## **BUREAU INTERNATIONAL DES POIDS ET MESURES**

## DETERMINATION OF THE DIFFERENTIAL TIME CORRECTIONS FOR GPS TIME EQUIPMENT LOCATED AT THE OP and CH

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### Abstract

The BIPM continues a series of differential calibrations of GPS equipment located in time laboratories contributing to TAI. This report details measurements which took place from 16 October 2003 to 2 February 2004, involving GPS time equipment located at the Observatoire de Paris (OP, Paris, France) and the Metrology and Accreditation Switzerland (CH, Bern, Swiss).

#### **INTRODUCTION**

The BIPM is conducting a series of differential calibrations of GPS equipment located in time laboratories contributing to TAI [1].

As for previous comparisons the GPS time equipment located at the OP was chosen as reference. To check the reproducibility of the measurements, the calibrations were organized as round trips beginning and ending at the OP. It has often served in the past as reference laboratory for GPS calibrations. Over the last twenty years the OP's GPS time receiver has been compared several times with the NIST absolutely-calibrated reference GPS time receiver. The difference between these two has never exceeded a few nanoseconds.

Repeated determinations of the differential time corrections for the GPS time equipment located in the various laboratories should:

- improve the accuracy of the access to UTC of participating laboratories;
- provide valuable information about the stability of GPS time equipment;
- serve as provisional differential calibrations of the two-way equipment at the laboratories.

This report details an exercise which took place from 16 October 2003 to 2 February 2004. Succeeding visits are scheduled to take place at four to five month intervals.

#### **EQUIPMENT**

Details of the receivers involved are provided in Table 1. More information about the set-up of equipment at each location is provided in Appendix I.

Table 1. GPS equipment involved in this comparison.

Laboratory	Receiver Maker	Receiver Type	Receiver Ser. No
OP	AOA	TTR-5	051
СН	AOA	TTR-5a	275
BIPM H portable receiver	AOS	TTS-2	021

The portable BIPM H receiver is equipped with a C101 cable. Its delay measured at the BIPM is 179.0 ns with a standard deviation of 0.5 ns.

This delay was measured using a double-weight pulse method with a time interval counter steered by an external frequency source (an Active Hydrogen Maser CH1-75, KVARZ). We measured at the beginning of the linear part of the rising pulse at each end of the cable using a 0.5 V trigger level [2].

The delay of this cable was also measured at the laboratories visited. The results are reported in Appendix II.

### **CONDITIONS OF COMPARISON**

For the present comparison, the portable equipment comprised the receiver, its antenna and a calibrated antenna cable. The laboratories visited supplied: (a) a 10 MHz reference signal; and (b) a series of 1 s pulses from the local reference, UTC(k), via a cable of known delay. In each laboratory, the portable receiver was connected to the same clock as the local receiver and the antenna of the portable receiver was placed close to the local antenna. The differential coordinates of the antenna phase centres were known at each site with standard uncertainties (1 $\sigma$ ) of a few centimetres.

#### RESULTS

The processing of the comparison data obtained in laboratory k consists first of computing, for each track i, the time differences:

 $dt_{k,i} = [UTC(k) - GPS time]_{BIPM,i} - [UTC(k) - GPS time]_{k,i}.$ 

The noise exhibited by the time series  $dt_k$  is then analysed, for each of the laboratories visited, by use of the modified Allan variance. In each case, white phase noise was exhibited up to an averaging interval of about one day. We illustrate this in Figure 1.



**Figure 1**. Square root of the modified Allan variance of the time series  $dt_{CH}$  for the period: 17 December 2003 to 12 January 2004.

The one-day averages are reported in Figure 2 and Appendix III. The level of noise for oneday averaging period is reported in Table 2.



[REF(Labk) – GPS time] <sub>BIPM</sub> – [REF(Labk) – GPS time] <sub>Labk</sub>

**Figure 2.** Daily averages of  $dt_{k,i}$  for each laboratory k (see Appendix III).

Next, we computed mean offsets for the full duration of comparison at each location, and the corresponding standard deviations of individual common view measurements (see Table 2).

