

1<sup>st</sup> June 2017



28th Meeting of the Consultative Committee for Thermometry (CCT)

# Acoustic Gas Thermometry





Roberto M. Gavioso

## hystorical development

- development of theory: Laplace was finally right
- wide ranging applications of acoustic gas thermometry ...
- ... including primary temperature standards

### milestones along a successful road

- theory and practice of a sphere
- son et lumiere: advantages of the new SI

#### results

- determinations of the molar gas constant *R* and the Boltzmann constant *k*
- determinations of  $T-T_{90}$

## ongoing work and future perspectives

- extending the temperature range of primary acoustic thermometers
- alternatives for dissemination: simplification of primary methods
- practical acoustic thermometers





Temperature / K



#### 1627 - Francis Bacon gedanken experiment



#### To try exactly the time wherein sound is propagated

[..] let a man stand in a steeple, with a candle, veiled; and let another man stand a mile off: then let the person in the steeple strike a bell and at the same instant withdraw the veil; the other, at a distance, may measure the time between the light seen and the sound heard, for light is propagated instantaneously\*

\*Or what comes very near thereto, for in the space of seven or eight minutes it is thought by some to travel from the sun to the earth.

Sylva Sylvarum 1627





#### versatility of Laplace equation

Low-frequency sound velocity near the critical point of xenon\*



1962

THE REVIEW OF SCIENTIFIC INSTRUMENTS



THE PHYSICS OF FLUIDS

VOLUME 10, NUMBER 7

#### JULY 1967

#### imultaneous Ultrasonic and Line Reversal Temperature

APRIL, 1962

#### **Determination in a Shock Tube**

Acoustic Thermometry

VOLUME 33, NUMBER 4

Joseph H. Apfel\*

John Jay Hopkins Laboratory for Pure and Applied Science, General Atomic Division of General Dynamics Corporation, San Diego, California (Received July 3, 1961; and in final form, January 8, 1962) E. H. CARNEVALE, S. WOLNIK, G. LARSON,\* C. CAREY Parametrics, Inc., Waltham, Massachusetts AND

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FIG. 2. Oscilloscope trace of voltage across transceiver. The transmitted burst occurs during the blank space and is followed by the reflected and "ringing" signals. From the decay of the ringing signal the cavity Q can be determined.





Fig. 7. Temperatures in reflected shock region in pure neo obtained by ultrasonics.

#### sonic anemometry (& thermometry)



sonic anemometers are sensors that are able to estimate wind speed vector by measuring the influence of local wind speed on the transmission of ultrasound signals between pairs of emitters and receivers that configure acoustic paths. This estimation is normally assigned to the geometric center of acoustic path midpoints



sonic anemometers are used to evaluate the turbulent heat flux from the sonic kinematic heat flux (or "temperature flux"), i.e. the covariance of the vertical wind velocity w and the sonic temperature T the vertical wind velocity w and the speed of sound *c* being simultaneously measured by the anemometer, and the speed of sound being then corrected for the effect of the crosswind

sonic kinematic heat flux



sonic temperature



turbulent heat flux





FIG. 1. Ray paths from source to receiver sites are refracted geodesics, i.e., great circles corrected for Earth flattening and horizontal sound speed gradients. The source array was suspended from R/V CORY CHOUEST 50 km southeast of Heard Island. Single dots indicate sites with single receivers. Dots connected by horizontal lines designate horizontal bottom-mounted arrays, vertical lines designate vertical arrays, and slanted lines designate arrays towed in the direction of the arrow. Signals were received at all sites except for the vertical array at Bermuda (which sank) and the Japanese station off Samoa.

# **Geophysical Research Letters**

# RESEARCH LETTER

10.1002/2015GL063438

#### Key Points:

- Deep-ocean temperature variations can
   be measured using only ambient noise
- This method can be more precise than direct temperature measurements

## Monitoring deep-ocean temperatures using acoustic ambient noise



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**abstract**: measuring temperature changes of the deep oceans, important for determining the oceanic heat content and its impact on the Earth's climate evolution, is typically done using free-drifting profiling oceanographic floats with limited global coverage. Acoustic thermometry provides an alternative and complementary remote sensing methodology for monitoring fine temperature variations of the deep ocean over long distances between a few underwater sources and receivers. We demonstrate a simpler, totally passive (i.e., without deploying any active sources) modality for acoustic thermometry of the deep oceans (for depths of ~ 500–1500 m), using only ambient noise recorded by two existing hydroacoustic stations of the International Monitoring System. We suggest that passive acoustic thermometry could improve global monitoring of deep-ocean temperature variations through implementation using a global network of hydrophone arrays



