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### BUREAU INTERNATIONAL DES POIDS ET MESURES

Statistical Summary of the Temperature Characteristics of 1  $\Omega$  and 10 k $\Omega$  Resistors Measured at the BIPM



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# Statistical Summary of the Temperature Characteristics of $1 \Omega$ and $10 k\Omega$ Resistors Measured at the BIPM

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#### I. INTRODUCTION

This report summarizes the temperature characteristics of the 1  $\Omega$  and 10 k $\Omega$  resistors measured at the BIPM, including resistors sent to the BIPM for comparisons and calibrations and the BIPM's own resistors. It is intended to provide information to aid in the consideration by the Comité Consultatif d'Electricité of values of temperatures to use as reference temperatures and as physical temperatures in the comparisons and calibrations carried out by the BIPM. The analysis of the data assumes that the temperature behavior of a standard resistor in the region within 10 K to 20 K to either side of the reference or physical temperatures is given by

$$R_{\rm t} = R_{\rm r} \left( 1 + \alpha \left( t - t_{\rm r} \right) + \beta \left( t - t_{\rm r} \right)^2 \right) \tag{1}$$

where  $R_t$  is the value of the resistance at temperature t,  $R_r$  is the value of the resistance at the reference temperature  $t_r$ ,  $\alpha$  is the linear coefficient of temperature (usually expressed in parts in 10<sup>6</sup> / K) and  $\beta$  is the quadratic coefficient of temperature (usually expressed in parts in 10<sup>6</sup> / K<sup>2</sup>). According to Eq. (1), the value of the resistance is maximum at the temperature,  $t_{max}$ , given by

$$t_{\max} = t_r - 2 \cdot \alpha / \beta \,. \tag{2}$$

This is also the temperature at which  $dR_t / dt$  is zero. The derivative of  $R_t$  is conveniently written as

$$(1/R_{\rm r}) \cdot dR_{\rm t}/dt = \alpha + 2 \cdot \beta \left(t - t_{\rm r}\right) \,. \tag{3}$$

The right side of Eq. (3) is sometimes written as  $\alpha_{tr}$ .

#### II. RESULTS

This report is concerned with 1  $\Omega$  and 10 k $\Omega$  standard resistors, the values most commonly used at the highest accuracy. Table 1 lists the relevant parameters for over 300 resistors of 1  $\Omega$  value. As the goal of this summary is to present typical results, a few outlying data were deleted. Column 1 lists the types or resistors, beginning with all types and continuing with those types most often measured at the BIPM. Column 2 gives the number of resistors in each group and column 3 lists the mean and standard deviation of the value of  $t_{max}$  for the corresponding group. Columns 4 to 6 list values of  $(1/R_r) \cdot dR_t/dt$  at three reference temperatures commonly used in electrical metrology laboratories. Clearly  $t_{max}$  is the optimal temperature to use as a reference and to physically maintain for measurement purposes. It is seen that  $t_{max}$  varies as a function of type of resistor. If a single standard temperature had to be chosen for all 1  $\Omega$  resistors, columns 4 to 6 may be helpful in choosing a temperature that would represent a compromise among various resistor types. Figure 1 presents the data for  $t_{max}$  in the form of histograms. The data have been divided into the same groups as those of Table 1. To give some appreciation of the veracity of one statistical model of the data, normal probability distributions are drawn for each group.

Table 2 lists the relevant parameters for 91 resistors of 10 k $\Omega$  values. As in the previous table, column 1 lists the types of resistors, beginning with all types and continuing with those types most often measured at the BIPM. Column 2 gives the number of resistors in each group and column 3 lists the mean and standard deviation of the value of  $t_{max}$  for the corresponding group. Columns 4 to 6 list values of  $(1/R_r) \cdot dR_t/dt$  at three reference temperatures commonly used in electrical metrology laboratories. About half of the 10 k $\Omega$  resistors are of the two types listed in rows 2 and 3. Again the values in column 3 indicate that  $t_{max}$  varies as a function of type of resistor. It should be noted that ESI model SR104 resistors are intended to be used in air. At the BIPM, they are measured in an air enclosure regulated at 20 °C. In contrast, the ZIP model P321 resistors presently are measured in an oil bath also regulated at 20 °C. Figure 2 presents histograms of the data for  $t_{max}$  for 10 k $\Omega$  resistors. The resistors are divided into the same groups as those of Table 2. Normal probability distributions are drawn for each group.

#### **III. DISCUSSION**

In view of the preceding data, the present temperature of 20°C used by the BIPM as the reference temperature for all non-thermostated resistors is too low except for 1  $\Omega$  resistors of the CSIRO type. One ohm resistors require oil baths which are expensive and voluminous so that the idea of using several baths at several different temperatures is not very attractive. A compromise temperature of 23 °C would reduce the mean temperature-related uncertainty for 1  $\Omega$  resistors by only about 40 % and would result in a mean temperature coefficient of (3.8 × 10<sup>-6</sup>) /K. For 10 k $\Omega$  resistors, a 23 °C reference temperature would reduce the mean temperature coefficient to (0.36 × 10<sup>-6</sup>) /K without increasing the uncertainty for any single type of resistor.

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## Table 1. SUMMARY OF TEMPERATURE STATISTICS ON 1 $\Omega$ RESISTORS

				(10 <sup>6</sup> x dR IR dt) / °C		(10 <sup>6</sup> x d <i>R /R</i> dt) / °C		(10 <sup>6</sup> x dR/R dt) / °C	
		t <sub>max</sub> / °C		at 20 °C		at 23 °C		at 25 °C	
TYPE(S)	NUMBER	mean	std dev	mean	std dev	mean	std dev	mean	std dev
ALL	305	26.36	6.19	6.54	5.85	3.76	5.49	1.91	5.39
L&N 4210	73	27.39	1.10	7.57	0.86	4.48	0.89	2.42	0.94
ZIP P321	39	23.65	3.15	3.47	2.65	0.46	2.75	-1.55	2.87
CSIRO (ALL)	23	20.65	3.80	-0.01	0.03	-0.10	0.11	-0.15	0.16
BZ 13	16	22.00	2.60	1.78	1.82	-1.51	2.14	-3.69	2.42

## Table 2. SUMMARY OF TEMPERATURE STATISTICS ON 10 k $\Omega$ RESISTORS

				(10 <sup>6</sup> x dR/Rdt) / °C		(10 <sup>6</sup> x dR/Rdt) / °C		(10 <sup>6</sup> x dR/Rdt) / °C	
		tmax /°C		at 20 °C		at 23 °C		at 25 °C	
TYPE(S)	NUMBER	mean	std dev	mean	std dev	mean	std dev	mean	std dev
ALL	91	24.32	4.84	1.43	3.78	0.36	3.43	-0.36	3.49
ESI SR104	32	23.09	3.20	0.14	0.13	-0.01	0.12	-0.11	0.12
ZIP P331	15	27.32	8.06	6.02	5.23	3.28	5.28	1.45	5.37











**Figure 1.** Histograms of the values of  $t_{max}$ , the temperature for which dR/dt = 0, for 1  $\Omega$  resistors measured at the BIPM; A) all resistors; B) L&N model 4210; C) ZIP model 321; D) CSIRO, all types; and E) BZ model 13.

L&N model 4210



12 18



**Figure 2.** Histograms of the values of  $t_{max}$ , the temperature for which dR/dt = 0, for 10 k $\Omega$  resistors measured at the BIPM; A) all resistors; B) ESI model SR104; C) ZIP model P331.