Table 2. Mean offsets for the full duration of the comparison at each location.

Lab	Period	Total	Mean	Standard	Level of	Dispersion
		number	offset	deviation of	noise	of daily
k		of	/ns	individual	for 1 day	mean
		commo		common view	/ns	/ns
		n views		observations		
				/ns		
OP	16/10/03 - 21/10/03	220	8.45	2.54	0.3	0.58
СН	30/10/03 - 16/01/04	1624	40.59	3.03	0.4	1.16
OP	28/01/04 - 02/02/04	218	7.85	2.68	0.5	0.63

The "closure" – the difference between the first and last sets of measurements made at the OP – was within one nanosecond, which is an excellent result. After averaging the results of the two sets of measurements at the OP, we then derived differential time correction which should be made (added) to time difference derived during the GPS comparison of the time scales kept by the visited laboratories. The results are summarized in Table 3.

**Table 3.** Differential time correction *d* to be added to  $[UTC(k_1) - UTC(k_2)]$ , and its estimated uncertainty u(d) for the period of comparison (1 $\sigma$ ).

$[UTC(k_1) - UTC(k_2)]$	d/ns	<i>u</i> ( <i>d</i> )/ns
[UTC(CH) - UTC(OP)]	+32.4	3.0

The uncertainty given in this table is conservative. It is mainly driven by the uncertainty due to the 'round-trip' reproducibility at the OP.

### CONCLUSION

These measurements are part of a series of differential calibrations of GPS equipment located in time laboratories contributing to TAI. They improve the accuracy of the access to UTC of the participating laboratories.

The present measurements were performed under good conditions with excellent closure of the travelling equipment at the OP. At the CH, the differential correction is large, and readjustment of the delay of GPS time equipment might be considered.

### Acknowledgements

The authors wish to express their gratitude to Laurent-Guy Bernier for the unreserved collaboration they have received. Without this help, the work could not have been accomplished.

### References

- [1] W. Lewandowski, P. Moussay, "Determination of the differential time corrections for GPS time equipment located at the OP, IEN, ROA, PTB, NIST, and USNO", *BIPM Report -2002/02*, July 2002.
- [2] G. de Jong, "Measuring the propagation time of coaxial cables used with GPS receivers," *Proc. 17th PTTI*, pp. 223-232, December 1985.

# Appendix I

Set-ups of local and portable equipment at each location (forms completed by the participating laboratories)

Laboratory:		BNM – SYRTE, Observatoire de Paris				
Date and hour of the beginning of	measurements:	16 October 2003				
Date and hour of the end of measurements:		21 October 2003				
Receiver setup information						
Local: NBS 51		1	Portable: BIPM H			
• Maker:	Allen Osborne Associates		AOS			
• Type:	TTR-5		TTS-2			
• Serial number:	051		S/N 021			
• Receiver internal delay (GPS) :	54 ns		-19.36			
• Receiver internal delay (GLO) :	-		-			
• Antenna cable identification:	505 IF		C101			
Corresponding cable delay :	$168 \text{ ns} \pm 0.3 \text{ ns}$	5	$179.0 \text{ ns} \pm 0.5 \text{ ns}$			
• UTC cable identification:	503		497			
Corresponding cable delay :	-		-			
Delay to local UTC :	304 ns		306 ns			
• Receiver trigger level:	0.5 V		0.5 V			
Coordinates reference frame:	ITRF		ITRF			
Latitude or X m 4 202 780.30 m		n	4 202 783.64 m			
Longitude or Y m 171 370.03 m			171 367.43 m			
Height or Z m 4 778 660.12 m		n	4 778 657.38 m			
Antenna information						
Local:			Portable:			
• Maker:	A.O.A.					
• Type:	-					
• Serial number:	-		-			
If the antenna is temperature stabil	ised					
• Set temperature value :	-		-			
Loca	antenna ca	able inforn	nation			
• Maker:			/			
• Type:		RG-58				
• Is it a phase stabilised cable:		No				
• Length of cable outside the build	ing :	Approximately 6 meters				
	General in	formation				
• Rise time of the local UTC pulse	:		4 ns			
• Is the laboratory air conditioned	!:	Yes				
• Set temperature value and uncert	ainty :	(21.5 ± 2) °C				
• Set humidity value and uncertain	ty:		/			
	Cable dela	ay control				
Cable identification	delay measu	red by BIPM	Delay measured by local method			
BIPM C101 179.0 ns		$\pm 0.5$ ns	_			

