

# DEVELOPMENT OF TWSTFT CARRIER PHASE TECHNIQUE IN LNE-SYRTE

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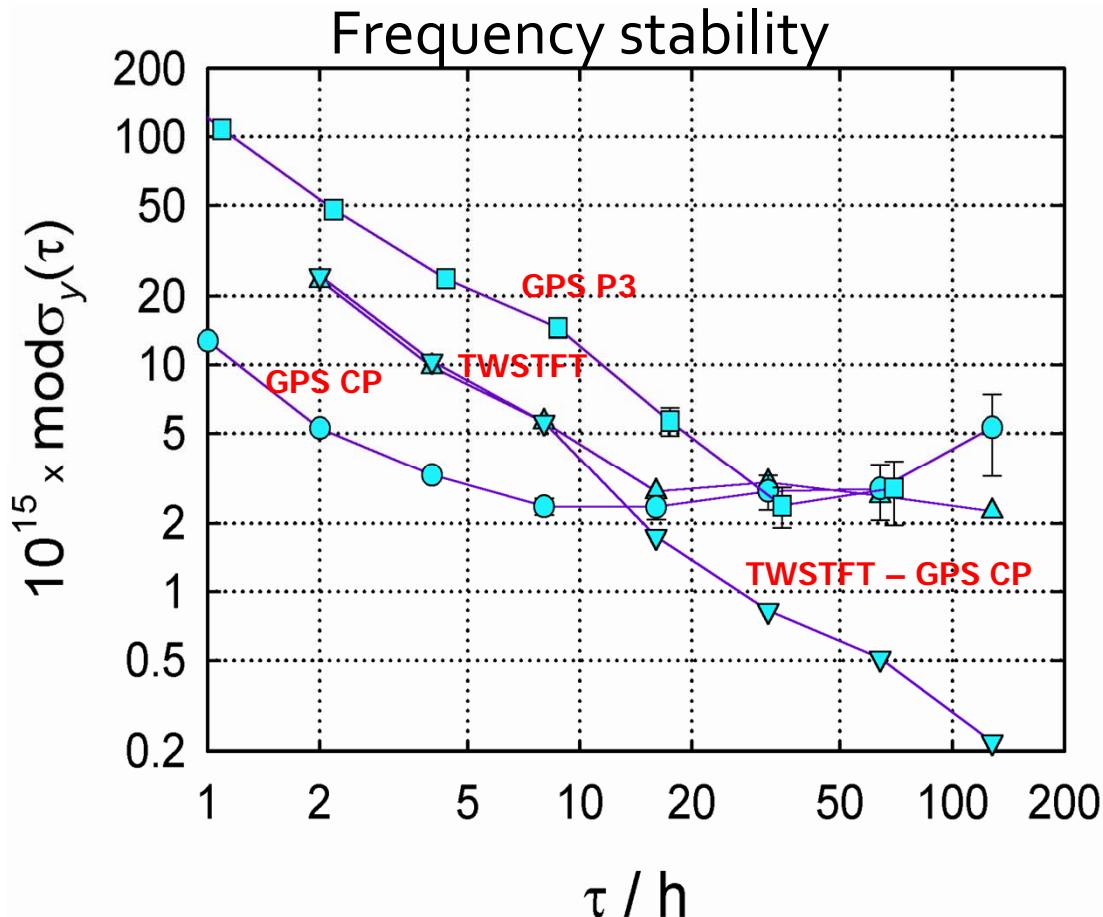
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# Outline

- Introduction and motivation
- Principle of TWSTFT carrier phase technique
- TWSTFT equation system
- Experimental validation of the system set-up
- Understanding the satellite LO frequency distortion
- Characterization of the TWCP link (stability)
- Conclusion and outlooks

# Introduction and motivation



Results obtained with 2.5 Mchips/s, OP-NPL link  
(Bauch et al., Metrologia **43** (2006) 109-120).

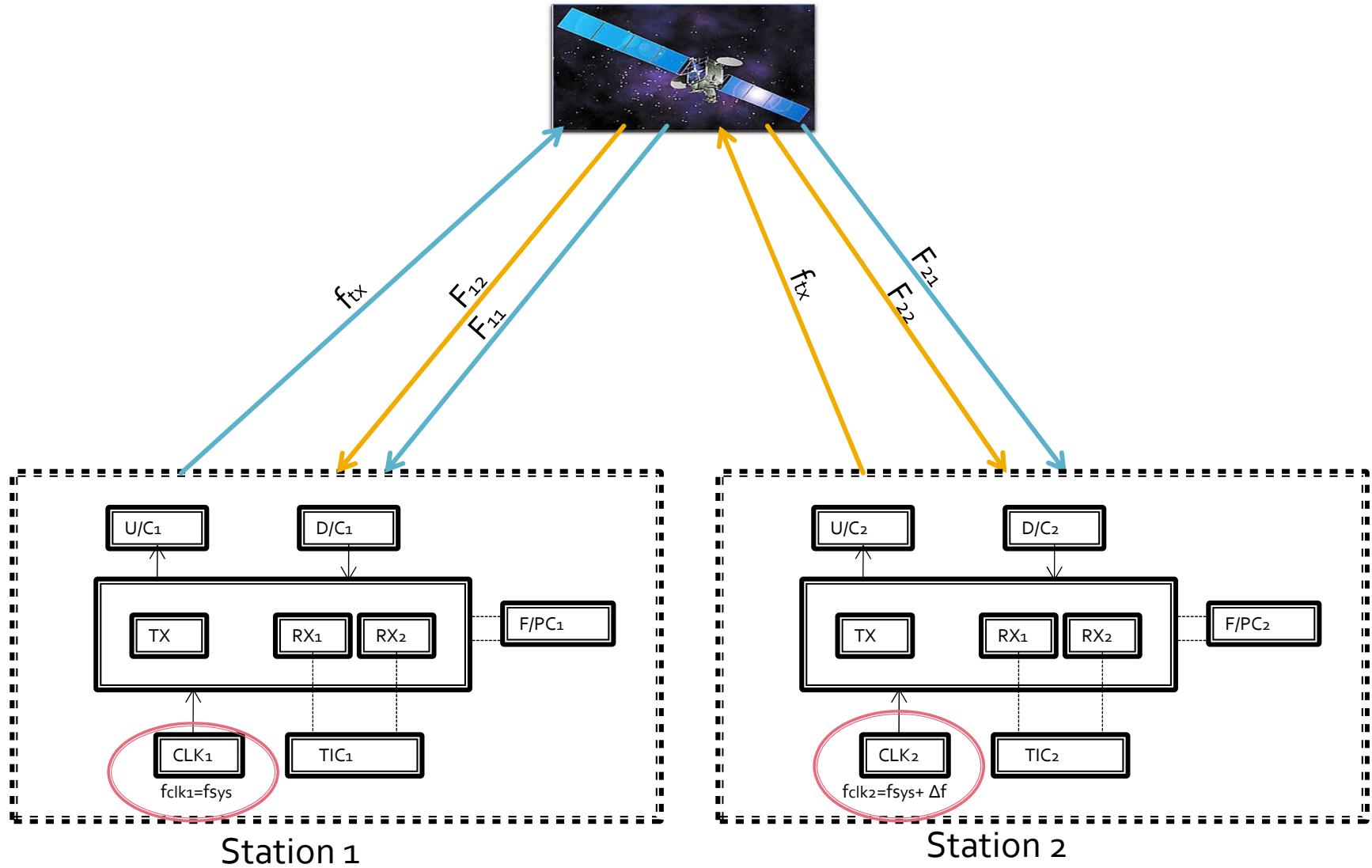
Best results:

- ◻  $8 \times 10^{-16}$  @ 1 day in 2009 with 2.5 Mchips/s
- ◻ Same performance can be reached today at 1 Mchips/s.

