Measuring the electron and positron magnetic moments to test the Standard Model's most precise prediction

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S. Fogwell Hoogerheide, J. C. Dorr, E. Novitski, and G. Gabrielse. "High efficiency positron accumulation for high-precision magnetic moment experiments." *Rev. Sci. Instrum*. 86, 053301 (2015)

Positrons trapped Expected precision e+ and e- improvement

- Design for better B field stability
- Cavity assisted sideband cooling
- Correlated measurement



Introduction to precision e⁺/e⁻ magnetic dipole moment measurements

$$\vec{\mu} = \mp \frac{g}{2} \mu_B \frac{\vec{S}}{\hbar/2} \qquad \qquad \mu_B = \frac{e\hbar}{2m}$$

- g/2 = 1/2 Classical particle with equal charge/mass distribution
- g/2 = 1 Dirac point particle

 $g/2 = 1.001 159 \dots$ Dirac point particle plus Standard Model vacuum

$$\frac{g}{2}(electron) = \frac{\mu}{\mu_B}(electron) = 1.001\ 159\ 652\ 180\ 73\ (28)\ [.28\ ppt]$$

D. Hanneke, S. Fogwell, and G. Gabrielse, Phys. Rev. Lett. 100, 120801 (2008)

Electron magnetic moment is the most precisely measured fundamental property of an elementary particle!

One motivation: testing the Standard Model by testing CPT symmetry

- Charge Conjugation: $e^- \rightarrow e^+$
- **P**arity Transformation:
- Time Reversal: $t \rightarrow -t$
- CPT Theorem: CPT is an exact symmetry for any local, Lorentz invariant quantum field theory (which includes the Standard Model)

G. Lüders, Ann. Phys. 2, 1 (1957)

 $\vec{x} \rightarrow -\vec{x}$

• CPT symmetry violation indicates beyond-the-Standard-Model physics

Positron/electron g comparison is best test of CPT symmetry in a lepton system

Standard Model predicts e+, e- magnetic moments should be same magnitude.

$$\frac{g}{2}(electron) = 1.001\ 159\ 652\ 180\ 73\ (28)\ [.28\ ppt]$$

 $\frac{g}{2}(positron) = 1.001\ 159\ 652\ 1879\ (4.3)\ [4.3\ ppt]$

(-)

D. Hanneke, S. Fogwell, and G. Gabrielse, *Phys. Rev. Lett.* **100**, 120801 (2008)

R. S. Van Dyck, Jr., P. B. Schwinberg, and H. G. Dehmelt, *Phys. Rev. Lett.* **59**. 26 (1987)

Best measurement of positron *g*-value is only <u>4.3 ppt</u>.

$$\frac{g(e^{-})}{g(e^{+})} = 1 + (0.5 \pm 2.1) \times 10^{-12}$$
Can be improved by 15x with positron measurement at current electron precision level!

Solution: new and improved apparatus with positron loading capability is built and trapping positrons!

Standard Model predicts g from α



Standard Model test requires an independent α

 $\frac{g}{2} = \frac{\mu}{\mu_B} = 1 + C_2 \left(\frac{\alpha}{\pi}\right) + C_4 \left(\frac{\alpha}{\pi}\right)^2 + C_6 \left(\frac{\alpha}{\pi}\right)^3 + C_8 \left(\frac{\alpha}{\pi}\right)^4 + C_{10} \left(\frac{\alpha}{\pi}\right)^5 + a_{\mu,\tau} + a_{hadronic} + a_{weak}$



Comparing our g to g from independent α tests Standard Model's most precise prediction

$$\frac{\mathscr{G}}{2} = \frac{\mu}{\mu_{B}} = 1 + C_{2} \left(\frac{\alpha}{\pi}\right) + C_{4} \left(\frac{\alpha}{\pi}\right)^{2} + C_{6} \left(\frac{\alpha}{\pi}\right)^{3} + C_{8} \left(\frac{\alpha}{\pi}\right)^{4} + C_{10} \left(\frac{\alpha}{\pi}\right)^{5} + a_{\mu,\tau} + a_{hadronic} + a_{weak}$$

Predicted:
$$\frac{g}{2} = 1.001\ 159\ 652\ 181\ 64\ (76)$$
- R. Bouchendira, P. Cladé, S. Guellati-Khélifa, F. Nez,
and F. Biraben, Phys. Rev. Lett. **106**, 080801 (2011).
- T. Aoyama, M. Hayakawa, T. Kinoshita, and M. Nio,
arXiv:1412.8284v2 (2015).Measured: $\frac{g}{2} = 1.001\ 159\ 652\ 180\ 73\ (28)$ - D. Hanneke, S. Fogwell, and G. Gabrielse, Phys. Rev.
Lett. **100**, 120801 (2008).