# **BIPM GPS calibration information sheet**





The method used to calibrate the cables is a double wheight method in five steps as shown above. At each step (i) the TIC gives the result ( $R_i$ ) of 100 measurments. The test cable delay is then obtained by the following formula:  $\begin{pmatrix} R + R \end{pmatrix} \begin{pmatrix} R + R \end{pmatrix}$ 

$$Delay = \frac{R_2 - \left(\frac{R_1 + R_3}{2}\right) + \left(\frac{R_3 + R_5}{2}\right) - R_4}{2} + corrections$$
  
The corrections are the estimated delay introduced by adaptators : - 0.1 ns / adaptator

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Laboratory:		CH (METAS, Bern, Switzerland)					
Date and hour of the beginning of	measurements:	2003-12-16 Tue MJD 52989 UTC 09:00					
Date and hour of the end of measur	rements:	2004-01-12 Mon MJD 53016 UTC 10:00					
Receiver setup information							
	Local:		Portable: BIPM H				
• Maker:	AOA		BIPM				
• Type:	TTR-5A		TTS-2				
• Serial number:	S/N 275		S/N 021 (BIPH)				
• Receiver internal delay (GPS) :	not cal. (INT I	DLY = 73  ns)	-19.36 ns				
• Receiver internal delay (GLO) :			-				
• Antenna cable identification:	KA-KR #12		C101				
Corresponding cable delay :	$208.0\pm0.5\ ns$		$179.0 \text{ ns} \pm 0.5 \text{ ns}$				
• UTC cable identification:	KA-KA#34		KA-KA#19				
Corresponding cable delay :	38.2 ns		50.6 ns				
Delay to local UTC :	REF-PPS(TTR	(-5A) = 0.0  ns	REF-PPS(BIPM) = +8.1  ns				
• Receiver trigger level:	unknown		0.5 V				
• Coordinates reference frame:	ITRF 2000		ITRF 2000				
Latitude or X m 46° 55' 25.430		)51"	46° 55' 25.488228''				
Longitude or Y m 7° 27' 51.2908		??	7° 27' 51.3027"				
Height or Z m 611.60			612.643				
Antenna information							
	Local:		Portable:				
• Maker:	AOA						
• Type:	TTR-5A						
• Serial number:	0600		TTS-2 serial 021				
If the antenna is temperature stabil	ised						
• Set temperature value :							
Local	antenna ca	able inforn	nation				
• Maker:			Andrew				
• Type:		HELIAX ¼" FSJ1-50A					
• Is it a phase stabilised cable:		very low temperature sensitivity					
• Length of cable outside the build	ing :	about 10 m					
	General in	formation					
• Rise time of the local UTC pulse	:	14 ns to TTR-5A, 10 ns to BIPM					
• Is the laboratory air conditione	d:	yes					
• Set temperature value and uncert	ainty :	21.0 ± 0.5 °C					
• Set humidity value and uncertain	ty :		50 ± 5 %				
	Cable dela	av control					
Cable identification	delay measu	red by BIPM   Delay measured by local metho					
BIPM C101	BIPM C101 179.0 ns		$179.4 \text{ ns} \pm 0.5 \text{ ns}$				

