Improvements in the algorithms for UTC

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Summary

- Progress on the UTC algorithm: changing of the weighting algorithm (January 2014)
- Analysis and limits of the algorithm for the uncertainty of [UTC-UTC(k)] published on sec. 1 of Circular T (with Gerard Petit and Aurelie Harmegnies)
- Future development: Kalman Filter applied to UTC (with Federica Parisi from the University of Turin)



To improve reliability and long-term stability of UTC, the maximum number of clocks of different types contributing is required.

With the revision of the weighting algorithm the clocks presenting strong signatures are used in an optimal way.

New Algorithm
Good clock: Predictable Clock
Weight = f(predictability)
Frequency drift considered
All type of clocks used in an optimal way
Wmax=4/N

Weighting procedure



Poids et
 Mesures

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Perfomance of EAL with repect to each PSFS and to the Rubidium Fountains



Mesures

By changing the weighting algorithm the role of the caesium clocks and Hydrogen Masers changed completely.



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Weight Analysis - 2

By changing the maximum weight from w_{max} =2.5/N to w_{max} =4/N the number of clocks at maximum weight decreases but the combined weight of clocks at maximum weight increases.



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Weighting algorithm changed

The performance of EAL and TAI and with respect to PSFS



The Uncertainty on [UTC-UTC(k)] (with G. Petit and A. Harmegnies)

The calculation of the uncertainties is obtained by applying the law of the propagation uncertainty on:

$$x_{j}(t) = EAL - h_{j}(t) = \sum_{i=1}^{N} w_{i}[h'_{i}(t) - x_{i,j}(t)]$$

The obtained solution is depending on the time link uncertainties and on the atomic clock weights:

$$u_{x_j}^2 = \sum_{i=1}^N w_i^2 u_{x_{i,j}}^2 + 2 \sum_{i=1}^{N-1} \sum_{k=i+1}^N w_i w_k u_{(x_{i,j}, x_{k,j})}$$

Until now the data are expressed as time links to a pivot laboratory (PTB) and are considered uncorrelated.

Present: Odd feature 1 (pivot uncertainty)

Date	2015 Oh UTC	JAN 27	FEB 1	FEB 6	FEB 11	FEB 16	FEB 21	FEB 26	Unce	rtaint	y/ns N	otes
1	MJD	57049	57054	57059	57064	57069	57074	57079	uA	uB	u	
Labor	atory k				[UTC-UTC	k)]/ns			111.000			
AOS	(Borowiec)	-0.8	0.2	0.7	1.4	0.6	-1.0	-3.2	0.3	5.1	5.1	
BEV	(Wien)	12.1	8.2	-3.7	-9.0	-19.2	-27.7	-38.5	0.3	3.1	3.1	
BIM	(Sofiya)	2019.8	2017.3	2043.3	2041.9	2065.6	2057.3	2071.9	1.5	7.0	7.2	
BIRM	(Beijing)	28.0	28.4	24.1	13.8	5.9	-4.6	-4.4	1.5	20.0	20.1	
CAO	(Cagliari)	-2937.7	-3053.5	-3177.4	-3298.8	-3419.3	-3544.6	-3668.8	8.0	7.0	10.7	
CH	(Bern-Wabern)	12.8	10.5	6.7	7.4	7.9	7.9	6.2	0.3	1.3	1.3	
DFNT	(Tunis)	72	4876.6	5077.1	5276.7	5481.0	5662.4	5843.2	1.5	20.0	20.1	
IT	(Torino)	-1.8	-0.6	-0.4	-0.1	-0.1	-0.3	-0.6	0.3	1.4	1.4	
NICT	(Tokyo)	-4.7	-6.1	-7.1	-9.3	-13.8	-17.3	-16.0	0.3	4.7	4.7	
NIST	(Boulder)	3.5	2.6	2.5	3.0	2.5	2.6	3.5	0.3	4.8	4.8	
OP	(Paris)	1.1	1.4	0.9	1.4	1.1	1.2	1.1	0.3	1.3	1.3	
PTB	(Braunschweig)	-0.6	-0.1	0.5	1.5	1.6	2.1	1.9	0.1	0.8	0.8	1
USNO	(Washington DC)	0.6	0.6	0.8	1.3	1.3	1.2	1.8	0.2	1.0	1.0	

6 - Time links used for the computation of TAI and their uncertainties.