(A) Locations of the two hydroacoustic stations (red dots) near Ascension and Wake Islands.. (B) Zoomed-in schematic of the hydrophone array configurations for the Ascension and Wake Island sites, which both have a similar layout. Each hydroacoustic station consists of a northern and southern triangle array of three hydrophones (or triad), with each triangle side equal to approximately 2 km. The distance L between triad centers is equal to 126 km and 132 km for the Ascension and Wake Island stations, respectively.

(C) Noise cross-correlation waveforms, averaged over three different years, obtained between all 9 pairwise combinations of the elements of the north and south triads for the Wake Island. (D) Same as C, but for Ascension Island. The beams shown by dashed lines in A are centered on the lines joining the centers of the south and north triads of each hydroacoustic station (yellow line) and which intersect the Polar regions where potential ice noise sources contributing to the coherent arrivals shown in C-D are located (18b). ideal gas assumptions:

- the molecules of the gas are indistinguishable, small, hard spheres
- collisions are elastic and motion is frictionless (no energy loss)
- Newton's laws apply

ideal das

- average distance between molecules is much larger than molecular size
- · the molecules constantly move in random directions with a distribution of speeds
- · there are no attractive or repulsive forces between the molecules

- DT / 1/

$$\begin{array}{l} \sum_{kinetic energy} & \overline{2} m v_{rms} = \frac{1}{2} \kappa I \\ u_0^2(T) = \left(\frac{\partial p}{\partial \rho}\right)_s = \gamma_0 \frac{kT}{m} = \gamma_0 \frac{RT}{M} = \frac{1}{3} \gamma_0 \frac{v_{rms}^2}{v_{rms}^2} \\ 1873 \\ \hline 1873 \\$$

mean



3

1\_7

2





Fig. 4. A comparison, with values of the  $T_{5*}$  scale, of temperatures derived from (i) SOUD (pressure-volume isotherm measurements, (ii) gas thermometry measurements, and (iii) acoustical-thermometer measurements (19). (Open circles, plain or bisected) Gas-Rayle (thermometer values [Schmidt and Keesom (20)]; (solid circles) gas-thermometer values [Kistemaker (21)]; (crosses) isotherm values [Kistemaker (21)]; (open triangles) gasexpel (Keller (23)]; (solid squares) He\* isotherm values [Keller (23)]; (solid triangles) preliminary acoustical-thermometer values [Cataland *et al.* (24)]; (solid diamonds) acousticalthermometer values obtained in the work described.  $T_x$  represents actual values of temperature as determined by the experimenters.



Fig. 5. A comparison between the acoustically derived temperature scale [NBS Provisional Scale 2-20 (1965)] and the NBS (1955) temperature scale (25). The difference in the values of the two scales, as indicated by two germanium resistors, is plotted as a function of the Kelvin temperature.

# **Gas-filled spherical resonators: Theory and experiment**

Michael R. Moldover Thermophysics Division, National Bureau of Standards, Gaithersburg, Maryland 20899

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<u> 1979 - 1988</u>

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(Received 9 August 1985; accepted for publication 20 October 1985)

$$u = \frac{2\pi a}{z_N} \left( f_N - \Delta f_{\text{thermal}} - \Delta f_{\text{viscous}} - \Delta f_{\text{shell}} - \Delta f_{\text{ducts}} \right)$$

 $g_N = g_{\text{bulk}} + g_{\text{thermal}} + g_{\text{viscous}} + g_{\text{ducts}}$ 



VOLUME 60, NUMBER 4

#### PHYSICAL REVIEW LETTERS

#### 25 JANUARY 1988

#### Measurement of the Universal Gas Constant R Using a Spherical Acoustic Resonator

1988

M. R. Moldover, J. P. M. Trusler, <sup>(a)</sup> and T. J. Edwards<sup>(b)</sup> Thermophysics Division, National Bureau of Standards, Gaithersburg, Maryland 20899

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and

R. S. Davis Length and Mass Division, National Bureau of Standards, Gaithersburg, Maryland 20899 (Received 6 November 1987)

 $k = R/N_{\rm A} = (1.380\ 651\ 3\ \pm\ 0.000\ 002\ 5) \times 10^{-23}\ {\rm J\ mol^{-1}\ K^{-1}}$ 

(1.8 ppm) Figure 10. Photograph of weights and weighing bottle ready to be loaded into the balance.