# **BIPM GPS calibration information sheet**





Laboratory:		BNM – SYRTE, Observatoire de Paris					
Date and hour of the beginning of	measurements:	28 January 2004					
Date and hour of the end of measur	rements:	02 February 2004					
Receiver setup information							
Local: NBS 51			Portable: BIPM H				
• Maker:	Allen Osborne	Associates	AOS				
• Type:	TTR-5		TTS-2				
• Serial number:	051		S/N 021				
• Receiver internal delay (GPS) :	54 ns		-19.36				
• Receiver internal delay (GLO) :	-		-				
• Antenna cable identification:	505 IF		C101				
Corresponding cable delay :	$168 \text{ ns} \pm 0.3 \text{ ns}$	5	$179.0 \text{ ns} \pm 0.5 \text{ ns}$				
• UTC cable identification:	503		497				
Corresponding cable delay :	-		-				
Delay to local UTC :	304 ns		306 ns				
Receiver trigger level:	0.5 V		0.5 V				
Coordinates reference frame:	ITRF		ITRF				
Latitude or X m 4 202 780.30 m		n	4 202 783.64 m				
Longitude or Y m 171 370.03 m			171 367.43 m				
Height or Z m	Height or Z m 4 778 660.12 m		4 778 657.38 m				
Antenna information							
	Antenna in	formation	L				
	Antenna in Local:	formation	Portable:				
• Maker:	Antenna in Local: A.O.A.	formation	Portable:				
• Maker: • Type:	Antenna in Local: A.O.A. -	formation	Portable:				
<ul> <li>Maker:</li> <li>Type:</li> <li>Serial number:</li> </ul>	Antenna in Local: A.O.A. - -	formation	Portable:				
<ul> <li>Maker:</li> <li>Type:</li> <li>Serial number:</li> <li>If the antenna is temperature stabil</li> </ul>	Antenna in Local: A.O.A. - - ised	formation	Portable:				
<ul> <li>Maker:</li> <li>Type:</li> <li>Serial number:</li> <li>If the antenna is temperature stabil</li> <li>Set temperature value :</li> </ul>	Antenna in Local: A.O.A. - - ised -	formation	Portable:           -           -           -				
<ul> <li>Maker:</li> <li>Type:</li> <li>Serial number:</li> <li>If the antenna is temperature stabil</li> <li>Set temperature value :</li> </ul>	Antenna in Local: A.O.A. - - ised - antenna ca	formation	Portable: -				
<ul> <li>Maker:</li> <li>Type:</li> <li>Serial number:</li> <li>If the antenna is temperature stabil</li> <li>Set temperature value :</li> <li>Local</li> <li>Maker:</li> </ul>	Antenna in Local: A.O.A. - - ised - antenna ca	formation	Portable: - - nation /				
<ul> <li>Maker:</li> <li>Type:</li> <li>Serial number:</li> <li>If the antenna is temperature stabil</li> <li>Set temperature value :</li> <li>Local</li> <li>Maker:</li> <li>Type:</li> </ul>	Antenna in Local: A.O.A. - - ised - antenna ca	tormation	Portable: - - nation / RG-58				
<ul> <li>Maker:</li> <li>Type:</li> <li>Serial number:</li> <li>If the antenna is temperature stabil</li> <li>Set temperature value :</li> <li>Local</li> <li>Maker:</li> <li>Type:</li> <li>Is it a phase stabilised cable:</li> </ul>	Antenna in Local: A.O.A. - - ised - <b>antenna ca</b>	tormation	Portable: - - nation / RG-58 No				
<ul> <li>Maker:</li> <li>Type:</li> <li>Serial number:</li> <li>If the antenna is temperature stabil</li> <li>Set temperature value :</li> <li>Local</li> <li>Maker:</li> <li>Type:</li> <li>Is it a phase stabilised cable:</li> <li>Length of cable outside the build</li> </ul>	Antenna in Local: A.O.A. - - ised - <b>antenna ca</b>	able inform	Portable: Portable: - - nation / RG-58 No Approximately 6 meters				
<ul> <li>Maker:</li> <li>Type:</li> <li>Serial number:</li> <li>If the antenna is temperature stabil</li> <li>Set temperature value :</li> <li>Local</li> <li>Maker:</li> <li>Type:</li> <li>Is it a phase stabilised cable:</li> <li>Length of cable outside the build</li> </ul>	Antenna in Local: A.O.A. - - ised - antenna ca ing : General in	tormation	Portable: Portable: - - nation / RG-58 No Approximately 6 meters				