1 A A		10 10			10	10 10	
Link	Type	uA/ns	uB/ns	Calibration Type	Calil	oration Da	ates
							2009
AOS /PTB	GPSPPP	0.3	5.0	LC(GPS P3)		2011	Jun
BEV /PTB	GPSPPP	0.3	3.0	BC (GPS MC)		2012	Mar
BIM /PTB	GPS MC	1.5	7.0	GPS EC/GPS EC	2007	Nov/2006	Sep
BIRM/PTB	GPS MC	1.5	20.0	NA /GPS EC		NA /2006	Sep
CAO /PTB	GPS MC	8.0	7.0	GPS EC/GPS EC	2004	Nov/2006	Sep
CH /PTB	TWGPPP	0.3	1.0	LC(TWSTFT)/BC(GPS PPP)	2008	Sep/2009	Aug
DFNT/PTB	GPS MC	1.5	20.0	NA /GPS EC		NA /2006	Sep
IT /PTB	TWGPPP	0.3	1.2	LC(TWSTFT)/BC(GPS PPP)	2008	Sep/2009	Aug
NICT/PTB	GPSPPP	0.3	5.0	GPS EC/GPS EC	2005	Jun/2004	Aug
NIST/PTB	TWSTFT	0.3	5.0	LC(TWSTFT)/BC(GPS PPP)	2005	May/2009	Aug
OP /PTB	TWGPPP	0.3	1.1	LC(TWSTFT)/BC(GPS PPP)	2008	Sep/2009	Aug
USNO/PTB	TWSTFT	0.3	1.0	TW EC		2014	Jun

Due to the absence of correlations, the uncertainty of the pivot PTB is underestimated and unrealistically small.

Present: Odd feature 2 (dependence on one link)

CH (Bern-Wabern) 0.3 2.1 2.1 1.2.1 CMM (Queretaro) 2.0 5.3 5.7 DTAG (Frankfurt/M) 0.3 10.2 10.2 10.2 EIM (Thessaloniki) 7.5 5.3 9.2 ESTC (Noordwijk) 0.3 2.1 2.1 NICT (Tokyo) 0.3 4.9 4.9 NIST (Braunschweig) 0.1 1.8 1.8 PF (Paris) 0.3 5.3 5.0 USNO (Washington DC) 0.2 3.4 3.4 G - Time links and their uncertainties. Link Type uA/ns uB/ns CH /PTB TWGPPP 0.3 5.0 5.0 5.0 DTAG/PTB GFSPRP 0.3 1.0 CNM (Washington DC) 0.2 0.3 5.0 DTAG/PTB GFSPRP 0.3 1.0 CNM (Washington DC) 0.2 0.9 9 CH /PTB TWGPPP 0.3 5.0 Intheremotion 0.3 5.0 Intheremotion DTAG /PTB GFSPRP 0.3 5.0 Intheremotion Intheremotion Inthe	Laboratory k Uncertainty/	າຣ uA ບ	ıBu		Laboratory k Uncertainty/ns	3 UA	uB u
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KOA / FIB INGPPP 0.3 5.0	POA / DTB TWGDDD 0.3	5.0		uncertainties	OP / PTB TWGPPP 0.3	1.1	
USNU/FLD DESERFE U.S. 5.U	USNO/PTB GPSPPP 0.3	5.0			KOA / PIB IWGPPP 0.3	5.0	

Two problems: absence of correlations and not optimal use of all available data.

Proposed solution: Consider a classical estimation problem

C Y = L

Where the solution $Y = (C^T S_L^{-1} C)^{-1} (C^T S_L^{-1}) L$ is the optimal solution if redundancy (and the unique solution if no redundancy)

S_L is the input variance matrix of the measurement vector L

 $S_{Y} = (C^{T} S_{L}^{-1} C)^{-1}$ is the variance matrix of the vector Y

The variance matrix S_{γ} will directly provide the total uncertainty u of [UTC-UTC(k)] when S_{L} has been filled with both u_{A} and u_{B} .