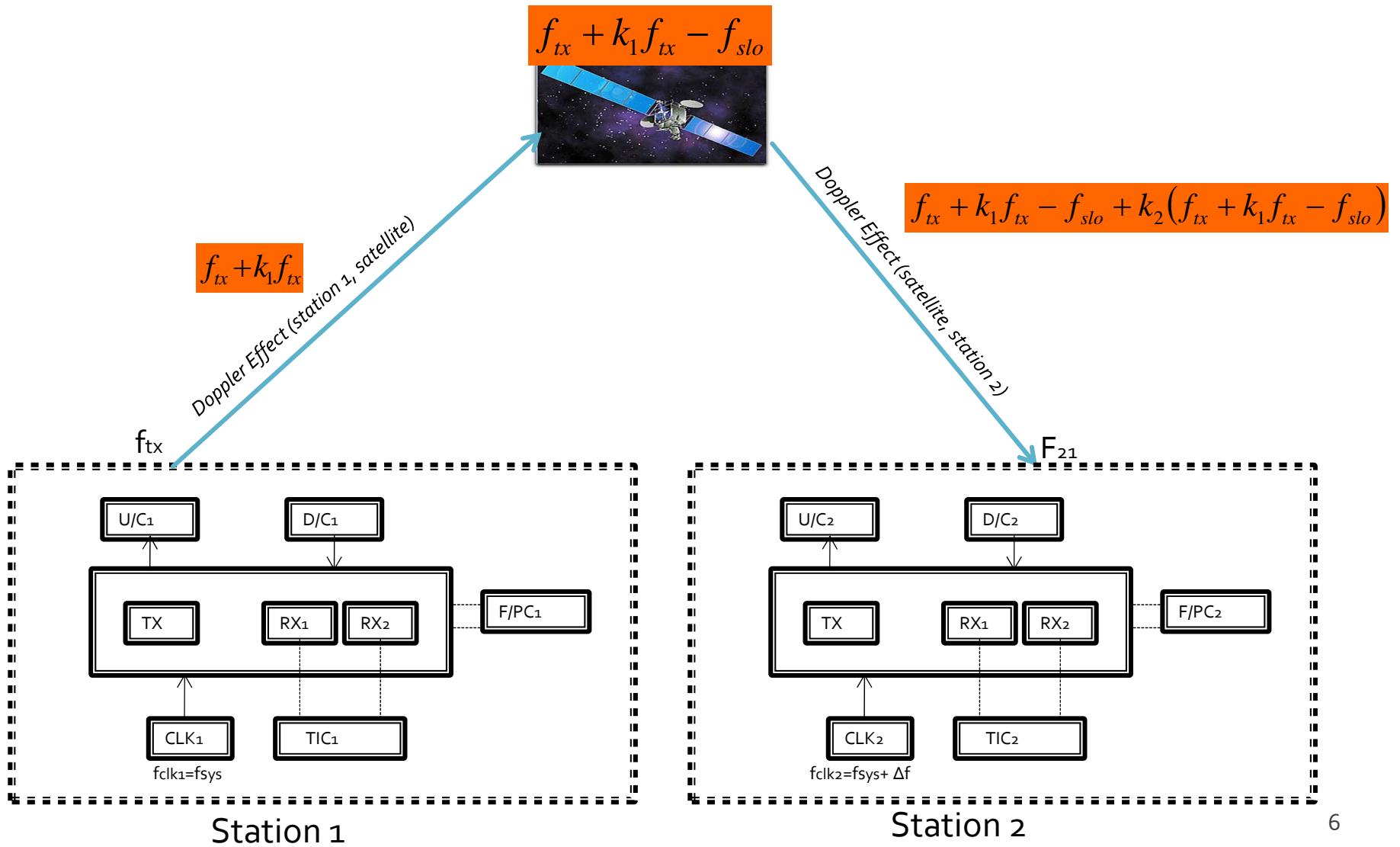
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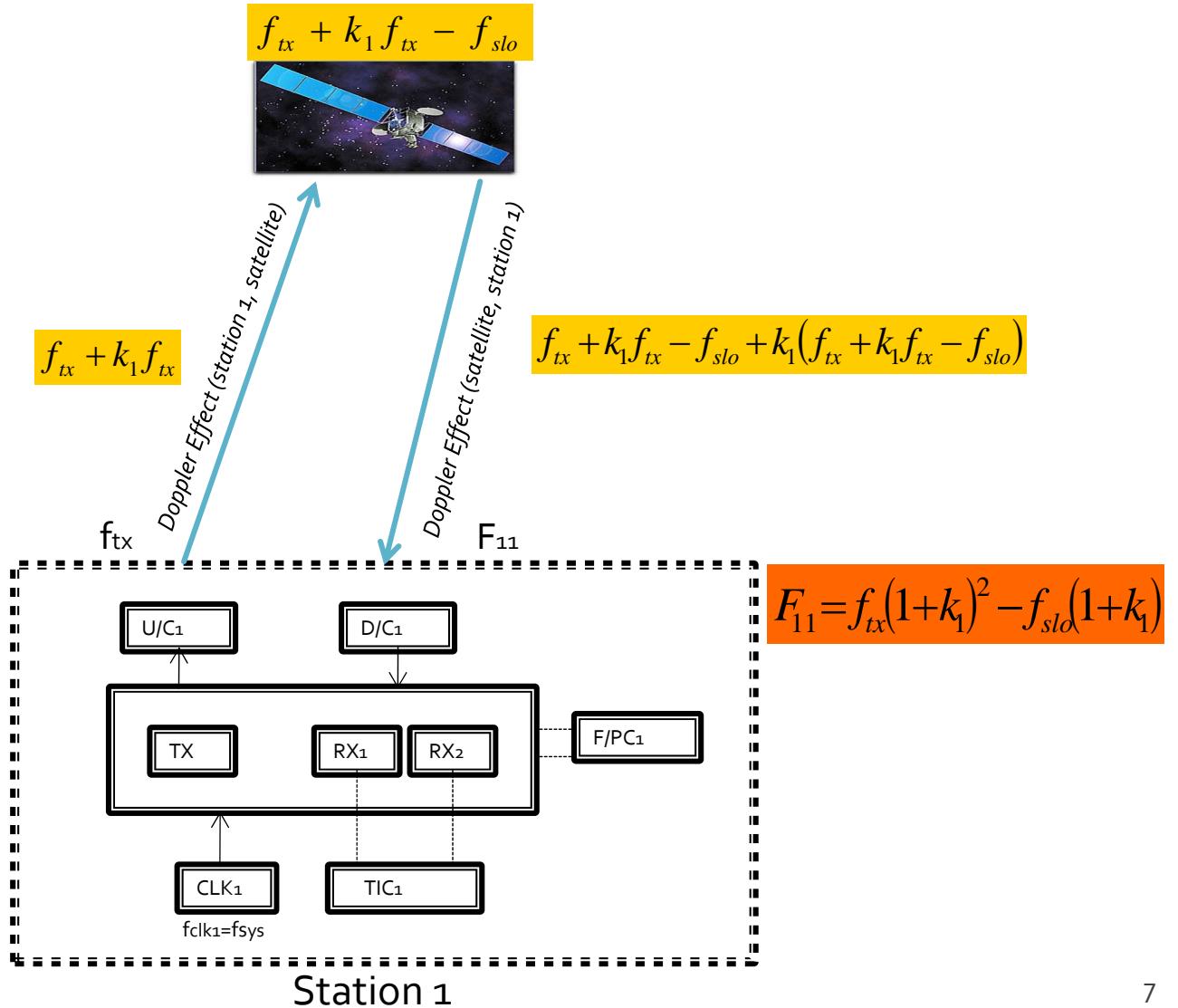
# TWSTFT carrier phase principle