<ul> <li>Maker:</li> <li>Type:</li> <li>Serial number:</li> <li>If the antenna is temperature stabil</li> <li>Set temperature value :</li> <li>Local</li> <li>Maker:</li> <li>Type:</li> <li>Is it a phase stabilised cable:</li> <li>Length of cable outside the build</li> <li>Rise time of the local UTC pulse</li> </ul>	Antenna in Local: A.O.A. - - ised - antenna ca ing : General in	able inform ble inform	Portable: Portable: nation / RG-58 No Approximately 6 meters 4 ns				
<ul> <li>Maker:</li> <li>Type:</li> <li>Serial number:</li> <li>If the antenna is temperature stabil</li> <li>Set temperature value :</li> <li>Local</li> <li>Maker:</li> <li>Type:</li> <li>Is it a phase stabilised cable:</li> <li>Length of cable outside the build</li> <li>Rise time of the local UTC pulse</li> <li>Is the laboratory air conditioned</li> </ul>	Antenna in Local: A.O.A. - - ised - antenna ca ing : General in :	able inform	Portable: Portable: - - nation / RG-58 No Approximately 6 meters 4 ns Yes				
<ul> <li>Maker:</li> <li>Type:</li> <li>Serial number:</li> <li>If the antenna is temperature stabil</li> <li>Set temperature value :</li> <li>Local</li> <li>Maker:</li> <li>Type:</li> <li>Is it a phase stabilised cable:</li> <li>Length of cable outside the build</li> <li>Rise time of the local UTC pulse</li> <li>Is the laboratory air conditioned</li> <li>Set temperature value and uncert</li> </ul>	Antenna in Local: A.O.A. - - ised - <b>antenna ca</b> ing : General in : : ainty :	tormation	Portable:         -         -         nation         /         RG-58         No         Approximately 6 meters         4 ns         Yes         (21.5 ± 2) °C				
<ul> <li>Maker:</li> <li>Type:</li> <li>Serial number:</li> <li>If the antenna is temperature stabil</li> <li>Set temperature value :</li> <li>Local</li> <li>Maker:</li> <li>Type:</li> <li>Is it a phase stabilised cable:</li> <li>Length of cable outside the build</li> <li>Rise time of the local UTC pulse</li> <li>Is the laboratory air conditioned</li> <li>Set temperature value and uncertain</li> </ul>	Antenna in Local: A.O.A ised - ised antenna ca ing : General in : : ainty : ty :	able inform	Portable:         -         -         nation         /         RG-58         No         Approximately 6 meters         4 ns         Yes         (21.5 ± 2) °C         /				
<ul> <li>Maker:</li> <li>Type:</li> <li>Serial number:</li> <li>If the antenna is temperature stabil</li> <li>Set temperature value :</li> <li>Local</li> <li>Maker:</li> <li>Type:</li> <li>Is it a phase stabilised cable:</li> <li>Length of cable outside the build</li> <li>Rise time of the local UTC pulse</li> <li>Is the laboratory air conditioned</li> <li>Set temperature value and uncertain</li> </ul>	Antenna in Local: A.O.A. - - ised - antenna ca ing : General in : : ainty : ty : Cable dela	formation	Portable:         -         - $ation$ /         RG-58         No         Approximately 6 meters         4 ns         Yes         (21.5 ± 2) °C         /				
<ul> <li>Maker:</li> <li>Type:</li> <li>Serial number:</li> <li>If the antenna is temperature stabil</li> <li>Set temperature value :</li> <li>Local</li> <li>Maker:</li> <li>Type:</li> <li>Is it a phase stabilised cable:</li> <li>Length of cable outside the build</li> <li>Rise time of the local UTC pulse</li> <li>Is the laboratory air conditioned</li> <li>Set temperature value and uncertain</li> <li>Cable identification</li> </ul>	Antenna in Local: A.O.A. - - ised - antenna ca ing : General in : : ainty : ty : Cable dela delay measure	formation	Portable:         -         -         nation         /         RG-58         No         Approximately 6 meters         4 ns         Yes         (21.5 ± 2) °C         /         Delay measured by local method				

