{cm}^2 \text{g}^{-1}$ | 0.290  | 0.190  | 0.162  | 0.137  |
| $\dot{K}_{\text{BIPM}} / \text{mGy s}^{-1}$             | 0.50   | 0.50   | 0.50   | 0.50   |

<sup>a</sup> Measured at the BIPM using an evacuated tube of length 280 mm.

### 5.2 The BIPM standard and correction factors

The reference plane for the BIPM standard was positioned at 1200 mm from the radiation source, with a reproducibility of 0.03 mm. The standard was aligned laterally on the beam axis to an estimated uncertainty of 0.1 mm. The beam diameter in the reference plane is 98 mm for all radiation qualities.

During the calibration of the transfer chambers, measurements using the BIPM standard were made using positive polarity only. A correction factor of 1.00015 was applied to correct for the known polarity effect in the standard. The leakage current for the BIPM standard, relative to the ionization current, was measured to be around 1 part in  $10^4$ .

The correction factors applied to the ionization current measured at each radiation quality using the BIPM standard, together with their associated uncertainties, are given in Table 5. The factor  $k_a$  corrects for the attenuation of the x-ray fluence along the air path between the reference plane and the centre of the collecting volume. It is evaluated using the measured air-attenuation coefficients given in Table 4. In practice, the values used for  $k_a$  take account of the temperature and pressure of the air in the standard. Ionization current measurements (both for the standard and for transfer chambers) are also corrected for changes in air attenuation arising from variations in the temperature and pressure of the ambient air between the radiation source and the reference plane.

Two new correction factors,  $k_{ii}$  and  $k_W$ , are implemented following the recommendations of ICRU Report 90 (ICRU 2016) and presented as the product  $k_{ii}k_W$  by Burns (2018). Both correction factors are related to the mean energy expended in dry air per ion pair formed,  $W_{\text{air}}$ . The initial ionization correction factor  $k_{ii}$  accounts for the fact that the definition of  $W_{\text{air}}$  does not include the charge of the initial charged particle, while the correction factor  $k_W$  accounts for the rapid increase in the value of  $W_{\text{air}}$  at electron energies below around 10 keV.

**Table 5. Correction factors for the BIPM standard**

| Radiation quality                           | 100 kV | 135 kV | 180 kV | 250 kV | $u_{iA}$ | $u_{iB}$ |
|---|--------|--------|--------|--------|----------|----------|
| Air attenuation $k_a$ <sup>a</sup>          | 1.0099 | 1.0065 | 1.0055 | 1.0047 | 0.0002   | 0.0001   |
| Photon scatter $k_{sc}$                     | 0.9952 | 0.9959 | 0.9964 | 0.9974 | -        | 0.0003   |
| Fluorescence $k_{fl}$                       | 0.9985 | 0.9992 | 0.9994 | 0.9999 | -        | 0.0003   |
| Electron loss $k_e$                         | 1.0000 | 1.0015 | 1.0047 | 1.0085 | -        | 0.0005   |
| Initial ionization $k_{ii}$                 | 0.9980 | 0.9980 | 0.9981 | 0.9986 | -        | 0.0005   |
| Energy dependence of $W_{\text{air}}$ $k_W$ |        |        |        |        |          |          |
| Ion recombination $k_s$                     | 1.0010 | 1.0010 | 1.0010 | 1.0010 | 0.0002   | 0.0001   |
| Polarity $k_{pol}$                          | 1.0002 | 1.0002 | 1.0002 | 1.0002 | 0.0001   | -        |
| Field distortion $k_d$                      | 1.0000 | 1.0000 | 1.0000 | 1.0000 | -        | 0.0007   |
| Diaphragm correction $k_{dia}$              | 0.9995 | 0.9993 | 0.9991 | 0.9980 | -        | 0.0003   |
| Wall transmission $k_p$                     | 1.0000 | 1.0000 | 0.9999 | 0.9988 | 0.0001   | -        |
| Humidity $k_h$                              | 0.9980 | 0.9980 | 0.9980 | 0.9980 | -        | 0.0003   |
| $1 - g_{\text{air}}$                        | 0.9999 | 0.9999 | 0.9998 | 0.9997 | -        | 0.0001   |

<sup>a</sup> Values for the BIPM reference conditions of 293.15 K and 101.325 kPa; each measurement is corrected using the air temperature and pressure measured at the time.