# Transfer from station 1 to station 2



# Ranging Signal



# Doppler effect

- The Doppler coefficients are calculated using the following equation :

$$k_n(t) = \frac{v_n(t)}{c}$$

- $v_n(t)$ : projection of the satellite velocity in the direction of station n at the instant t.
- c : speed of light

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# TWSTFT carrier phase equation system

$$\begin{cases} F_{11} = f_{tx}(1+k_1)^2 - f_{slo}(1+k_1) \\ F_{12} = f_{tx}\left(\frac{f_{sys} + \Delta f}{f_{sys}}\right)(1+k_1)(1+k_2) - f_{slo}(1+k_1) \\ F_{21} = f_{tx}\left(\frac{f_{sys}}{f_{sys} + \Delta f}\right)(1+k_1)(1+k_2) - f_{slo}\left(\frac{f_{sys}}{f_{sys} + \Delta f}\right)(1+k_2) \\ F_{22} = f_{tx}(1+k_2)^2 - f_{slo}\left(\frac{f_{sys}}{f_{sys} + \Delta f}\right)(1+k_2) \end{cases}$$

# System's unknowns

The unknowns of the system are :

- $\Delta f$  : frequency shift between clocks in comparison
- $k_1$  : Doppler coefficient according to station 1
- $k_2$  : Doppler coefficient according to station 2
- $f_{\text{slo}}$  : on-board satellite LO frequency

# Solving the equation system

- Linearization of the equations of the TWSTFT carrier phase system by applying Taylor development and neglecting the terms from the second order

$$\frac{\Delta f}{f_{sys}} = - \left[ \frac{F_{11} - F_{22} - F_{12} + F_{21}}{2} - \frac{f_{tx}(F_{12} - F_{22})}{f_{tx} - f_{slo}} \right] \frac{1}{2f_{tx}}$$

$F_{11}, F_{22}, F_{12}, F_{21}$  are measured.

$f_{slo}, k_1$  and  $k_2$  must be known by other means.

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# System set-up

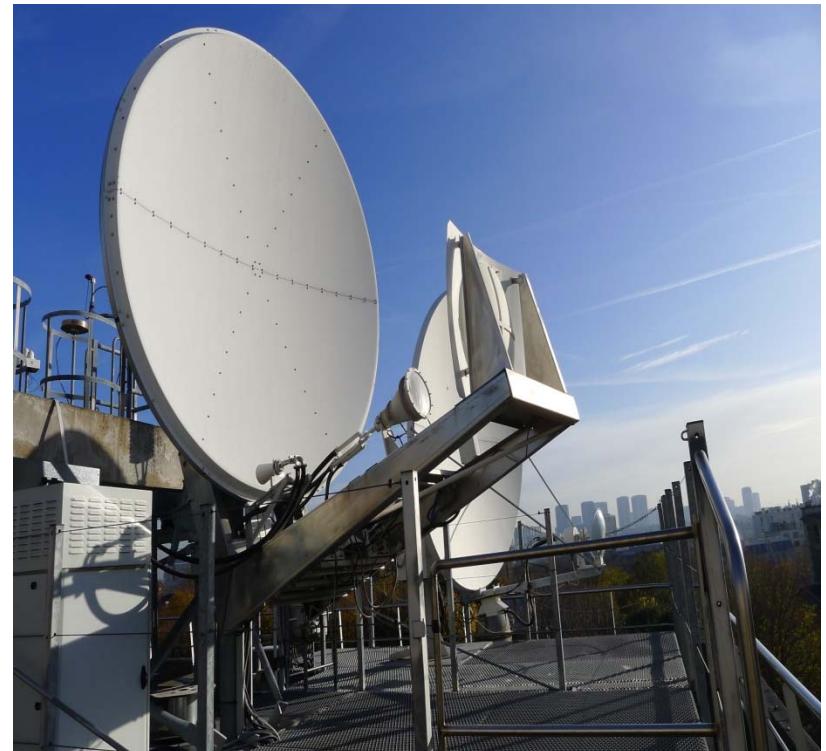
Equipment used :

- 2 TWSTFT stations
- 2 SATRE modems
- 1 Maser clock
- Satellite simulator

Experimental data recorded every second:

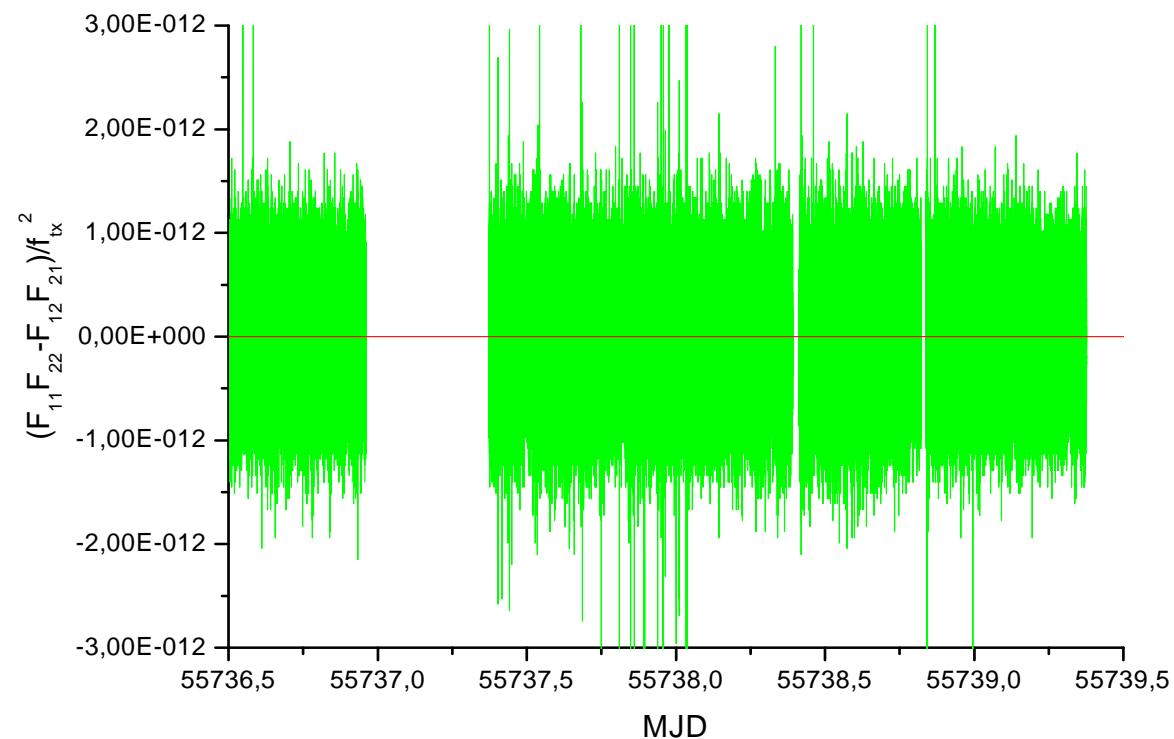
- 1 Mchip/s code delay
- Carrier frequency

- Satellite: Telstar 11 N in the Ku band
- 50 min of measurements during odd hours over one month
- 3 days of continuous 1 s measurements