Sets a bound on electron substructure or new physics beyond the standard model

Standard Model gives the most accurate fine structure constant from g ~ 1

$$\frac{g}{2} = \frac{\mu}{\mu_{B}} = 1 + C_{2} \left(\frac{\alpha}{\pi}\right)^{2} + C_{4} \left(\frac{\alpha}{\pi}\right)^{2} + C_{6} \left(\frac{\alpha}{\pi}\right)^{3} + C_{8} \left(\frac{\alpha}{\pi}\right)^{4} + C_{10} \left(\frac{\alpha}{\pi}\right)^{3} + A_{\mu,\tau} + A_{hadronic} + A_{weak}$$

Calculated analytically Calculated numerically

 $\alpha^{-1} = 137.035\ 999\ 157\ (33)(4)\ [0.24\ ppb,\ exp.][0.03\ ppb,\ th.]$

= 137.035 999 157 (33) [0.24 ppb]

Sources of uncertainty in α determination from g



Experimental determination of g/2 now the primary source of uncertainty \rightarrow improved g/2 = improved α

9 D. Hanneke, S. Fogwell, and G. Gabrielse, Phys. Rev. Lett. 100, 120801 (2008) T. Aoyama, M. Hayakawa, T. Kinoshita, and M. Nio, , Phys. Rev. D 91, 033006 (2015)

Measuring g as a frequency ratio

• g in free space (in a magnetic field):



Spin frequency:

$$v_s = v_c \frac{g}{2}$$



Nice experimental feature: the magnetic field cancels out



$g/2 = 1.001 \ 159 \ 652 \ 180 \ 73...$

Dirac point particle plus Standard Model vacuum

Measuring g-2 as a frequency ratio

• g in free space (in a magnetic field):

Define anomaly frequency:



Louisell, W. H., Pidd, R. W., & Crane, H. R., *Physical Review*, *94*(1), 7 (1954). D. Hanneke, S. Fogwell, and G. Gabrielse, *Phys. Rev. Lett.* **100**, 120801 (2008)

g in a Penning trap



Brown-Gabrielse invariance theorem

Special relativistic shift requires knowledge of exact cyclotron/spin state

Special relativistic shift to cyclotron frequency matters at our precision level:

$$\Delta v_c = -\delta(n = 1 + m_s)$$
$$\frac{\delta}{v_c} = \frac{hv_c}{mc^2} \approx 10^{-9}$$

Solution: drive exactly the same transition every time

- 6 T magnetic field to give ~7 K cyclotron level spacing
- Dilution refrigerator with T=100 mK to stay in ground state
- Excite and detect single cyclotron or anomaly transitions
- Special relativistic shift can be calculated from measured frequencies





The new apparatus



S. Fogwell Hoogerheide, J. C. Dorr, E. Novitski, and G. Gabrielse. Rev. Sci. Instrum. 86, 053301 (2015)

The new apparatus



S. Fogwell Hoogerheide, J. C. Dorr, E. Novitski, and G. Gabrielse. Rev. Sci. Instrum. 86, 053301 (2015)

¹⁵



Ingredients of a g/2 measurement

$$\frac{g}{2} = \frac{v_s}{v_c} = 1 + \frac{v_s - v_c}{v_c}$$

 $=1+\frac{v_{a}}{2}$

- Measure cyclotron frequency
- Measure anomaly frequency



Ingredients of a g/2 measurement



- Measure cyclotron frequency
- Measure anomaly frequency
- Measure axial frequency (less precision needed)
- Calculate special relativistic shift (δ)
- Calculate $\Delta \omega / \omega$ from measured cavity mode couplings



Cyclotron/anomaly lineshapes dominate uncertainty



g/2 = 1.001 159 652 180 73 (28) [0.28 ppt]

Uncertainties for g in parts-per-trillion.