### 5.3 Transfer chamber positioning and calibration at the BIPM

The reference point for each transfer chamber was positioned in the reference plane (1200 mm from the radiation source), with a reproducibility of 0.03 mm. Each chamber was aligned on the beam axis to an estimated uncertainty of 0.1 mm.

The leakage current was measured before and after each series of ionization current measurements and a correction made using the mean value. The relative leakage current was around 1 part in  $10^4$  for the NE 2571 and 4 parts in  $10^4$  for the NE 2561.

For each transfer chamber and at each radiation quality, two or more sets of seven measurements were made, each measurement with integration time 100 s for the NE 2561 and 60 s for the NE 2571. The relative standard uncertainty of the mean ionization current for each set was below 2 parts in  $10^4$ . Repeat calibrations were made for both chambers at several qualities (after repositioning). An uncertainty component of 3 parts in  $10^4$  is included in Table 11 for the short-term reproducibility of the calibration coefficients determined at the BIPM.

## 6. Calibration at the GUM

### 6.1 The GUM irradiation facility and reference radiation qualities

The medium-energy x-ray facility at the GUM is an YXLON MG-325 industrial unit with a tungsten-anode x-ray tube model Y.TU.320-D03 having an inherent filtration of 3 mm beryllium. The short-term stability of the generating potential is 1 part in  $10^4$ . No transmission monitor is used. The standard deviation of repeat air-kerma rate determinations over a period of many months is typically 1.5 parts in  $10^3$ . The characteristics of the GUM realization of the CCRI comparison qualities (CCEMRI 1972) are given in Table 6.

The irradiation area is temperature controlled at around 23 °C and is stable over the duration of a calibration to better than 0.05 °C. Two PT-401 thermometers are used to measure the temperature of the ambient air and the air inside the standard. The air pressure is measured by means of a calibrated Vaisala PTB-220 barometer.

**Table 6. Characteristics of the GUM reference radiation qualities**

| Radiation quality                                     | 100 kV | 135 kV | 180 kV | 250 kV |
|---|--------|--------|--------|--------|
| Generating potential / kV                             | 100    | 135    | 180    | 250    |
| Inherent Be filtration / mm                           | 3      | 3      | 3      | 3      |
| Additional Al filtration / mm                         | 3.402  | 2.919  | 2.919  | 2.919  |
| Additional Cu filtration / mm                         | -      | 0.199  | 0.464  | 1.563  |
| Al HVL / mm   | 4.040  | -      | -      | -      |
| Cu HVL / mm   | 0.154  | 0.478  | 0.985  | 2.467  |
| $(\mu/\rho)_{\text{air}} / \text{cm}^2 \text{g}^{-1}$ | 0.288  | 0.189  | 0.162  | 0.139  |
| $\dot{K}_{\text{GUM}} / \text{mGy s}^{-1}$            | 0.56   | 0.55   | 0.76   | 0.96   |

### 6.2 The GUM standard and correction factors

The reference plane for the GUM standard was positioned at 1000 mm from the radiation source, with a reproducibility of 0.1 mm. The standard was aligned laterally on the beam axis to an estimated uncertainty of 0.1 mm. The beam diameter in the reference plane is 80 mm for all radiation qualities.

During the calibration of the transfer chamber, measurements using the GUM standard were made at both polarities to correct for any polarity effect in the standard. The measured difference was typically 3 parts in  $10^4$ . The relative leakage current was below 3 parts in  $10^4$ .

The correction factors applied to the ionization current measured at each radiation quality using the GUM standard, together with their associated uncertainties, are given in Table 7. The correction factor  $k_a$  is evaluated using the measured air-attenuation coefficients given in Table 6. In practice, the values used for  $k_a$  take account of the temperature and pressure of the air in the standard at the time of measurements. As for the BIPM standard, two new correction factors,  $k_{ii}$  and  $k_W$ , are implemented as the product  $k_{ii}k_W$  (Knyziak 2019).