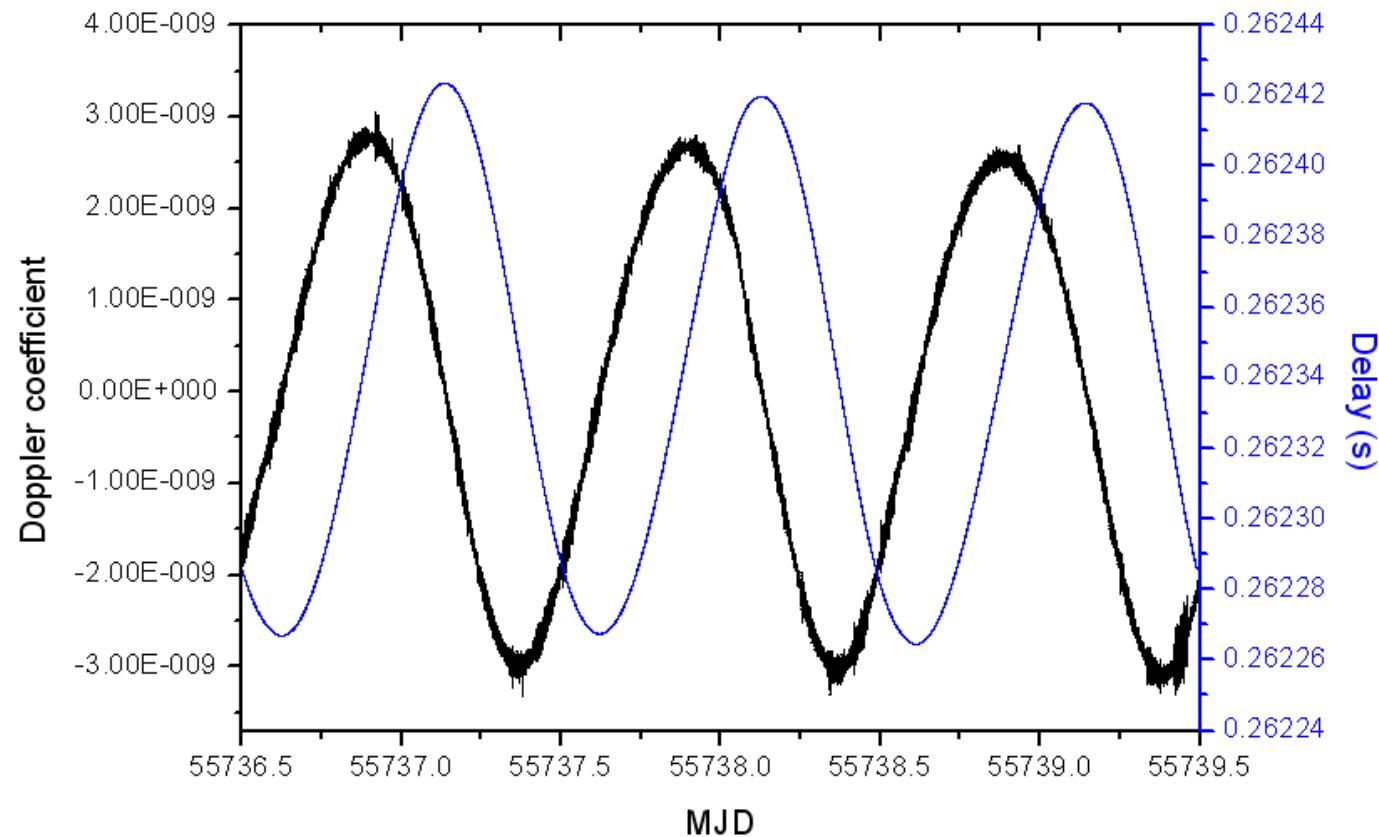
# Results: Experimental validation of the different carrier frequencies