| Total | 0.73 | 0.30 | 0.34 | 0.53 |
|-----------------|-------|-------|-------|-------|
| lineshape model | | | | |
| Correlated | 0.24 | 0.24 | 0.24 | 0.24 |
| lineshape model | | | | |
| Uncorrelated | 0.56 | 0.00 | 0.15 | 0.30 |
| Cavity shift | 0.13 | 0.06 | 0.07 | 0.28 |
| Statistics | 0.39 | 0.17 | 0.17 | 0.24 |
| v_{c} / GHz = | 147.5 | 149.2 | 150.3 | 151.3 |

Cyclotron/anomaly lineshapes dominate uncertainty

Excitation fractions vs. frequency



[•] Blurring could be caused by B-field noise or instability, e.g. from trap electrodes moving with respect to magnet

• Lineshape blurring limits linesplitting to about 1 part in 10

 Better design and new methods possible in new apparatus should yield cleaner, narrower cyclotron and anomaly lines

D. Hanneke, S. Fogwell, and G. Gabrielse, Phys. Rev Lett. **100**, 120801 (2008) S. Fogwell Hoogerheide, J. C. Dorr, E. Novitski, and G. Gabrielse. *Rev. Sci. Instrum.* 86, 053301 (2015)

Part of the solution: new apparatus is designed to be extremely stable



Improvements to reduce possible sources of lineshape blurring include:

- Better mechanical support structure and alignment reduces susceptibility to vibration-induced noise
- Very low magnetic field drift
- Better magnetic field shielding (self-shielding solenoid)
- Improved helium hold time
- More fridge cooling power for stabler temperature
- More room for electronics– positron loading trap

With stability come practical challenges



• Need to lower warm apparatus straight into a liquid helium dewar without quenching the magnet

- 4-5 hour cooling time
- Sliding seal plus glove bag to avoid paramagnetic oxygen ice



With stability come practical challenges



• Need to lower warm apparatus straight into a liquid helium Dewar without quenching the magnet

- 4-5 hour cooling time
- Sliding seal plus glove bag to avoid paramagnetic oxygen ice
- Helium for new large Dewar is expensive, so need efficient recovery
 - Added helium reliquifier

With stability come practical challenges



S. Fogwell Hoogerheide, J. C. Dorr, E. Novitski, and G. Gabrielse. Rev. Sci. Instrum. 86, 053301 (2015)

Besides improving magnetic field stability, what can we do?



• More details about linewidth and detection...



• Don't detect single 150 GHz photon from single cyclotron jump

 Instead, couple to 200
 MHz axial motion and detect that

<sup>D. Hanneke, S. Fogwell, and G. Gabrielse, Phys. Rev Lett. 100, 120801 (2008)
S. Fogwell Hoogerheide, J. C. Dorr, E. Novitski, and G. Gabrielse.</sup> *Rev. Sci. Instrum.* 86, 053301 (2015)

Detection of single-particle axial motion



• Axial motion is driven to increase signal



The single-particle self-excited oscillator

- Need large stable signal to quickly read axial frequency without ambiguity
- Set feedback gain to exactly cancel damping from amp
- Adjust the gain in real time to maintain a stable amplitude

$$m\left(\ddot{z} + (1 - G)\gamma_z \dot{z} + \omega_z^2 z\right) = 0$$
SEO signal from a single electron in the new apparatus
$$\int_{-300}^{0.004} 0.002 \int_{-100}^{0.004} 0.002 \int_{-100}^{0.0$$

frequency-201,178,017 (Hz)

Signal

Out

G

φ

Spin and cyclotron state detection via coupling to axial motion

Axial motion:



Change in cyclotron or spin state causes measurable shift in axial frequency:

$$\frac{\Delta v_z}{v_z} \approx 7 \times 10^{-9} \left(n + \frac{1}{2} + \frac{g}{2}m_s\right)$$

Spin and cyclotron state detection via coupling to axial motion



Spin and cyclotron state detection via coupling to axial motion



But this coupling to axial motion broadens cyclotron and anomaly lines



Shifts to axial frequency in old and new traps



New apparatus: smaller magnetic bottle → reduced coupling strength → expected narrower lines