- Approach valid for a redundant system: all available info (TW) may be used.
- GNSS measurements introduced in their original form: UTC(k) GNSStime

TEST: Proposed solution by using GNSS data wrt GNSS time scale

Example of current data used

Lab1	Ref/LAB	Туре	u _A /ns	u _B / ns
СН	PTB	TWGPPP	0.3	1
CNM	PTB	GPS MC	1	5
DTAG	PTB	GPSPPP	0.3	10
IT	PTB	GPSPPP	0.3	5
EIM	PTB	GPS MC	7.5	5
OP	PTB	TWGPPP	0.3	1
ROA	PTB	TWGPPP	0.3	5
USNO	PTB	GPSPPP	0.3	5

Example of new data proposed

Lab1	Ref/LAB	Туре	u _A /ns	u _B /ns
СН	РТВ	TWGPPP	0.3	1
CNM	GNSS	GPS MC	1	3.5
DTAG	GNSS	GPSPPP	0.3	6
IT	GNSS	GPSPPP	0.3	3.5
EIM	GNSS	GPS MC	7.5	3.5
OP	РТВ	TWGPPP	0.3	1
ROA	РТВ	TWGPPP	0.3	5
USNO	GNSS	GPSPPP	0.3	3.5
РТВ	GNSS	GPSPPP	0.3	3.5

 Least square method resolution of non-redondant system to obtain EAL wrt UTC(k)

CY = L

Design Matrix						
-1	0	0	0	0	1	
0	-1	0	0	0	1	
0	0	-1	0	1	0	
0	0	0	-1	1	0	
0	0	0	0	-1	1	
W ₁₀₀₅₇	W ₁₀₀₄₈	W ₁₀₀₁₁	W ₁₀₀₂₀	W ₁₀₀₀₅	W _{IGRT}	

	EAL - lab		Lab - REF
	EAL – 10057		10057 - IGRT
	EAL – 10048		10048 - IGRT
{	EAL – 10011	=	10011 - 10005
	EAL – 10020		10020 - 10005
	EAL – 10005		10005 - IGRT
	EAL – IGRT		Prediction

Proposed solution exemple

Resolution of previous system : C Y = L

$$Y = (C^{T} S_{L}^{-1} C)^{-1} C^{T} S_{L}^{-1} L$$

$$S_{Y}$$

$$I = Inks Variance-covariance Matrix$$

$$U_{GNSS} Cov 0 0 0 cov 0$$

$$Cov U_{GNSS} 0 0 cov 0$$

$$Cov U_{GNSS} 0 0 cov 0$$

$$0 0 0 U_{TW} 0 0 0$$

$$0 0$$

$$V_{TW} 0 0 0$$

$$0$$

$$V_{TW} 0 0$$

$$0$$

$$V_{TW} 0 0$$

$$V_{TW} 0$$

$$V_{SNSS} 0$$

$$V_{TW} 0$$

Introducing correlations: use of original GNSS data, expressed with respect to a reference timescale to which an uncertainty can be attributed

Laboratory	u - Correlated / [ns]	u - Uncorrelated / [ns]
AOS	0.27	0.33
IT	0.34	0.32
NIST	0.34	0.32
OP	0.33	0.32
PTB	0.18	0.14
USNO	0.25	0.23
SCL	5.99	6.0
ZA	1.49	1.5

The low value of the pivot in the uncorrelated case is less marked in the correlated case. Differences vary with the amount of correlation introduced.

In the case of correlated data, the total uncertainty u depends less on the USNO link quality than in the case of uncorrelated measures (all values in ns).

LAB	USNO / uB=1 ns	USNO / uB=5 ns
AOS	4.1	4.4
IT	2.0	2.6
NIST	3.8	4.1
OP	2.0	2.5
РТВ	1.7	2.3
USNO	1.8	3.8
SCL	11.3	11.5
VMI	19.8	19.9



A First application of the Kalman Filter routine to UTC (with Federica Parisi)

- The Kalman Filter is a very powerful tool used in many field. If the parameters are well estimated the KF is able to «clean» the noise affecting the data.
- We introduce the Kalman Filter as basic filter to deal with the white phase noise in time transfer system
- > We use it to build time scale.
- Many work is still necessary

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EXAMPLE: OP – PTB GPSP3 data



Test of Kalman Filter on 139 atomic clocks

- 139 atomic clocks always present without time and frequency steps are used
- EAL was calcuated only with these clocks
- KF time scale is calcuated with these clocks and with the weights used in EAL
- The only difference between EAL and KF time scale is the «prediction component»



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The effects of the new weiting algorithm are already evident in the short term stability of EAL (limited by the time transfer noise).

A new solution has been proposed to solve the odd features of the uncertainties on UTC-UTC(k).

We started a study on the use of redudant time link and on the effect on the uncertainties.

A new work on the use of the Kalman Filter for UTC has been started.