**VOLUME 34, NUMBER 4** 

## Measurement of the ratio of the speed of sound to the speed of light

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$$u(p,T) = f_{ac}(p,T) \frac{2\pi a(p,T)}{z_{ac}}$$
$$c(p,T) = \left\langle f_{mw}(p,T) \right\rangle \frac{2\pi a(p,T)}{z_{mw}}$$

$$\frac{u(p,T)}{c(p,T)} = \frac{f_{ac}(p,T)}{\left\langle f_{mw}(p,T) \right\rangle} \frac{z_{mw}}{z_{ac}}$$



$$\left[\text{temperature}\right] = \frac{\left[\text{energy}\right]}{\left[k_{\text{B}}\right]} = \frac{\left[\text{mass}\right]\left[\text{velocity}\right]^{2}}{\left[k_{\text{B}}\right]} = \frac{\left[\text{mass}\right]}{\left[k_{\text{B}}\right]} c_{0}^{2} \lim_{p \to 0} \frac{\left[\text{frequency}\right]^{2}_{\text{sound}}}{\left[\text{frequency}\right]^{2}_{\text{light}}}$$







# Thermodynamic Temperatures of the Triple Points of Mercury and Gallium and in the Interval 217 K to 303 K



M. R. Moldover, S. J. Boyes<sup>1</sup>, C. W. Meyer, and A. R. H. Goodwin<sup>2</sup>

$$\frac{T}{T_{\text{TPW}}} = \lim_{p \to 0} \left( \frac{u^2(p,T)}{u^2(p,T_{\text{TPW}})} \right)$$



**Table 2.** Standard uncertainties  $u_s \times 10^6$  from various sources in the re-determination of  $(T-T_{90})/T$  is calculated twice: first, including Rows 4 and 5, but not Rows 6 and 7; and second, including

Source	217 K	234 K
	Microwave values for $[a(T)/a(T_w)]^2$	
1. Discrepancies among triplets	0.32	0.27
2. $\delta_{\rm m}(T)$ calc. from resistivity $(0.04 \times \rho)$	0.39	0.25
3. $\delta_{\rm m}(T)$ calc. $-\delta_{\rm m}(T)$ meas.	0.24	0.24
	Acoustic (isotherm fits)	
4. Uncertainty of $A_0(T_w)/a^2$	1.67	1.67
5. Uncertainty of $A_0(T)/a^2$	2.31	1.85
	Acoustic (surface fit)	
6. Uncertainty of $A_0(T_w)/a^2$	0.25	0.25
7. Uncertainty of $A_0(T)/a^2$	0.52	0.38
	Thermometry	
8. SPRT & bridge repeat. @ $T_w$ (10 $\mu\Omega$ )	0.46	0.43
9. Difference between calibrations	0.22	0.15
10. Temperature gradient	0.46	0.43
11. Non-uniqueness of ITS-90	0.9	0.0
	Additional sources	
12. Thermal conductivity (0.3 %)	0.20	0.20
13. Uncertainty of pressure zero	0.21	0.12
14. Isotherm fits: RSS	3.13	2.62
15. Surface fit: RSS	1.42	0.92
16. Isotherm fits: RSS×( $T$ /mK)	0.68	0.61
17. Surface fit: RSS×(T/mK)	0.31	0.22
· · ·		



FIGURE 1. The spherical resonator and its thermal environment: 1, spherical resonator; 2, isothermal shield; 3, vacuum jacket; 4, thermometer mount; 5, copper block; 6, copper block; 7, inlet tube; 8, to vacuum; 9, to vacuum guage.

100 mm



# 303 K, 430 K, 505 K

# NIST

# Progress in Primary Acoustic Thermometry at NIST: 273 K to 505 K

G. F. Strouse, D. R. Defibaugh, M. R. Moldover, and D. C. Ripple

TABLE 3. NIST Acoustic Thermometer uncertainty budget in millikelvins for the determination of  $T - T_{90}$ .