L. S. Brown and G. Gabrielse, Rev. Mod. Phys. **58**, 233 (1986) B. D'Urso *et al.*, Phys. Rev. Lett. **94**, 113002 (2005) D. Hanneke, S. Fogwell, and G. Gabrielse, Phys. Rev Lett. **100**, 120801 (2008. S. Fogwell Hoogerheide, J. C. Dorr, E. Novitski, and G. Gabrielse. *Rev. Sci. Instrum.* **86**, 053301 (2015) ³¹

New technique for defeating magnetic field drifts: Correlated Measurement

2008 Protocol

 Cyclotron attempts followed by anomaly attempts



 Combine data, adjust for field drift, fit both lines to extract g/2



New Protocol

• Apply cyclotron and anomaly drives simultaneously



 Generate 2-D correlated lineshape, extract g/2



Advantages of the Correlated Measurement protocol

- Eliminates magnetic field drifts between a given anomaly and cyclotron data point
- In low-axial-damping limit, system stays in single axial state during a measurement, creating discrete peaks
- Combined with cooling to axial ground state, successive attempts see same very small range of fields from magnetic bottle distortion, which makes for very narrow lines





L. S. Brown and G. Gabrielse, Rev. Mod. Phys. **58**, 233 (1986) B. D'Urso, Ph.D. thesis, Harvard University (2003) $\frac{g}{2} = 1 + \frac{v_{a}}{v_{c}} \qquad n_{c} = 1 \qquad hv_{a} \qquad hv_{c} \qquad n_{c} = 0 \qquad hv_{c} \qquad$

Excitation probability for drive frequency pairs



cyclotron frequency detuning ³³

Technical challenges of the Correlated Measurement protocol

- Lower transition success rate, so statistics could be an issue
 - Both cyclotron and anomaly drive attempts must be successful to get an excitation
 - Much narrower lines, and must still know Bfield well enough to drive transitions
- Need to be in low axial damping limit to see discrete quantum states, so must develop a method of decoupling particle from amplifier. Development of cryogenic low-loss high-B-field-tolerant RF switch is ongoing
- For maximum benefit, need to cool to axial ground state with cavity-assisted axial sideband cooling

Next technique in development!



Axial-cyclotron sideband cooling

Want to reduce axial state to reduce spread of magnetic fields particle sees during an axial oscillation:



- Decouple axial motion from amp => no thermalization to 100 mK
- Apply a drive at $\overline{\omega}_{c} \overline{\omega}_{z}$ to drive sideband transition that decreases axial state and increases cyclotron state
- Cyclotron decays via synchrotron radiation
- Cooling limit: $T_z = \frac{\omega_z}{\omega_c'} T_c \approx 1 \times 10^{-4} K$
 - Good enough to get to axial ground state for correlated measurement

L. S. Brown, G. Gabrielse, K. Helmerson, and J. Tan, Phys. Rev. Lett. **51**, 44-47 (1985) D. Hanneke, S. Fogwell, and G. Gabrielse, Phys. Rev Lett. **100**, 120801 (2008) Compare: axial state spacing is about 10 mK



Penning trap as microwave cavity

- Walls of the cylindrical electrodes form a resonant microwave cavity near electron's cyclotron frequency
- Changing B field changes cyclotron frequency, brings particle into and out of resonance with modes
- Particle's interaction with mode fields affects cyclotron lifetime, cyclotron frequency, and our ability to couple microwaves into cavity



• Double-edged sword



cyclotron frequency / GHz

L. S. Brown, G. Gabrielse, K. Helmerson, and J. Tan, Phys. Rev. Lett. **51**, 44-47 (1985) D. Hanneke, S. Fogwell, and G. Gabrielse, Phys. Rev Lett. **100**, 120801 (2008)

Cavity inhibits spontaneous emission

- Free space cyclotron lifetime is 89 msec • Lifetime in cavity can be as high at 16 sec far from from strong cyclotron coupling modes cyclotron frequency / GHz • Inhibited by factor of 180! 140 138 142 144 146 148 150 152 154 TM₁₁₇ TM₁₄₁ (TE₁₁₇ TE₁₂₇ TM₁₃₅ TM₁₂₇ TM₁₄₃ TE₁₃₆ 40 Need some inhibition to have time to average self-٠ excited oscillator to detect axial frequency shifts that
 - 40 d_{a}^{0} 30 d_{a}^{0} 20 h_{a}^{0} 20 h_{a}^{0} 5 10 15 20 25 30 time / s

indicate transitions

Strong coupling modes affect cyclotron frequency as well as lifetime



Cavity shifts do not limit g-2 uncertainty at current level



Uncertainties for 2008 g in parts-per-trillion.