$$F_{11}F_{22} - F_{12}F_{21} = 0$$



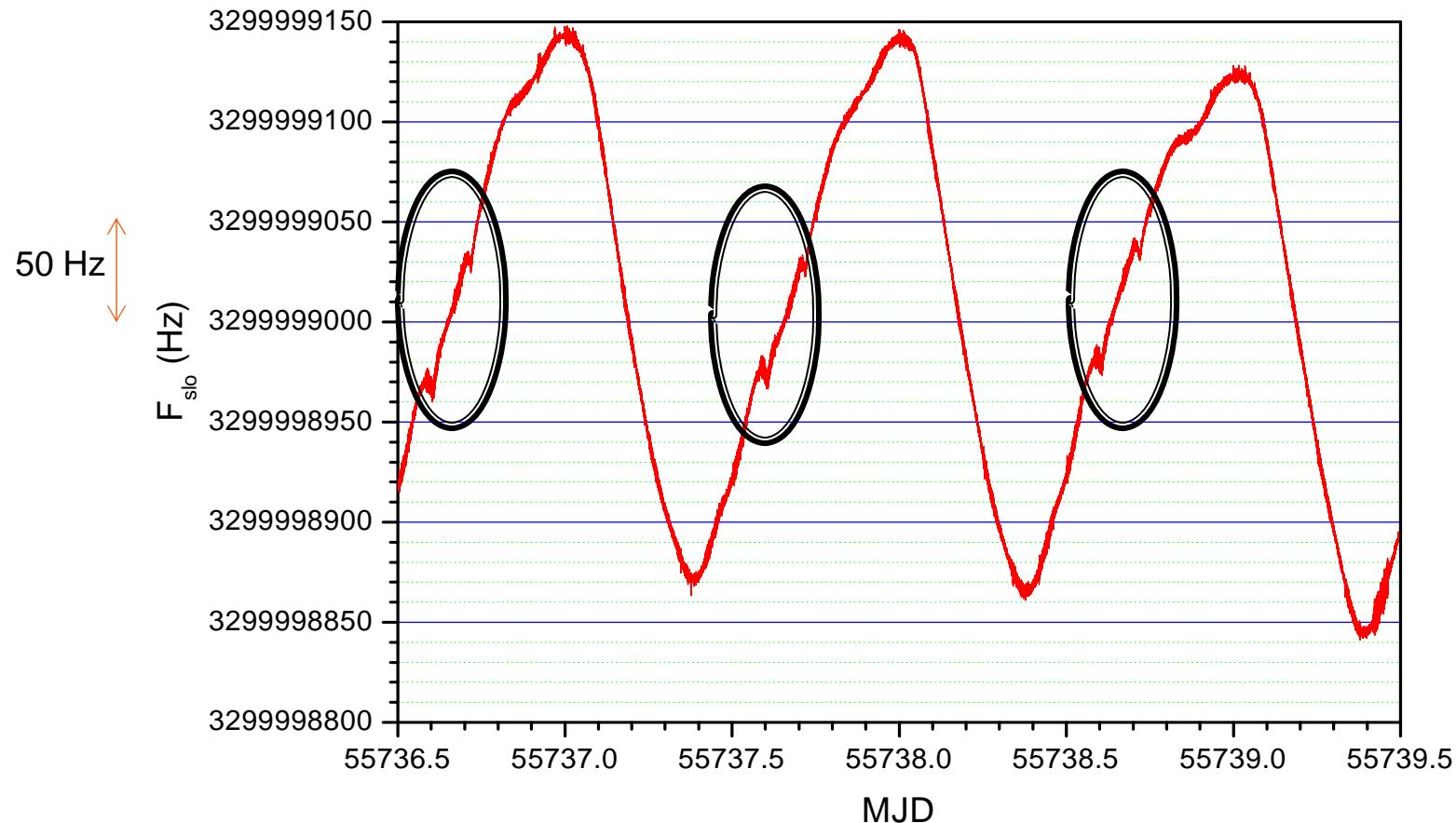
No drift nor offset observed

# Results: Determination of ranging delay and Doppler coefficients



# Results: Satellite LO frequency

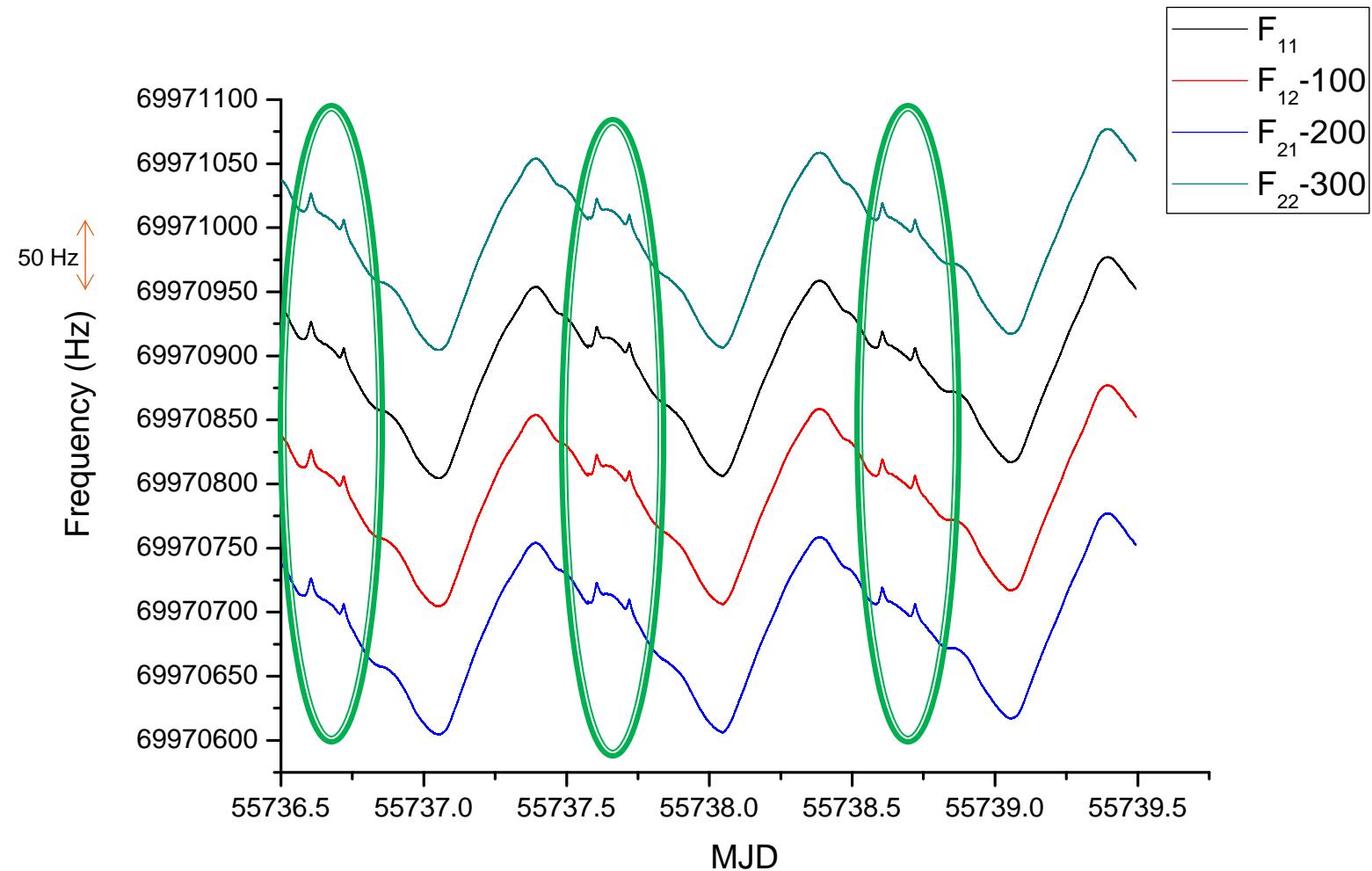
$$f_{slo} = -\left[ \frac{F_{11}}{(1+k_1)} - (1+k_1)f_{tx} \right]$$