**FIGURE 1.** Schematic of the NIST acoustic thermometer inside the pressure vessel.

**FIGURE 3.**  $T - T_{90}$  and corresponding uncertainty (k = 1) values for the NIST Acoustic Thermometer and results from the literature.

Metrologia 41 (2004) 74-98

# Acoustic measurements of the thermodynamic temperature between the triple point of mercury and 380 K

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Frequency / MHz

METROLOGIA





OCTOBER 2004



NIST National Institute of Standards and Technology U.S. Department of Commerce

# Quasi-spherical cavity resonators for metrology based on the relative dielectric permittivity of gases

Eric F. May,<sup>a)</sup> Laurent Pitre,<sup>b)</sup> James B. Mehl,<sup>c)</sup> Michael R. Moldover,<sup>d)</sup> and James W. Schmidt Process Measurement Division, National Institute of Standards and Technology, Gaithersburg, Maryland 20899-8360

(Received 20 April 2004; accepted 23 June 2004; published 22 September 2004)





Temperature / K



#### 271 K to 552 K

# Acoustic Thermometry Results from 271 to 552 K

D. C. Ripple · G. F. Strouse · M. R. Moldover



Fig. 1 Deviation of measured thermodynamic temperature T from  $T_{90}$  for recent acoustic determinations and the constant-volume gas thermometry (CVGT) of Edsinger and Schooley [4] and Schooley [5]. For the present work, standard uncertainties are only shown for the recommended Surface Fit







coordinator J. Fischer

2008 - 2011 iMERA- Plus Research Project Determination of the Boltzmann constant for the redefinition of the kelvin





National Institute of



# Thermodynamics vs. ITS



Metrologia Boltzmann Special Issue 2015, R. White and J. Fischer Figure 1: Relative uncertainty in the value of Boltzmann's constant. Also shown is the relative reproducibility of the practical temperature scales, in the vicinity of 100 °C.

Physikalisch-Technische Bundesanstalt 
Braunschweig und Berlin

#### determinations of k with AGT and other methods 2017 (yesterday)







EURAMET

coordinator G. Machin

# 2012 - 2015 EMRP Research Project

Implementing the new kelvin - InK







METROLOGICA

Int J Thermophys (2014) 35:971-984

2016 - 2019 EMRP Research Project

Implementing the new kelvin 2 - InK2

coordinator G. Machin

 $T-T_{90}$  by Acoustic Gas Thermometry (AGT) between 430 K and 933 K



# Microwave-cavity measurements for gas thermometry up to the copper point

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METROLOGIA

doi:10.1088/0026-1394/50/3/219











2016 -2019 EMRP Research Project Implementing the new kelvin 2 - InK2

# T- $T_{90}$ by Acoustic Gas Thermometry between 5 K and 200 K



#### **Benefits**

- 2-stage pulse-tube cryostat → no LHe
- 2 thermal shields and 2 vacuum chambers
- minimum temperature < 4 K
- same calorimeter for T and  $T_{90}$  realization
- houses a larger number of CSPRTs
- provides good stability especially in ranges 30 K – 77 K and 150 K – 234 K

#### Risks and drawbacks

- vibrations could affect measurements
- complex design, needed long realization time

extending the temperature range of primary thermometers

AGT at T < 4 K

## The cold valve



The prototype sphere





# The Cryogenic Current Comparator Amplification and its shield









alternatives for dissemination: simplification of primary methods

$$u_0^2(p,T) = u^2(p,T) - [A_1(T)p + A_2(T)p^2 + ...]$$



measured

#### calculable for He

- material: copper; shape: triaxial ellipsoid; interrnal radius: 4 cm; interrnal volume: 260 cm<sup>3</sup>; thick wall to minimize shell coupling; the cavity is designed to be vacuum- and pressure tight
- excitation of acoustic and microwave resonances by waveguides
- embedded thermometer wells for cSPRTs and long-stem SPRTs
- working gas: helium (calculable properties) purity maintained by a getter
- temperature range of initial tests: 230 K to 430 K;
- aimed accuracy: ± 5 ppm



termination of acoustic and microwave waveguides











calibration zone with Peltiers





Int J Thermophys DOI 10.1007/s10765-010-0793-x

Practical Acoustic Thermometry with Acoustic Waveguides

M. de Podesta + G. Sutton + R. Underwood + S. Legg + A. Steinitz