**Table 7. Correction factors for the GUM standard**

| Radiation quality                    | 100 kV | 135 kV | 180 kV | 250 kV | $u_{iA}$ | $u_{iB}$ |
|--------------------------------------|--------|--------|--------|--------|----------|----------|
| Air attenuation $k_a$ <sup>a</sup>   | 1.0137 | 1.0090 | 1.0077 | 1.0066 | 0.0003   | 0.0002   |
| Photon scatter $k_{sc}$              | 0.9921 | 0.9923 | 0.9950 | 0.9962 | -        | 0.0003   |
| Fluorescence $k_{fl}$                |        |        |        |        |          |          |
| Electron loss $k_e$                  | 1.0000 | 1.0002 | 1.0011 | 1.0034 | -        | 0.0005   |
| Initial ionization $k_{ii}$          | 0.9980 | 0.9980 | 0.9980 | 0.9984 | -        | 0.0005   |
| Energy dependence of $W_{air}$ $k_W$ |        |        |        |        |          |          |
| Ion recombination $k_s$              | 1.0012 | 1.0012 | 1.0013 | 1.0013 | 0.0002   | 0.0002   |
| Polarity $k_{pol}$                   | 0.9998 | 0.9999 | 0.9999 | 0.9999 | 0.0002   | 0.0002   |
| Field distortion $k_d$               | 1.0000 | 1.0000 | 1.0000 | 1.0000 | -        | 0.0005   |
| Aperture transmission $k_l$          | 0.9999 | 0.9999 | 0.9998 | 0.9997 | -        | 0.0003   |
| Wall transmission $k_p$              | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 0.0001   | -        |
| Humidity $k_h$                       | 0.9980 | 0.9980 | 0.9980 | 0.9980 | -        | 0.0003   |
| $1 - g_{air}$                        | 1.0000 | 1.0000 | 1.0000 | 1.0000 | -        | 0.0001   |

<sup>a</sup> Values for 293.15 K and 101.325 kPa; each measurement is corrected using the air density measured at the time.

### 6.3 Transfer chamber positioning and calibration at the GUM

The reference point for each transfer chamber was positioned at the reference distance (1000 mm from the radiation source), with a reproducibility of 0.1 mm. Alignment on the beam axis was to an estimated uncertainty of 0.1 mm.

The leakage current for each transfer chamber was measured before and after each series of ionization current measurements and a correction made using the mean value. The relative leakage current was typically 1 part in  $10^3$  for the NE 2561 chamber and 8 parts in  $10^4$  for the NE 2571 chamber.

The relative standard uncertainty of the mean of 5 series of 10 measurements at each radiation quality was typically 5 parts in  $10^4$  for the NE 2561 chamber and 3 parts in  $10^4$  for the NE 2571 chamber.

## 7. Additional considerations for transfer chambers calibrations

### 7.1 Ion recombination, polarity, radial non-uniformity and field size

As can be seen from Tables 4 and 6, the air-kerma rates at the GUM are up to a factor of two greater than those at the BIPM. However, for these thimble-type chambers the difference in volume recombination at the two laboratories is well below 1 part in  $10^4$ . Consequently, no corrections are applied for ion recombination. Each transfer chamber was used with the same polarity at each laboratory and so no corrections are applied for polarity effects in the transfer chambers.

No correction is applied at either laboratory for the radial non-uniformity of the radiation field. For small chambers with cavity dimensions below 2 cm, the effect should be small and will cancel to some extent at the two laboratories. A relative standard uncertainty of 3 parts in  $10^4$  is introduced in Table 12 for this effect. The radiation field size at the GUM, 80 mm in diameter, is smaller than the BIPM beam diameter of 98 mm. The effect of this on the transfer chamber calibrations was estimated by the GUM using Monte Carlo calculations to be at most 1 part in  $10^3$ . Consequently, a standard uncertainty of 1 part in  $10^3$  is included in Table 12 for this effect.

### 7.2 Radiation quality correction factors $k_Q$

As noted in Section 4.1, slight differences in radiation qualities might require a correction factor  $k_Q$ . From Tables 4 and 6 it is evident that the radiation qualities at the BIPM and at the GUM are reasonably matched in terms of the HVL in copper, except for the 100 kV quality. A set of correction factors  $k_Q$  was evaluated for each chamber from a fit to the results obtained at the BIPM; the results are included in Table 8 and are applied according to Equation (3). A standard uncertainty for these factors of 2 parts in  $10^4$  is included in Table 12.

## 8. Comparison results

The calibration coefficients  $N_{K,GUM}$  and  $N_{K,BIPM}$  for the transfer chambers are given in Table 8 and the comparison results  $R_{K,GUM}$  evaluated according to Equation (3) are presented in Table 9. For each quality, the final result in bold in Table 9 is evaluated as the unweighted mean for the two transfer chambers. The standard uncertainty  $u_{tr}$  arising from the difference in the results for the two chambers is also given. The root mean square value of  $u_{tr}$  for the four qualities  $u_{tr,comp} = 0.0016$  is included in Table 12.