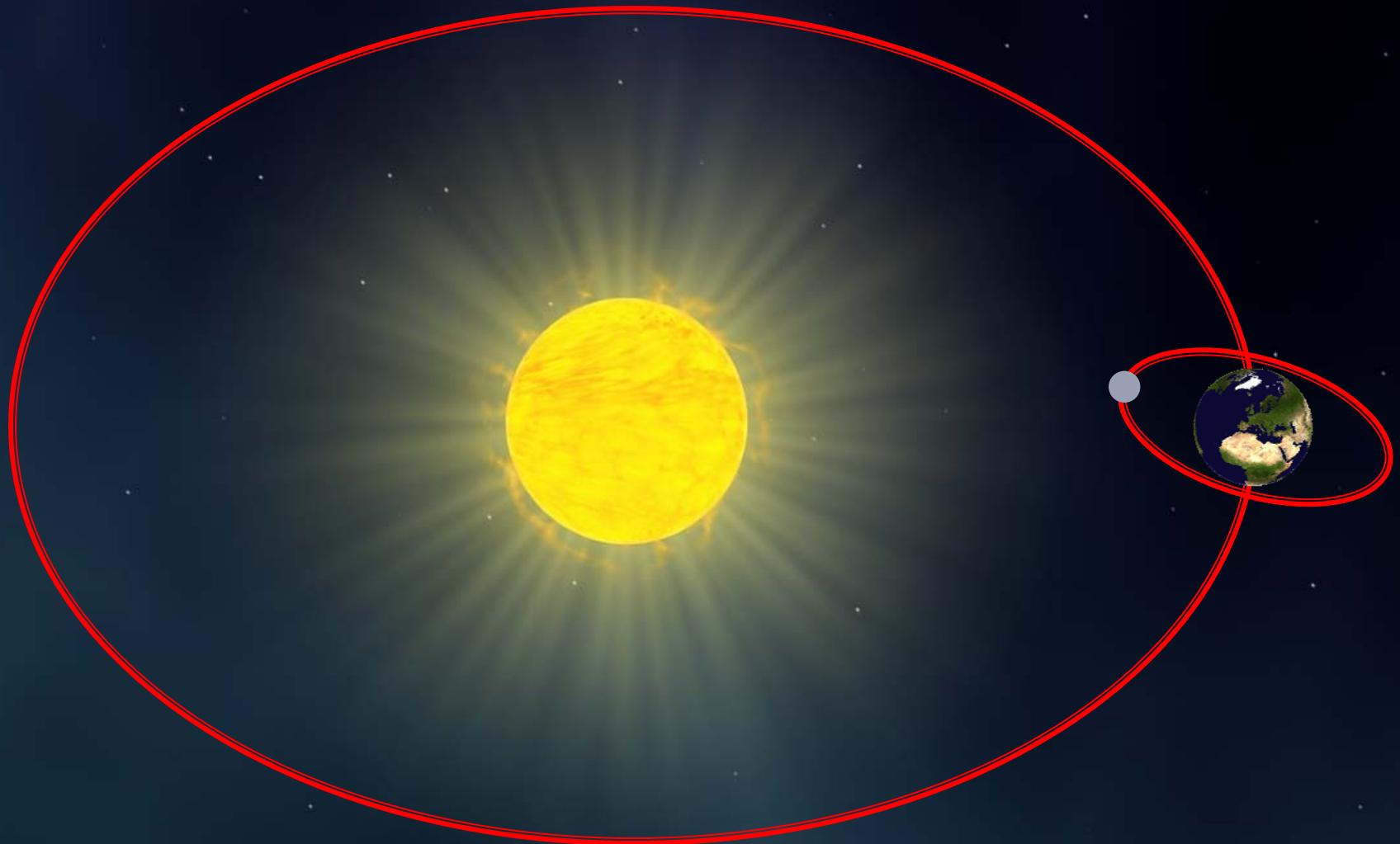


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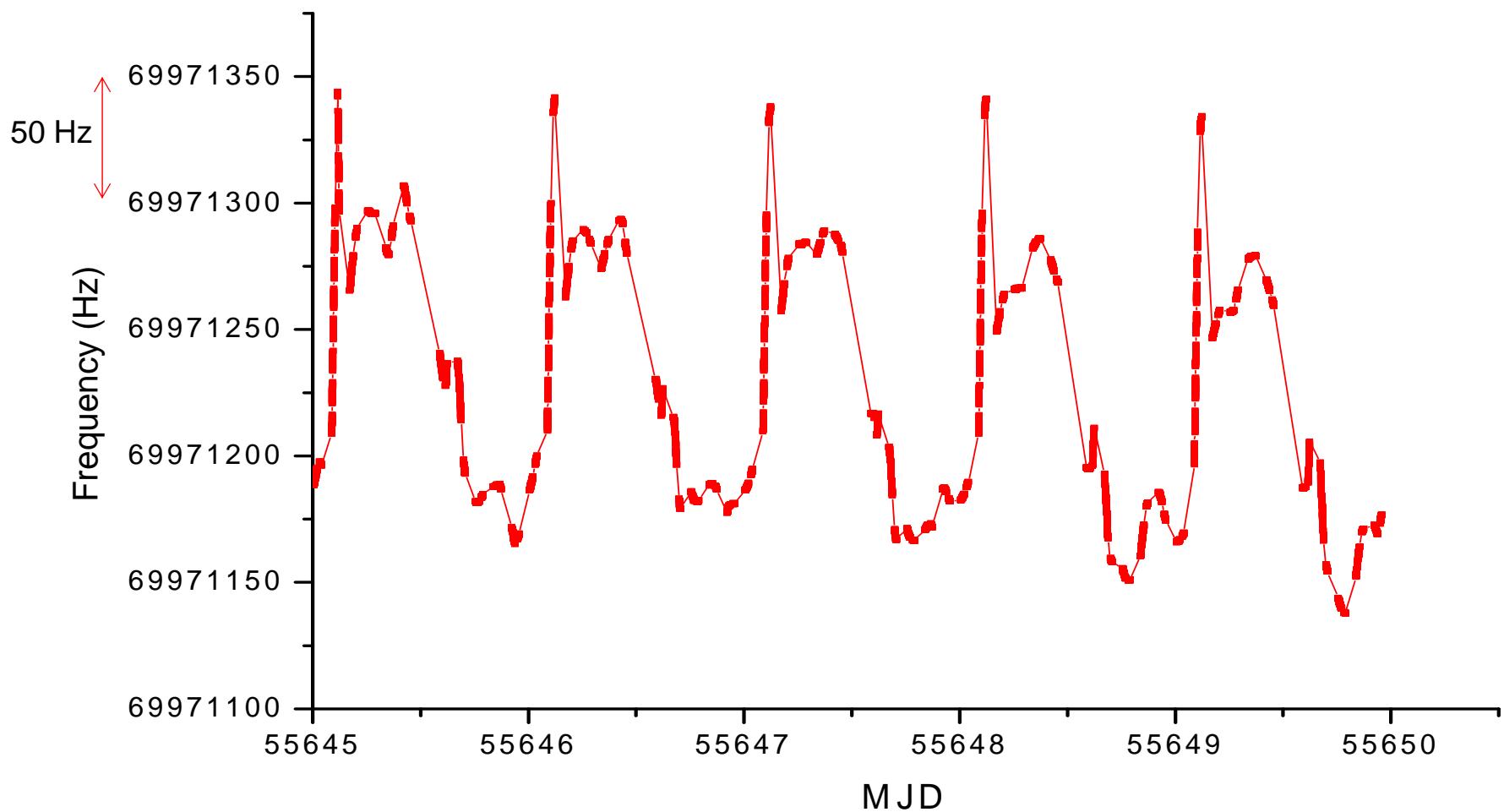
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# Results: Carrier frequency measurements