## **BIPM GPS calibration information sheet**





The method used to calibrate the cables is a double wheight method in five steps as shown above. At each step (i) the TIC gives the result (R<sub>i</sub>)of 100 measurments. The test cable delay is then obtained by the following formula:  $R_2 - \left(\frac{R_1 + R_3}{2}\right) + \left(\frac{R_3 + R_5}{2}\right) - R_4$ 

$$Delay = \frac{R_2 - \left(\frac{R_1 + R_3}{2}\right) + \left(\frac{R_3 + R_5}{2}\right) - R_4}{2} + corrections$$

The corrections are the estimated delay introduced by adaptators : - 0.1 ns / adaptator

# <u>Appendix II</u>

# Measurement of portable cables at the visited laboratories

Laboratory	BIPM C101 cable	<b>Measurement method</b>	
	/ns		
BIPM	$179.0\pm0.5$	Double Weight Pulse method	
OP (before trip)	—		
СН	$179.4 \pm 0.5$	Pulse method	
OP (after trip)	—		

# <u>Appendix III</u>

# Daily averages of $dt_{k,i}$ for each laboratory k

LAB	MJD	Mean	Standard deviation of	Standard	Number of
		offset	individual common	deviation of	individual common
k			view observations	the mean	views
		/ns	/ns	/ns	
OP	52928	9.00	2.71	0.53	26
	52929	8.79	2.84	0.42	45
	52930	8.40	2.31	0.35	44
	52931	8.30	2.32	0.35	45
	52932	8.49	2.38	0.36	44
	52933	7.36	3.04	0.74	17
СН	52942	40.68	1.88	0.37	26
	52943	38.23	2.82	0.51	31
	52944	37.87	2.43	0.41	35
	52945	40.04	2.86	0.46	38
	52946	39.21	2.26	0.36	40
	52947	40.01	2.68	0.43	38
	52948	40.51	3.76	0.59	41
	52949	40.78	2.52	0.39	41
	52983	41.48	2.80	0.53	28
	52984	40.50	2.32	0.37	40
	52985	41.12	2.91	0.46	40
	52986	41.16	3.29	0.51	41
	52987	41.59	2.40	0.38	41
	52988	40.85	2.29	0.36	40
	52990	40.81	2.22	0.36	38
	52991	40.35	2.40	0.39	39
	52992	40.87	2.99	0.46	42
	52993	41.58	2.35	0.37	41
	52994	41.44	2.29	0.37	38
	52995	39.87	2.60	0.41	40
	52996	40.38	2.85	0.46	39
	52997	39.94	2.37	0.37	41
	52998	40.05	2.82	0.44	42
	52999	40.22	2.66	0.43	39
	53000	40.93	2.08	0.34	38
	53001	41.14	2.34	0.38	39
	53002	40.78	2.90	0.45	41
	53003	41.10	2.81	0.44	41
	53004	41.45	2.71	0.45	37
	53005	41.88	3.52	0.57	38
	53006	41.05	1.90	0.31	38
	53007	40.94	2.94	0.46	40
	53008	40.69	2.52	0.40	39
	53009	41.41	2.23	0.35	41
	53010	40.61	2.63	0.41	42
	53011	40.69	2.63	0.42	39
	53012	40.53	2.27	0.37	37
	53013	41.37	2.44	0.38	41
	53014	41.71	2.40	0.39	37
	53015	41.58	2.25	0.36	39
	53016	39.78	2.52	0.73	12

ſ	OP	53032	8.30	2.93	0.55	28
		53033	6.65	2.67	0.40	45
		53034	8.34	1.98	0.30	43
		53035	8.07	3.05	0.45	45
		53036	8.05	2.47	0.37	44
		52937	8.01	2.73	0.73	14