Also given in Table 9 are the results of the previous comparison of the GUM and BIPM standards (Burns *et al.* 2013), revised for the changes made to both standards.

## 9. Uncertainties

The uncertainties associated with the primary standards are listed in Table 10 and those for the transfer chamber calibrations in Table 11. The combined standard uncertainty  $u_c$  for the comparison results  $R_{K,GUM}$  is presented in Table 12. The uncertainty  $u_c$  takes into account correlation in the type B uncertainties associated with the physical constants, the humidity correction and the product of the correction factors  $k_{ii}k_W$ . Correlation in the values for  $k_{sc}$ ,  $k_{fl}$  and  $k_e$  at the BIPM and at the GUM, derived from Monte Carlo calculations in each laboratory, are taken into account in an approximate way by assuming half of the uncertainty value for each factor at each laboratory. This is consistent with the analysis of the results of the BIPM comparisons in medium-energy x-rays in terms of degrees of equivalence described in Burns (2003).



**Table 8. Calibration coefficients for the transfer chambers**

| Radiation quality                               | 100 kV | 135 kV | 180 kV | 250 kV |
|---|--------|--------|--------|--------|
| <i>Transfer chamber NE 2561-301</i>             |        |        |        |        |
| $N_{K,GUM}$ (pre-comp) / Gy $\mu\text{C}^{-1}$  | 92.13  | 92.51  | 93.04  | 93.60  |
| $N_{K,GUM}$ (post-comp) / Gy $\mu\text{C}^{-1}$ | 92.21  | 92.52  | 93.21  | 93.74  |
| $N_{K,BIPM}$ / Gy $\mu\text{C}^{-1}$            | 91.29  | 92.12  | 92.66  | 93.36  |
| $k_Q$   | 0.9998 | 1.0003 | 0.9999 | 1.0001 |
| <i>Transfer chamber NE 2571-2676</i>            |        |        |        |        |
| $N_{K,GUM}$ (pre-comp) / Gy $\mu\text{C}^{-1}$  | 42.09  | 41.45  | 41.12  | 40.76  |
| $N_{K,GUM}$ (post-comp) / Gy $\mu\text{C}^{-1}$ | 42.15  | 41.52  | 41.14  | 40.82  |
| $N_{K,BIPM}$ / Gy $\mu\text{C}^{-1}$            | 41.96  | 41.39  | 41.04  | 40.71  |
| $k_Q$   | 1.0005 | 0.9995 | 1.0001 | 0.9999 |

**Table 9. Comparison results**

| Radiation quality                         | 100 kV        | 135 kV        | 180 kV        | 250 kV        |
|---|---------------|---------------|---------------|---------------|
| $R_{K,GUM}$ using NE 2561-301             | 1.0094        | 1.0046        | 1.0049        | 1.0034        |
| $R_{K,GUM}$ using NE 2571-2676            | 1.0043        | 1.0018        | 1.0023        | 1.0019        |
| Standard uncertainty $u_{tr}$             | 0.0026        | 0.0014        | 0.0013        | 0.0008        |
| <b>Final <math>R_{K,GUM}</math></b>       | <b>1.0069</b> | <b>1.0032</b> | <b>1.0036</b> | <b>1.0027</b> |
| <i>Revised results of 2010 comparison</i> | <i>1.0035</i> | <i>1.0036</i> | <i>1.0044</i> | <i>1.0046</i> |

## 10. Discussion

With the exception of the 100 kV radiation quality, the comparison results presented in Table 9 show the GUM and the BIPM standards to be in reasonable agreement at the level of the standard uncertainty of the comparison of 3.0 parts in  $10^3$ . The results for the three qualities are consistent and, in view of the uncertainty of 1.5 parts in  $10^3$  for reproducibility at the GUM as stated in Table 11, they are in agreement with those obtained during the 2010 comparison (corrected for changes to both standards in the interim period) as given in the final row of Table 9.