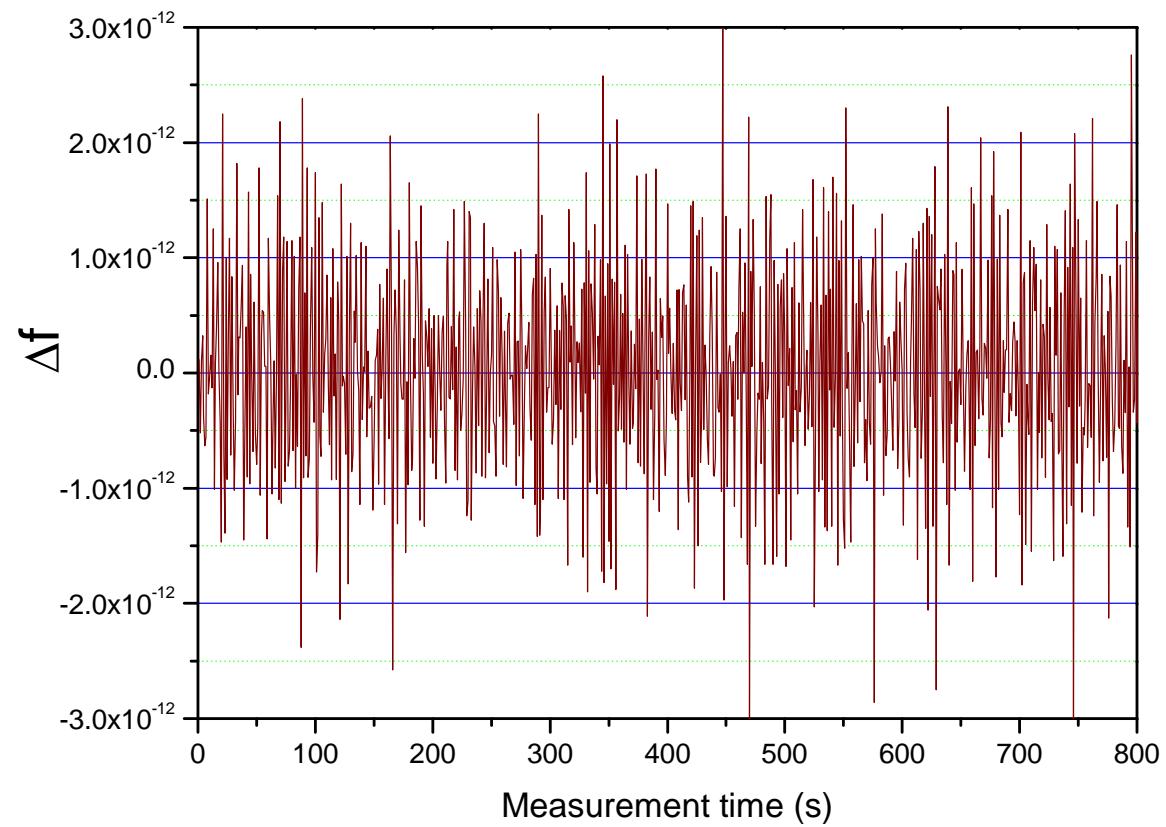
# Understanding the signal distortion

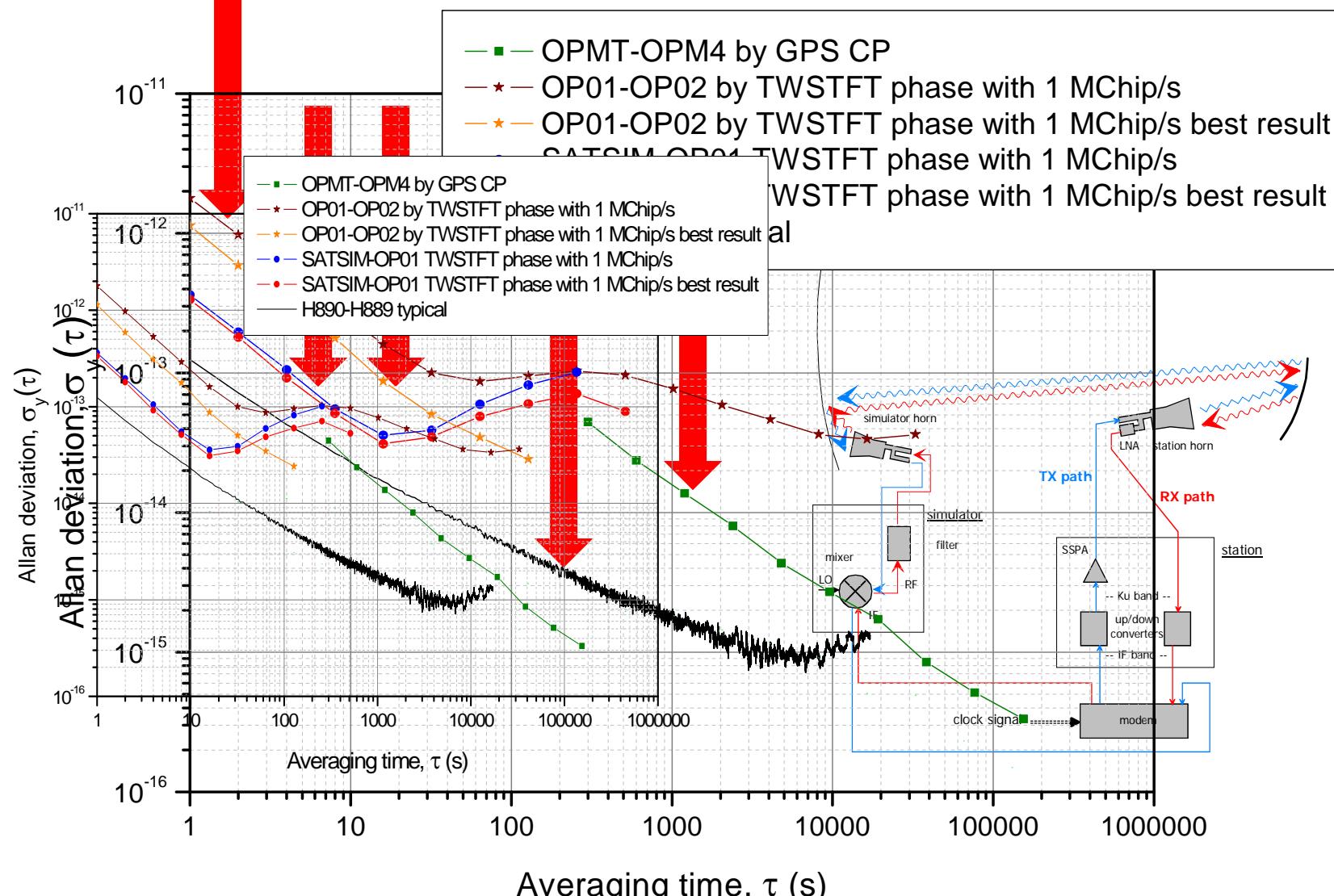


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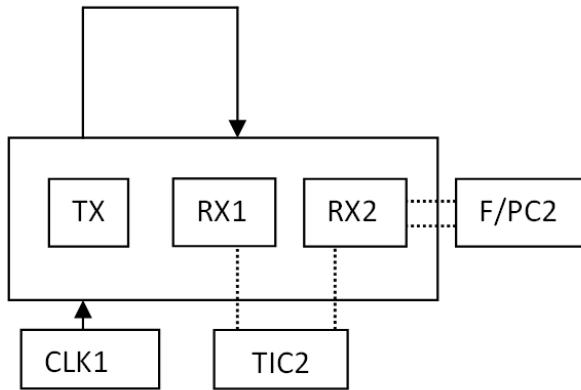
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# Results: Determination of clocks offset (common clock in this case)

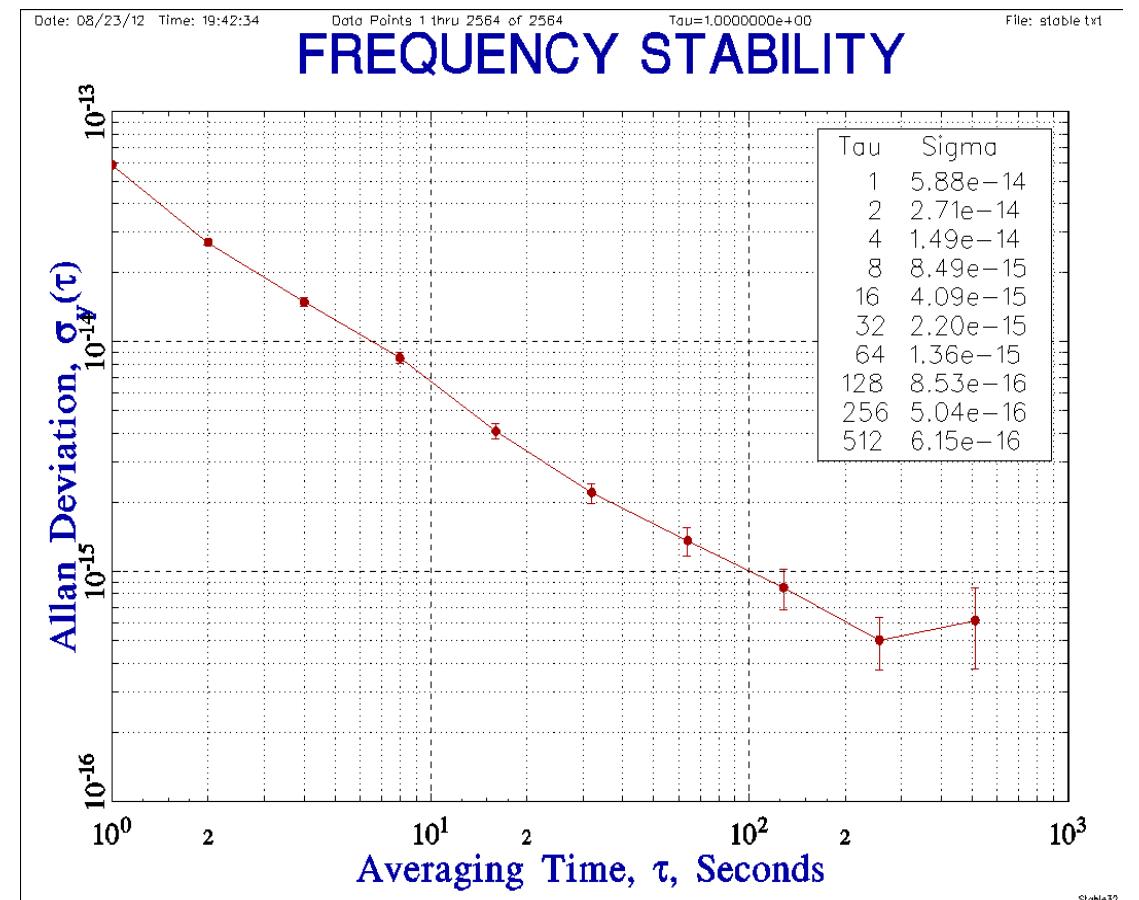




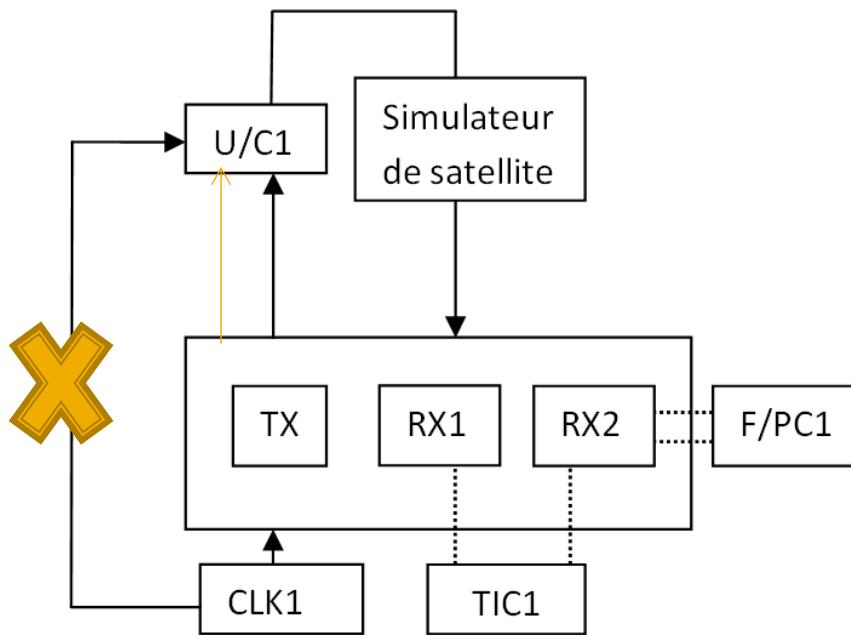
# Additional tests (1)