| v _c / GHz = | 147.5 | 149.2 | 150.3 | 151.3 |
|-------------------------------|-------|-------|-------|-------|
| Statistics | 0.39 | 0.17 | 0.17 | 0.24 |
| Cavity shift | 0.13 | 0.06 | 0.07 | 0.28 |
| Uncorrelated lineshape model | 0.56 | 0.00 | 0.15 | 0.30 |
| Correlated lineshape model | 0.24 | 0.24 | 0.24 | 0.24 |
| Total | 0.73 | 0.30 | 0.34 | 0.53 |

Cavity shifts no longer limit g-2 uncertainty



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But other cavity modes can also actively help us cool axial motion!

Cavity assistance in axial sideband cooling



- Need to drive on a "cooling mode" with correct geometry for these sideband transitions:
 - E field like $z\hat{\rho}$ or $\rho\hat{z}$
- If far from cooling mode, almost all microwave power is reflected
- On cooling mode, good power transmission and order-x10 geometrical enhancement of E field
- But also need to stay away from strong coupling modes that shift g factors and reduce cyclotron lifetime!



Transverse E-field on cross sections of a cooling mode in the trap



Cavity mode structure of the 2008 trap prevented cavity-assisted axial sideband cooling

• 2008 trap: all cooling modes were too close to strong cyclotron coupling modes, so none could be used at g-measurement locations



Cavity mode structure of the new trap will enable cavity-assisted axial sideband cooling

•2008 trap: all cooling modes were too close to strong cyclotron coupling modes, so none could be used at g-measurement locations Relative frequencies of modes depend of trap geometry



Cavity mode structure of the new trap will enable cavity-assisted axial sideband cooling



Another frontier: better statistics

- Rate-limiting step: wait several lifetimes for cyclotron decay after anomaly transition attempt (or correlated transition attempt)
- To speed this step, sweep down with adiabatic fast passage or π-pulse

D. Hanneke, S. Fogwell, and G. Gabrielse, Phys. Rev Lett. 100, 120801 (2008)D. Hanneke, S. Fogwell Hoogerheide, and G. Gabrielse, Phys Rev A 83, 052122 (2011)

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Uncertainties for g in parts-per-trillion.

Positron loading mechanism

- Positrons come from beta decay of ²²Na
- Positrons pass through single crystal tungsten moderator → form loosely bound positronium
- Electric field in trap strips away electron and leaves positron trapped



Positron loading demonstrated in new apparatus with small retractable source



 Method was developed for accumulating millions of positrons with large ~ mCi radioactive sources (a safety headache)

• Relatively tiny 6.5 uCi source requires no shielding

- Source is retractable to preserve pristine environment for measurement
 - Required wider dilution refrigerator
 - Design challenges at 100 mK: 0.8 mm hole from 300 K to 100 mK would cause 200 uW of heating

Additional Penning trap to catch positrons from source



Positron loading demonstrated in new apparatus with small retractable source



Driven axial response from trapped positrons in loading trap

 Demonstrated higher positron loading rate than 1987 UW positron measurement with 75x smaller source (6.5 μC)

• Next step: pulsed transfer to precision trap

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S. Fogwell Hoogerheide, J. C. Dorr, E. Novitski, and G. Gabrielse. Rev. Sci. Instrum. 86, 053301 (2015)

Status and outlook

Improvements that have already been implemented

 New apparatus with positrons, improved stability, smaller magnetic bottle, better cavity mode structure, and more... Driven axial response from trapped positrons



Remaining basic preparation

- Transfer positrons from loading trap into precision trap to prepare for positron measurement
- Characterize apparatus (cavity mode structure, systematic checks, etc)



New techniques in development

- Cavity-assisted axial sideband cooling
- Correlated measurement



Status and outlook

Improvements that have already been implemented

New apparatus to enable improved tests of the Standard Model via new measurements of positron and electron g-2 at greater precision than the 2008 electron measurement

Remaining basic preparation

- Transfer positrons from loading trap into precision trap to prepare for positron measurement
- Characterize apparatus (cavity mode structure, systematic checks, etc)



New techniques in development

- Cavity-assisted axial sideband cooling
- Correlated measurement



requercy - vz (KHZ)

Thank you