The high comparison result obtained at 100 kV arises from a very high value of  $N_{K,GUM}$  for the NE 2561 transfer chamber at this quality, both before and after the measurements at the BIPM. This is unlikely to be an issue with the chamber itself; the same chamber was used for the comparison in 2010 and the BIPM results  $N_{K,BIPM}$  given in Table 8 agree with those obtained in 2010 (corrected for the new factor  $k_{ij}k_W$ ) at the level of 5 parts in  $10^4$  for this quality (and even closer for the remaining qualities). Post-comparison investigations at the GUM found no clear

explanation, other than the possibility that a correction for the smaller field size at the GUM might reduce the 100 kV result for this chamber by around 1 part in  $10^3$ .

## 11. Degrees of Equivalence

The analysis of the results of BIPM comparisons in medium-energy x-rays in terms of degrees of equivalence is described in Burns (2003). Following a decision of the CCRI, the BIPM determination of the air-kerma rate is taken as the key comparison reference value, for each of the CCRI radiation qualities. It follows that for each laboratory  $i$  having a BIPM comparison result  $x_i$  with combined standard uncertainty  $u_i$ , the degree of equivalence with respect to the reference value is the relative difference  $D_i = (K_i - K_{\text{BIPM},i}) / K_{\text{BIPM},i} = x_i - 1$  and its expanded uncertainty  $U_i = 2 u_i$ . The results for  $D_i$  and  $U_i$ , expressed in mGy/Gy and including those of the present comparison, are shown in Table 13 and in Figure 1.

When required, the degree of equivalence between two laboratories  $i$  and  $j$  can be evaluated as the difference  $D_{ij} = D_i - D_j$  and its expanded uncertainty  $U_{ij} = 2u_{ij}$ , both expressed in mGy/Gy. In evaluating  $u_{ij}$ , account should be taken of correlation between  $u_i$  and  $u_j$  (Burns 2003).

**Table 10. Uncertainties associated with the standards**

| Standard                          | BIPM     |          | GUM      |          |
|-----------------------------------|----------|----------|----------|----------|
| Relative standard uncertainty     | $u_{iA}$ | $u_{iB}$ | $u_{iA}$ | $u_{iB}$ |
| Ionization current                | 0.0002   | 0.0002   | 0.0002   | 0.0002   |
| Positioning                       | 0.0001   | 0.0001   | 0.0001   | 0.0001   |
| Volume                            | 0.0001   | 0.0005   | 0.0001   | 0.0005   |
| Correction factors (excl. $k_h$ ) | 0.0003   | 0.0011   | 0.0004   | 0.0010   |
| Humidity $k_h$                    | -        | 0.0003   | -        | 0.0003   |
| Physical constants                | -        | 0.0035   | -        | 0.0035   |
| $\dot{K}$                         | 0.0004   | 0.0037   | 0.0005   | 0.0037   |

**Table 11. Uncertainties associated with the calibration of the transfer chambers**

| Laboratory                      | BIPM     |          | GUM      |          |
|---------------------------------|----------|----------|----------|----------|
| Relative standard uncertainty   | $u_{iA}$ | $u_{iB}$ | $u_{iA}$ | $u_{iB}$ |
| $\dot{K}$                       | 0.0004   | 0.0037   | 0.0005   | 0.0037   |
| $I_{\text{tr}}$                 | 0.0002   | 0.0002   | 0.0005   | 0.0002   |
| Positioning of transfer chamber | 0.0001   | -        | 0.0001   | 0.0001   |
| Reproducibility                 | 0.0003   | -        | 0.0015   | -        |
| $N_{K,\text{lab}}$              | 0.0005   | 0.0037   | 0.0017   | 0.0037   |

## 12. Conclusions

The key comparison BIPM.RI(I)-K3 for the determination of air kerma in medium-energy x-rays shows the standards of the GUM and the BIPM to be in agreement at the level of the expanded uncertainty of the comparison of 6.0 parts in  $10^3$ .

Tables and graphs of degrees of equivalence, including those for the GUM, are presented for entry in the BIPM key comparison database. Note that the data presented in the tables, while correct at the time of publication of the present report, become out of date as laboratories make new comparisons with the BIPM. The formal results under the CIPM MRA are those available in the BIPM key comparison database (KCDB 2021).