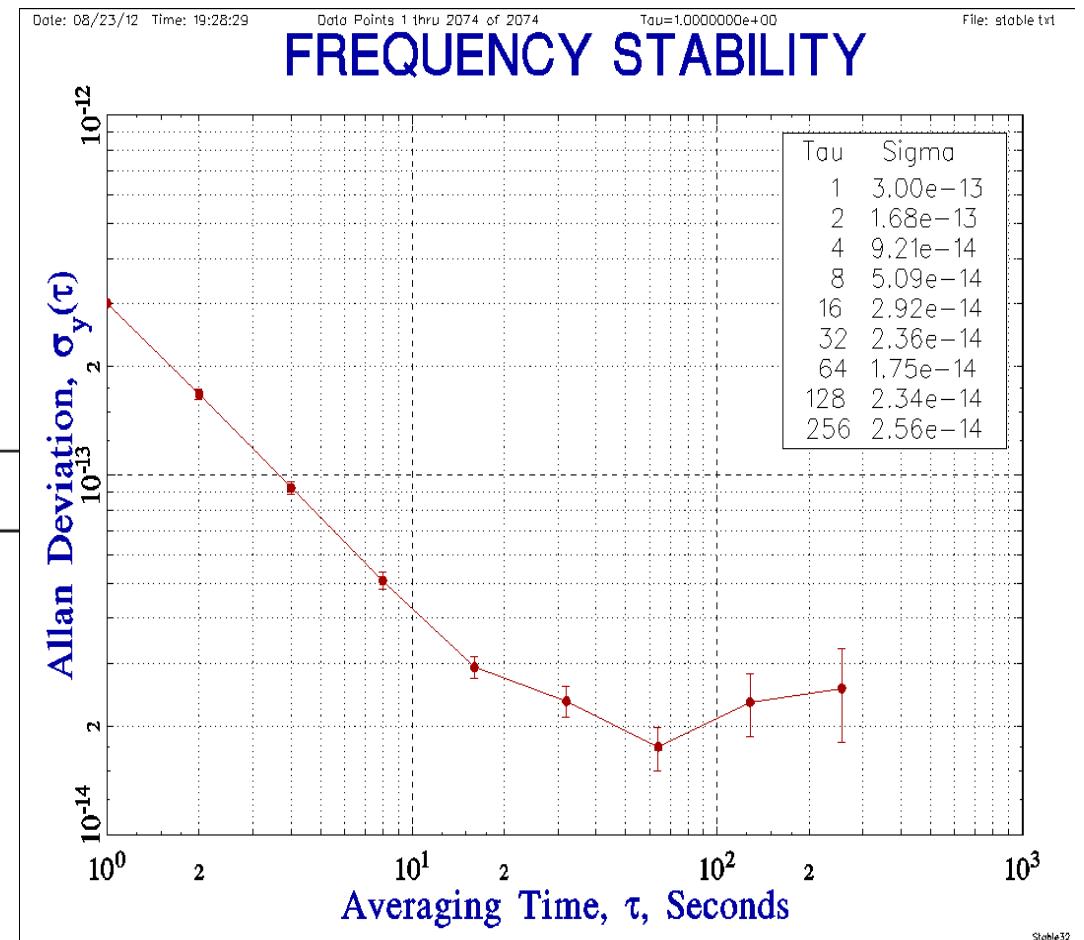
- Satellite
- Atmospheric propagation
- Up and down converters



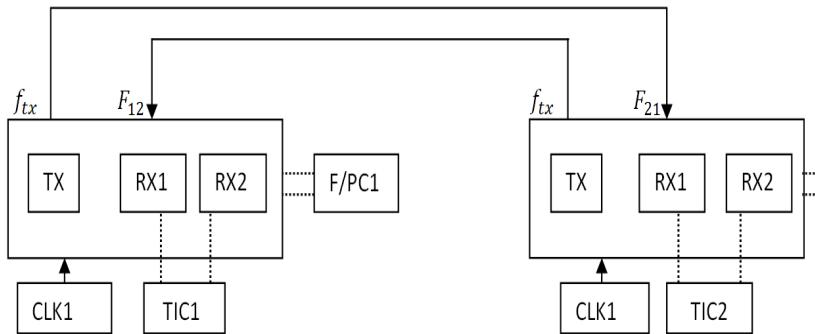
# Additional tests (2)



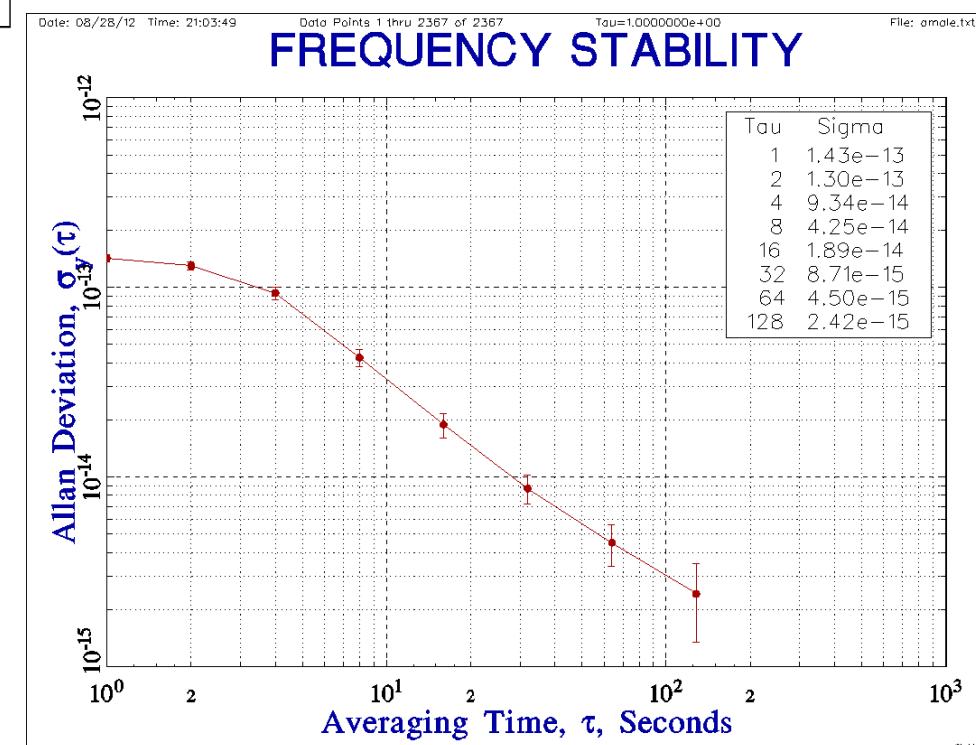
- Satellite
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# Additional tests (3)



- Satellite
- Atmospheric propagation
- Up and down converters



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# Conclusion and outlooks

- We have presented the first results of application of TWSTFT carrier phase method in colocation at LNE SYRTE and we have reported the following performances:
  - ✓  $1 \times 10^{-12}$  at 1 s.
  - ✓  $3 \times 10^{-14}$  at 100 s.
  - ✗ Stability degradation at 300 s seems coming from the used equipments.
- The use of phase data instead of frequency data to overcome the need for doing continuous measurements as in the present case.
- Study of atmospheric effects impact on TWSTFT carrier phase.



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Thank you

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