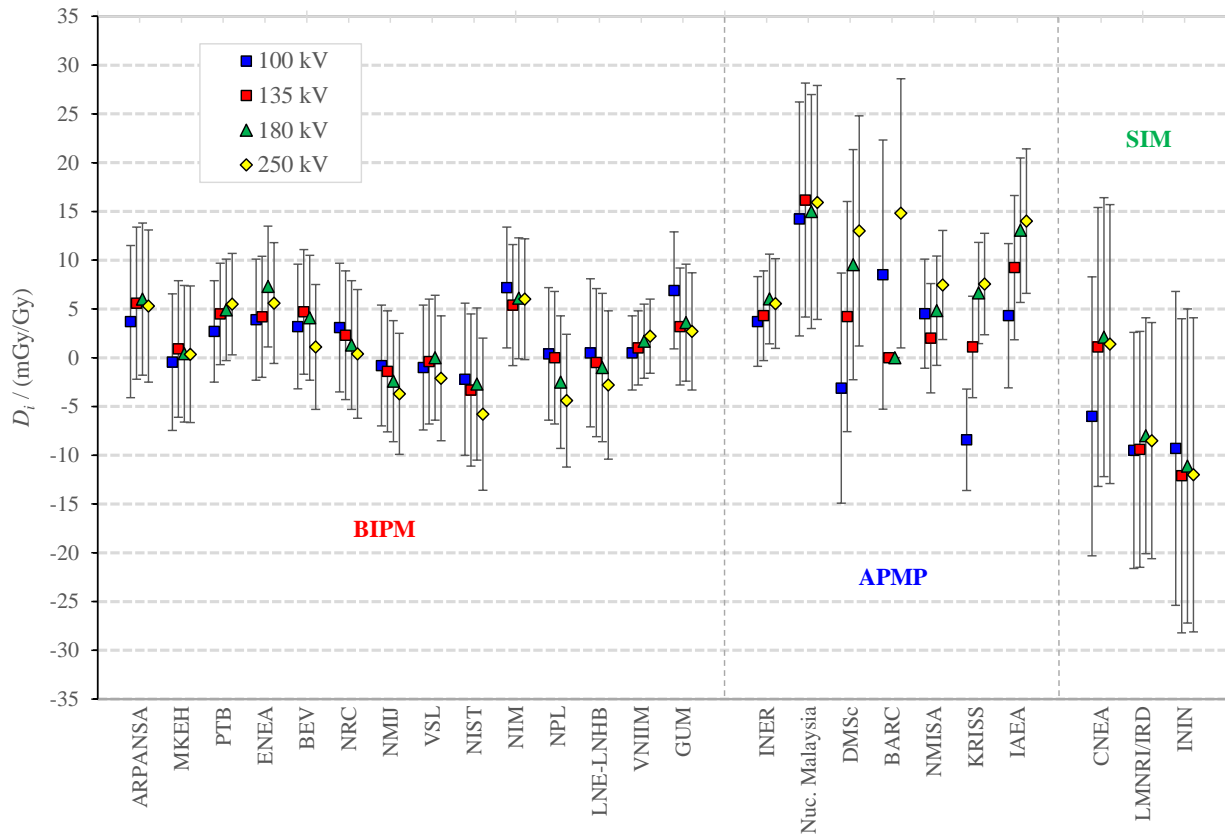
**Table 12. Uncertainties associated with the comparison results**

| Relative standard uncertainty                     | $u_{iA}$       | $u_{iB}$            |
|---|----------------|---------------------|
| $N_{K,GUM} / N_{K,BIPM}$                          | 0.0017         | 0.0015 <sup>a</sup> |
| Beam non-uniformity                               | -              | 0.0003              |
| Field size  | -              | 0.0010              |
| $k_Q$   | -              | 0.0002              |
| Agreement between transfer chambers $u_{tr,comp}$ | 0.0016         | -                   |
| $R_{K,GUM}$                                       | 0.0023         | 0.0018              |
|   | $u_c = 0.0030$ |                     |

<sup>a</sup> Takes account of correlation in type B uncertainties.

Table 13. Degrees of equivalence. For each laboratory  $i$ , the degree of equivalence with respect to the key comparison reference value is the difference  $D_i$  and its expanded uncertainty  $U_i$ . Tables formatted as they appear in the BIPM key comparison database; **red** indicates participation in BIPM.RI(I)-K3, **blue** in APMP.RI(I)-K3 and **green** in SIM.RI(I)-K3.

|                      | 100 kV             |       | 135 kV             |       | 180 kV             |       | 250 kV             |       |
|----------------------|--------------------|-------|--------------------|-------|--------------------|-------|--------------------|-------|
| Lab $i$              | $D_i$<br>/(mGy/Gy) | $U_i$ | $D_i$<br>/(mGy/Gy) | $U_i$ | $D_i$<br>/(mGy/Gy) | $U_i$ | $D_i$<br>/(mGy/Gy) | $U_i$ |
| <b>ARPANSA</b>       | 3.7                | 7.8   | 5.6                | 7.8   | 6.0                | 7.8   | 5.3                | 7.8   |
| <b>MKEH</b>          | -0.4               | 7.0   | 0.9                | 7.0   | 0.4                | 7.0   | 0.4                | 7.0   |
| <b>PTB</b>           | 2.7                | 5.2   | 4.5                | 5.2   | 4.9                | 5.2   | 5.5                | 5.2   |
| <b>ENEA</b>          | 3.9                | 6.2   | 4.2                | 6.2   | 7.3                | 6.2   | 5.6                | 6.2   |
| <b>BEV</b>           | 3.2                | 6.4   | 4.7                | 6.4   | 4.1                | 6.4   | 1.1                | 6.4   |
| <b>NRC</b>           | 3.1                | 6.6   | 2.3                | 6.6   | 1.3                | 6.6   | 0.4                | 6.6   |
| <b>NMIJ</b>          | -0.8               | 6.2   | -1.4               | 6.2   | -2.4               | 6.2   | -3.7               | 6.2   |
| <b>VSL</b>           | -1.0               | 6.4   | -0.4               | 6.4   | 0.0                | 6.4   | -2.1               | 6.4   |
| <b>NIST</b>          | -2.2               | 7.8   | -3.3               | 7.8   | -2.7               | 7.8   | -5.8               | 7.8   |
| <b>NIM</b>           | 7.2                | 6.2   | 5.4                | 6.2   | 6.1                | 6.2   | 6.0                | 6.2   |
| <b>NPL</b>           | 0.4                | 6.8   | 0.0                | 6.8   | -2.5               | 6.8   | -4.4               | 6.8   |
| <b>LNE-LNHB</b>      | 0.5                | 7.6   | -0.5               | 7.6   | -1.0               | 7.6   | -2.8               | 7.6   |
| <b>VNIIM</b>         | 0.5                | 3.8   | 1.0                | 3.8   | 1.7                | 3.8   | 2.2                | 3.8   |
| <b>GUM</b>           | 6.9                | 6.0   | 3.2                | 6.0   | 3.6                | 6.0   | 2.7                | 6.0   |
| <b>INER</b>          | 3.7                | 4.6   | 4.3                | 4.6   | 6.0                | 4.6   | 5.5                | 4.6   |
| <b>Nuc. Malaysia</b> | 14.2               | 12.0  | 16.2               | 12.0  | 15.0               | 12.0  | 15.9               | 12.0  |
| <b>DMSc</b>          | -3.1               | 11.8  | 4.2                | 11.8  | 9.6                | 11.8  | 13.0               | 11.8  |
| <b>BARC</b>          | 8.5                | 13.8  |                    |       |                    |       | 14.8               | 13.8  |
| <b>NMISA</b>         | 4.5                | 5.6   | 2.0                | 5.6   | 4.8                | 5.6   | 7.5                | 5.6   |
| <b>KRISS</b>         | -8.4               | 5.2   | 1.1                | 5.2   | 6.6                | 5.2   | 7.6                | 5.2   |
| <b>IAEA</b>          | 4.3                | 7.4   | 9.2                | 7.4   | 13.1               | 7.4   | 14.0               | 7.4   |
| <b>CNEA</b>          | -6.0               | 14.3  | 1.1                | 14.3  | 2.1                | 14.3  | 1.4                | 14.3  |
| <b>LMNRI/IRD</b>     | -9.5               | 12.1  | -9.4               | 12.1  | -8.0               | 12.1  | -8.5               | 12.1  |
| <b>ININ</b>          | -9.3               | 16.1  | -12.1              | 16.1  | -11.1              | 16.1  | -12.0              | 16.1  |



**Figure 1.** Degrees of equivalence for each laboratory  $i$  with respect to the key comparison reference value. Results to the left are for the ongoing international comparison **BIPM.RI(I)-K3**, those in the middle section for the regional comparison **APMP.RI(I)-K3** and those to the right for the regional comparison **SIM.RI(I)-K3**.

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